

# GALAXY FORMATION



**Joe Silk**  
**IAP/Oxford**  
**Dublin July 2011**



# SUMMARY OF LECTURE 2

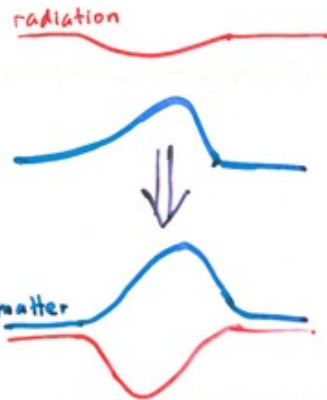
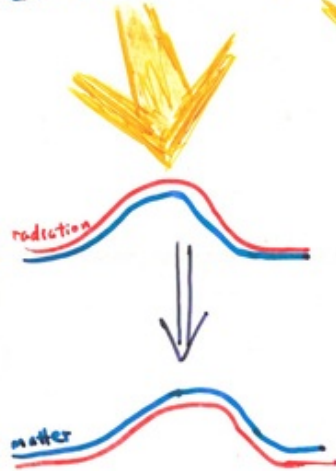
- Linear theory of density fluctuations
- Non-linear theory
- Galaxy luminosity function
- Disk galaxy formation
- Spheroidal galaxy formation
- Feedback
- Cold flows
- First star formation

# FLUCTUATION MODES

**SCALAR**  
 ↓  
 Curvature      entropy

**VECTOR**  
 ↓  
 vorticity  
 ↓  
 decays

**TENSOR**  
 ↓  
 gravitational waves  
 ↓  
 incompressible;  
 decay (M-D)



$$\begin{aligned}
 \rho_r a^4 &= \text{const} \\
 \rho_m a^3 &= \text{const} \\
 + \delta S &= 0 \\
 \uparrow \\
 \delta \left( \frac{\rho_r}{\rho_m} \right) &= 0
 \end{aligned}$$

$$\frac{\delta \rho_m}{\rho_m} = \frac{3}{4} \frac{\delta \rho_r}{\rho_r}$$

constant entropy:  
 predicted if  $\frac{n_b}{n_\gamma} = \text{const}$   
 inflation  
 (and baryogenesis)

$$\delta \rho_m + \delta \rho_r = 0$$

primordial  
 isocurvature or entropy  
 fluctuations (eg. phase transition)

$$\frac{\delta \rho_m}{\rho_m} = \frac{\rho_r}{\rho_m} \delta S$$

$$\frac{\delta \rho_r}{\rho_r} = \frac{\delta \rho_m}{\rho_m}$$

# NEWTONIAN ANALYSIS $(\lambda \ll ct, v \ll c)$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot [(\rho + P)\vec{V}] = 0,$$

$$\frac{\partial \vec{V}}{\partial t} + (\vec{V} \cdot \nabla)\vec{V} = -\frac{\rho}{\rho + P}\nabla\Phi - \frac{1}{\rho + P}\nabla P$$

$$\nabla^2\Phi = 4\pi G(\rho + 3P)$$

$$\frac{\ddot{a}}{a} = -4\pi G(\rho + 3p/c^2)$$

$$\rho a^3 = \text{constant}$$

Linearize about Friedmann background

Define comoving coordinate :  $X = \frac{\text{physical coordinate}}{a(t)} = \frac{r}{a}$



Eliminate  $\phi$  via Poisson eqn,  $\nabla$  via continuity eqn,

$$\delta \equiv \delta\rho/\rho$$

$$\frac{\partial^2}{\partial t^2} \delta + 2\frac{\dot{a}}{a} \frac{\partial}{\partial t} \delta = 4\pi G\rho\delta + \frac{1}{a^2} \frac{d\rho}{d\rho} \nabla^2 \delta$$

Hubble damping

Self-gravity  
destabilizes

pressure  
gradient  
stabilizes

Let  $\delta(x,t) = \sum \delta_k \exp(i\mathbf{k}\cdot\mathbf{x})$

Define physical wavelength  $\lambda = 2\pi \frac{a}{k}$

UNSTABLE IF  $\lambda > \lambda_J = c_s \left( \frac{\pi}{G\rho_0} \right)^{\frac{1}{2}}$   $c_s^2 = \frac{\nabla\delta P}{\nabla\delta\rho}$

GROWTH RATE :  $\delta \propto t^{2/3}, t^{-1}$  (matter domination)

allows density fluctuation growth when  $\rho_m > \rho_{rad}$

$$\frac{d^2 \delta_m}{dt^2} + 2\frac{\dot{a}}{a} \frac{d\delta_m}{dt} = 4\pi G \rho_m \delta_m$$

$$\Rightarrow \delta_m \equiv \frac{\delta \rho_m}{\rho_m} = 1 + \frac{3}{2} \frac{\rho_m}{\rho_{rad}}$$

$$\delta K \sim \frac{G \delta M}{L c^2} \sim G \frac{\delta \rho L^2}{c^2}$$

$$\sim \left( \frac{\delta \rho}{\rho} \right) \left( \frac{L}{ct} \right)^2$$

$$\frac{\delta \rho}{\rho} \sim \delta K \left[ \frac{ct}{a(t)} \right]^2 \left( \frac{a(t)}{L} \right)^2$$

$$\propto t^{2/3} M^{-2/3}$$

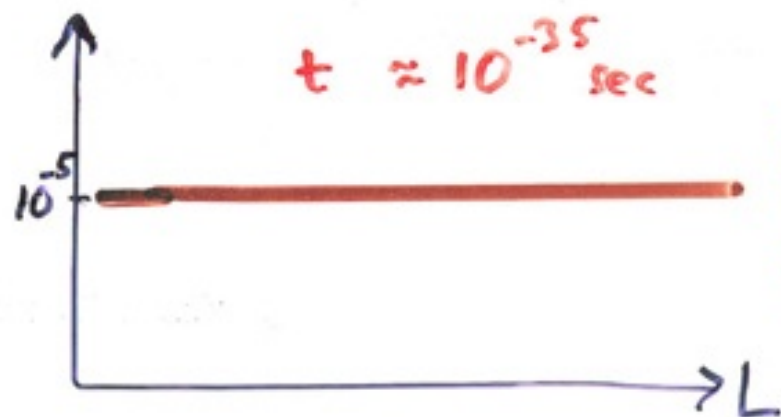
COMOVING

for  $a \propto t^{2/3}$   
(matter-dominated regime)

if  $\delta K = \text{constant}$   
 $\uparrow$   
 scale invariance: { Harrison, Zeldovich  
 Inflation

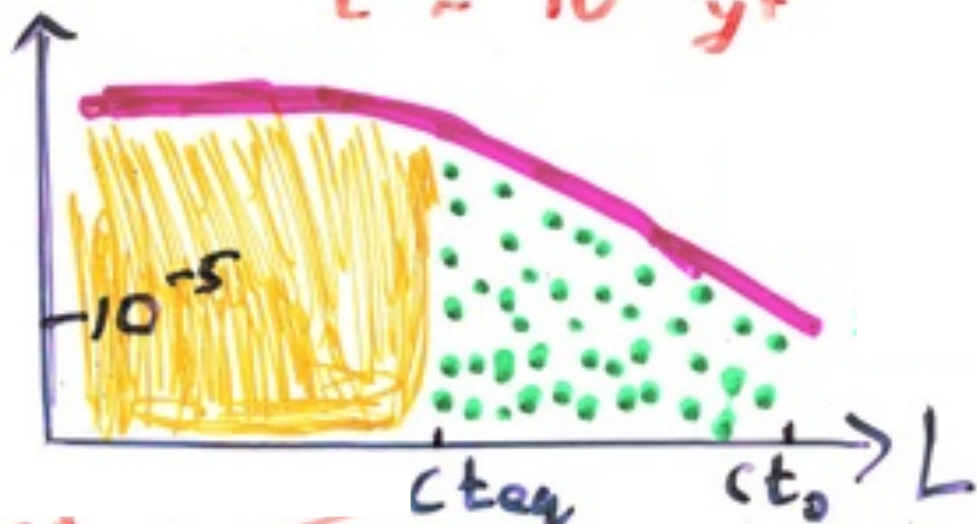
INFLATION

$\delta K$   
curvature



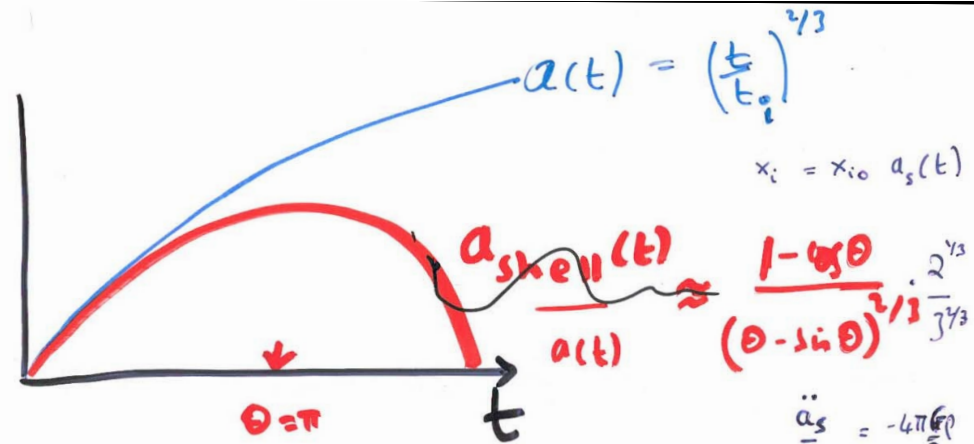
primordial  
metric  
fluctuations

$\delta e/p$





# spherical top hat



$$\frac{\ddot{a}_s}{a_s} = -\frac{4\pi G \rho}{3} = -\frac{4\pi G \rho_0 (1+z)^3}{3}$$

$$\frac{\rho_{max\ expansion}}{\rho} = \frac{9\pi^2}{16}$$

$$a_s = \frac{1 - \cos \theta}{2\delta}$$

$$t/t_i = \frac{3}{4} \frac{\theta - \sin \theta}{\delta^{3/2}}$$

$$\text{at } \frac{t}{t_i} = \frac{3\pi}{8} \frac{1}{\delta_i^{3/2}}$$

FINAL RADIUS (no dissipation)

$$= \frac{1}{2} R_{max}$$

galaxy "formation" epoch  
 $= \frac{3\pi}{4} \delta_i^{-3/2} t_i$

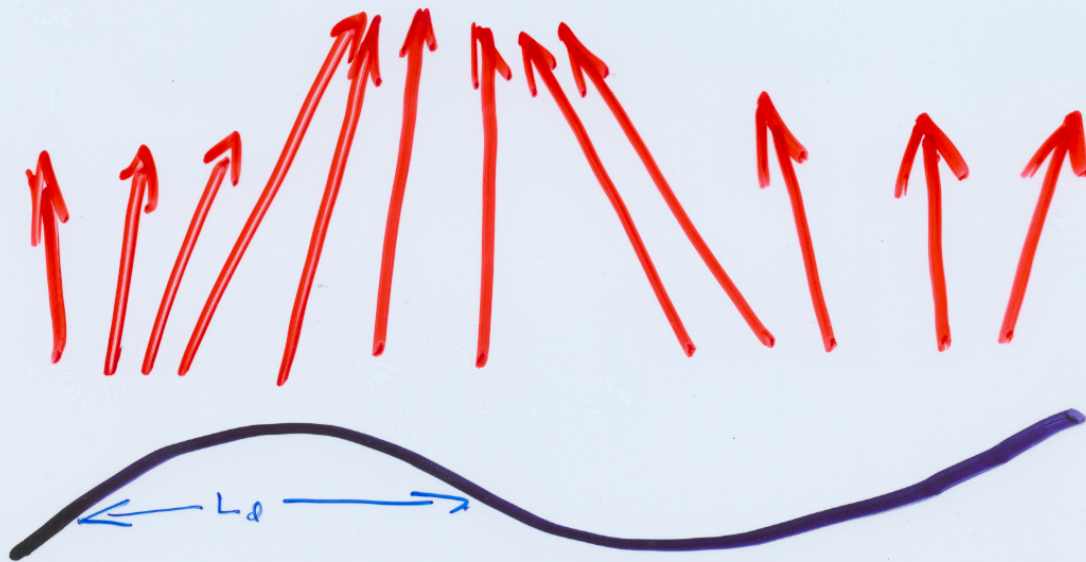
FINAL (  $t_{virialization} = 2 t_{Rmax}$  )

$$\frac{\rho_{virial}}{\rho(t_{virial})} = \frac{9\pi^2}{16} \times \frac{8}{1/4} = 18\pi^2$$

pancake

1-D solution (Zel'dovich)

$$Z(t, z_i) = a(t) \left[ z_i - \frac{a(t)}{a_p} \sin\left(\frac{\pi z_i}{L_d}\right) \right]$$



velocity perturbation

1-D trajectories

Caustic develops

$$\rho = \frac{\rho_0}{1 - \frac{a(t)}{a_p} \cos\left(\frac{\pi z_i}{L_d}\right)}$$

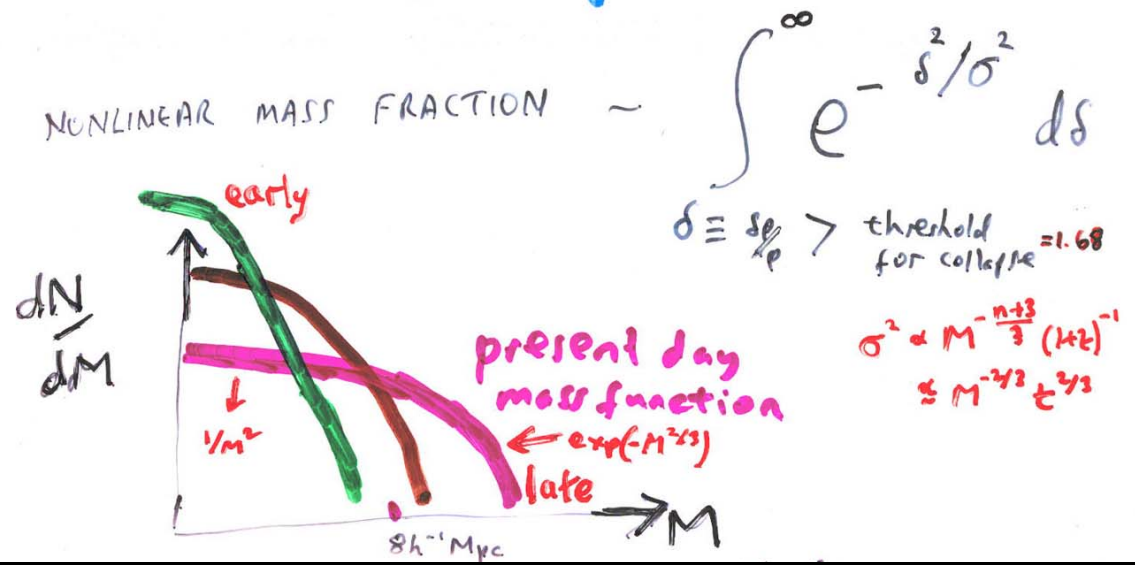
$\langle (\delta\rho/\rho)^2 \rangle_{\text{mass}}^{1/2} \equiv \sigma(M) \propto t^{2/3} \quad (\text{if } \Omega=1)$

$\langle (\delta\rho/\rho)^2 \rangle_{\text{light}}^{1/2} \text{ at } z=0 \sim 1$  averaged over  $8h^{-1}\text{Mpc}$  spheres if  $\Omega_m \leq 1$   $\Rightarrow$  need larger  $C$  at specified  $M$

*growth suppressed at  $1+z < 1/\Omega_m$*

calculate number of newly non-linear objects

sensitive to gaussian tail i.e. rare peaks





A visualization of the Millennium Simulation, showing a dense network of dark purple and blue filaments and nodes representing the cosmic web. The structure is highly interconnected and fractal-like. A horizontal scale bar is located at the top left, with the text "1 Gpc/h" above it. The text "Millennium Simulation" and "10.077.696.000 particles" is centered in the upper half. The text "(z = 0)" is in the bottom left corner.

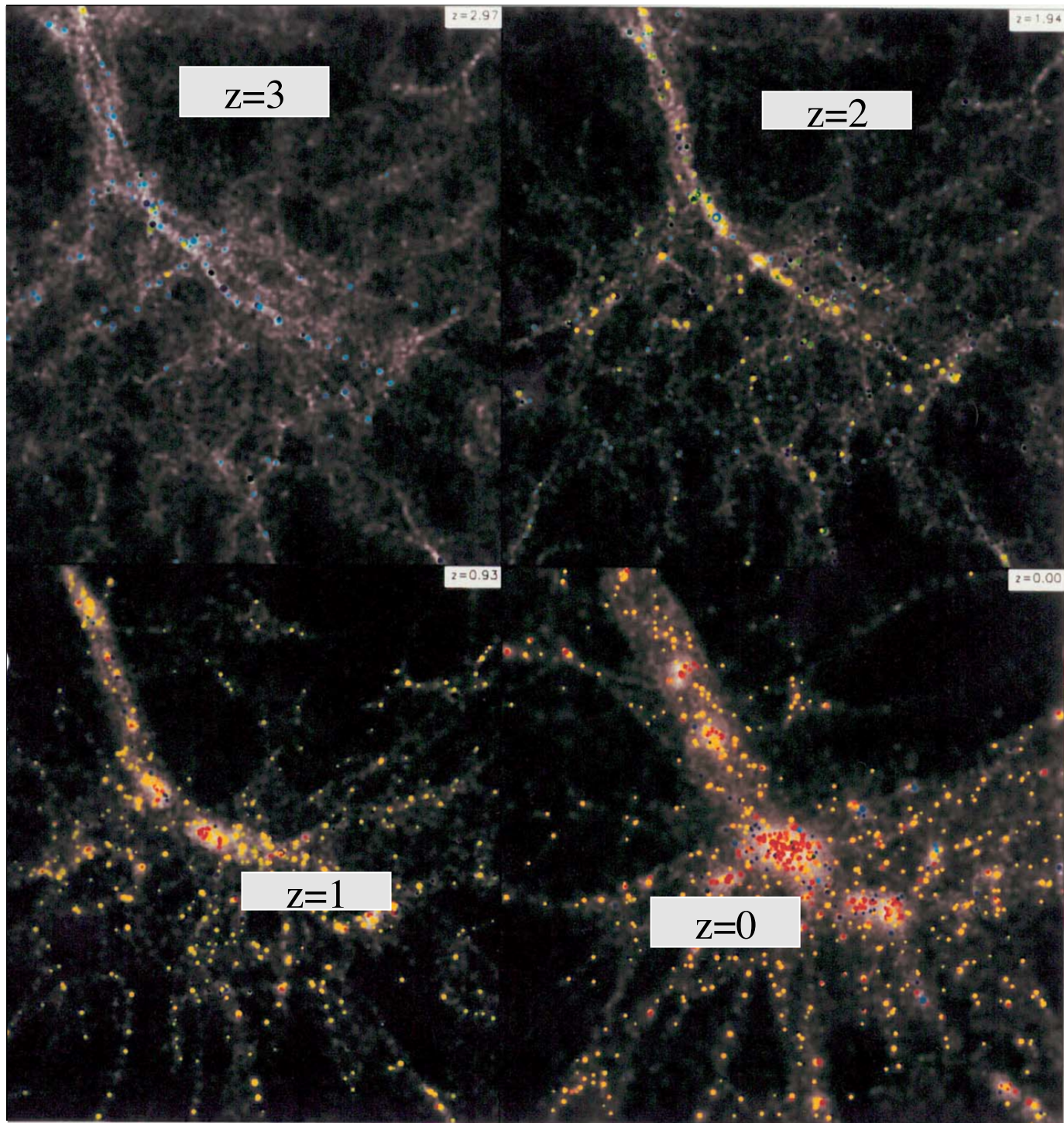
1 Gpc/h

Millennium Simulation

10.077.696.000 particles

( $z = 0$ )

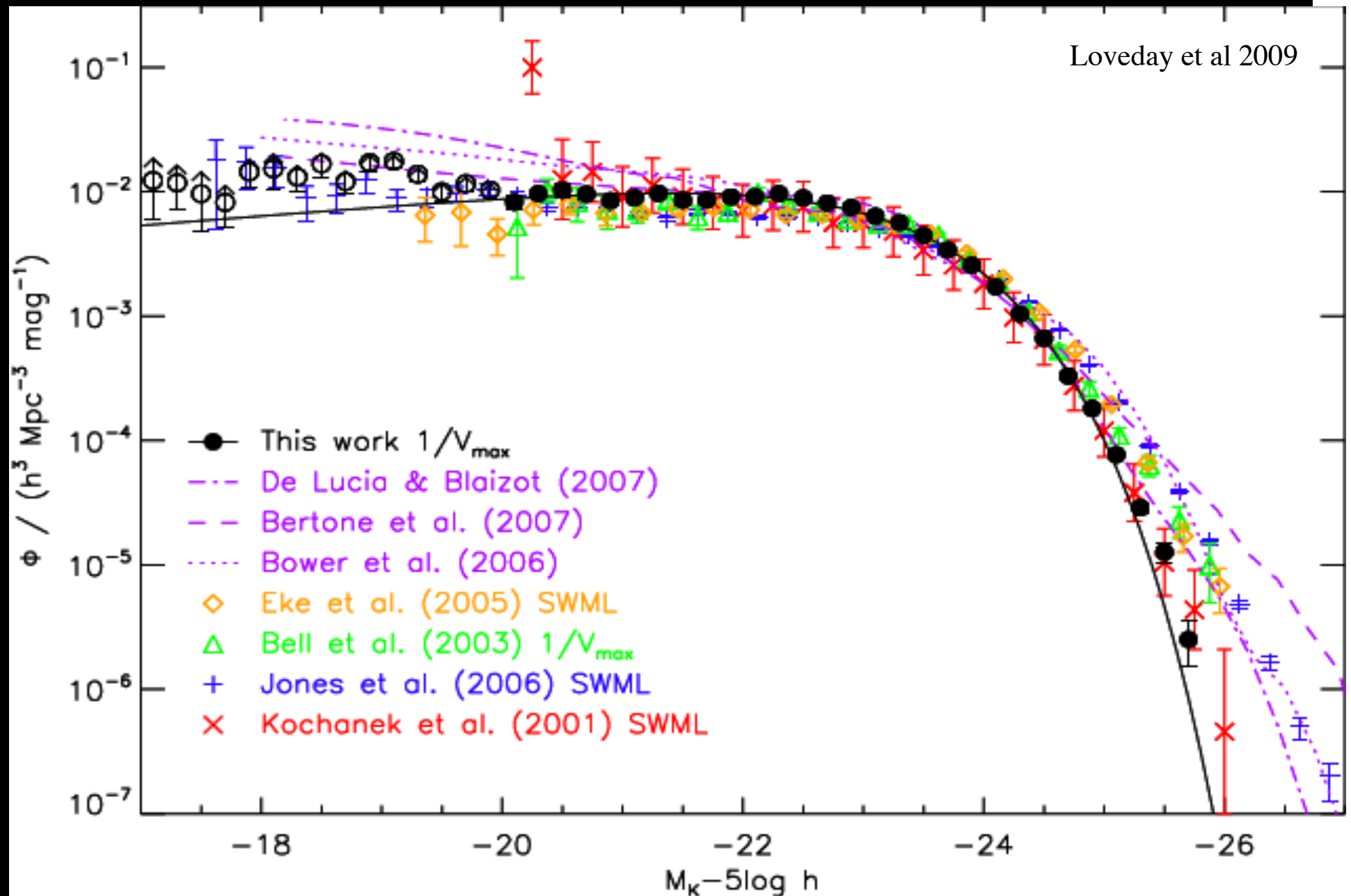




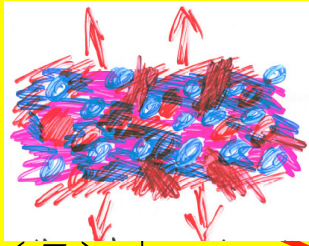
G, Kauffmann 2008

# Luminosity function of galaxies

Loveday et al 2009



# Feedback is needed



$$M_{\text{cooled-baryons}} \sim \alpha_g^{-2} \alpha^3 \left( \frac{m_p}{m_e} \right) \left( \frac{t_{\text{cool}}}{t_{\text{dyn}}} \right) T^{1+2\beta}$$

theory (CDM-motivated)

$$\alpha_g = Gm_p^2/e^2$$

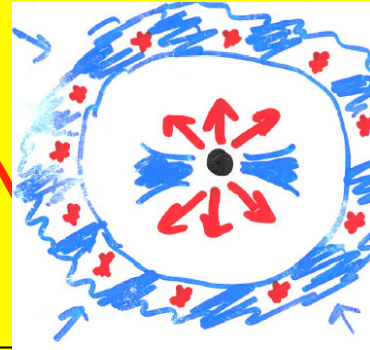
$\phi(L)$

$$L_* \sim 3 \times 10^{10} L_\odot$$

$$t_{\text{cool}} \sim \frac{nkT}{\Lambda(T)n^2}$$

$$t_{\text{dyn}} \sim \frac{1}{\sqrt{Gm_p n}}$$

observations



Galaxy luminosity/mass

SN

AGN

Memories of the epoch of the first galaxies  
in the luminosity function of dwarfs...

# FEEDBACK IS ESSENTIAL

Reionization

Supernovae

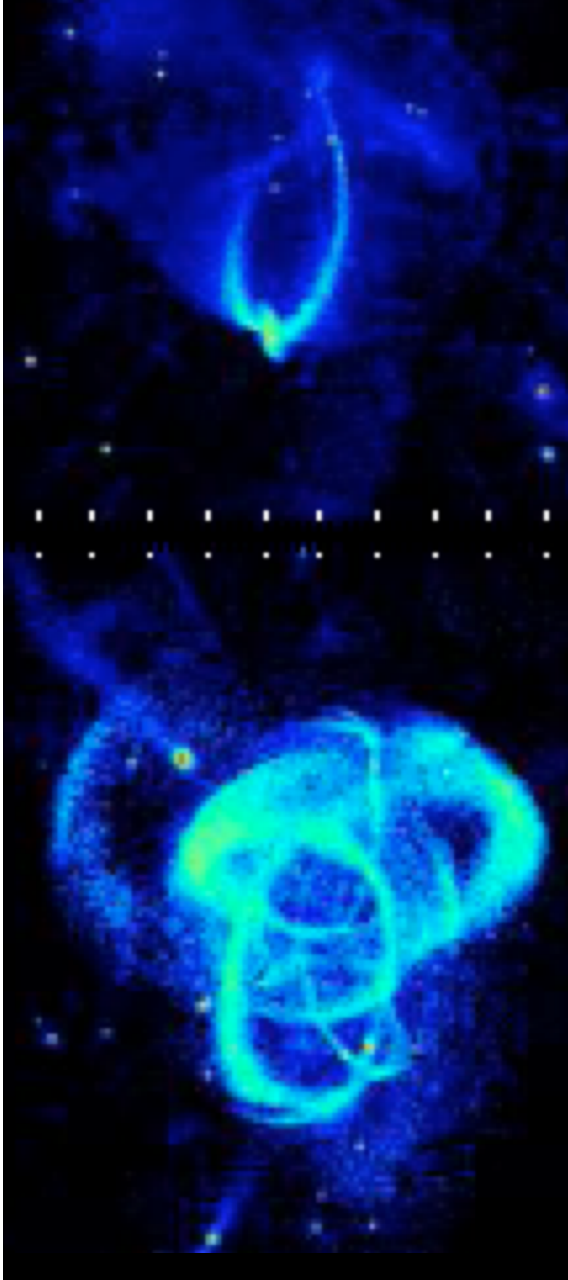
Tidal stripping

Active galactic nuclei



# FEEDBACK BY TIDAL DISRUPTION

Cooper et al 2010



Martinez-Delgado et al 2008



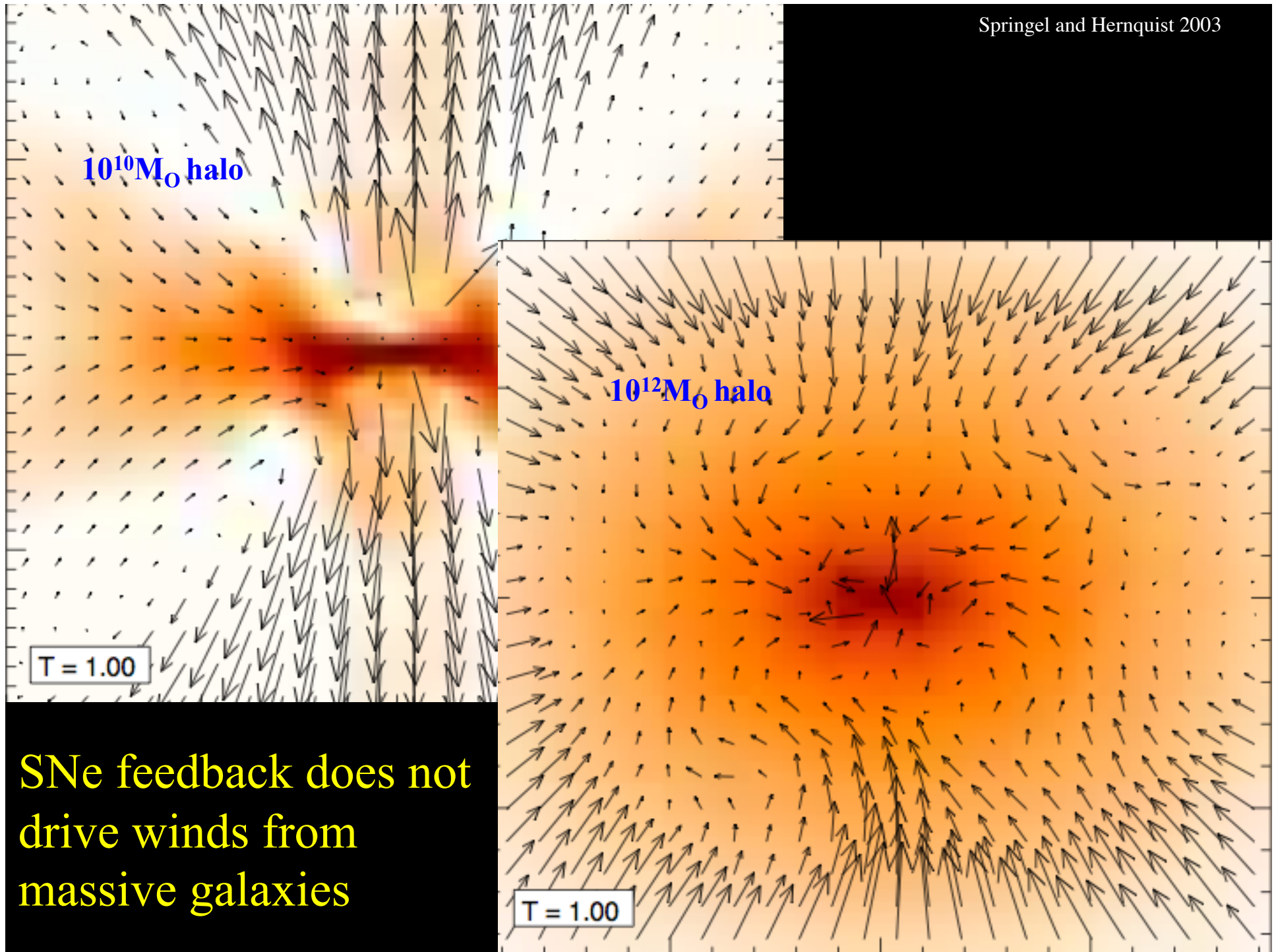
$10^{10}M_{\odot}$  halo

$10^{12}M_{\odot}$  halo

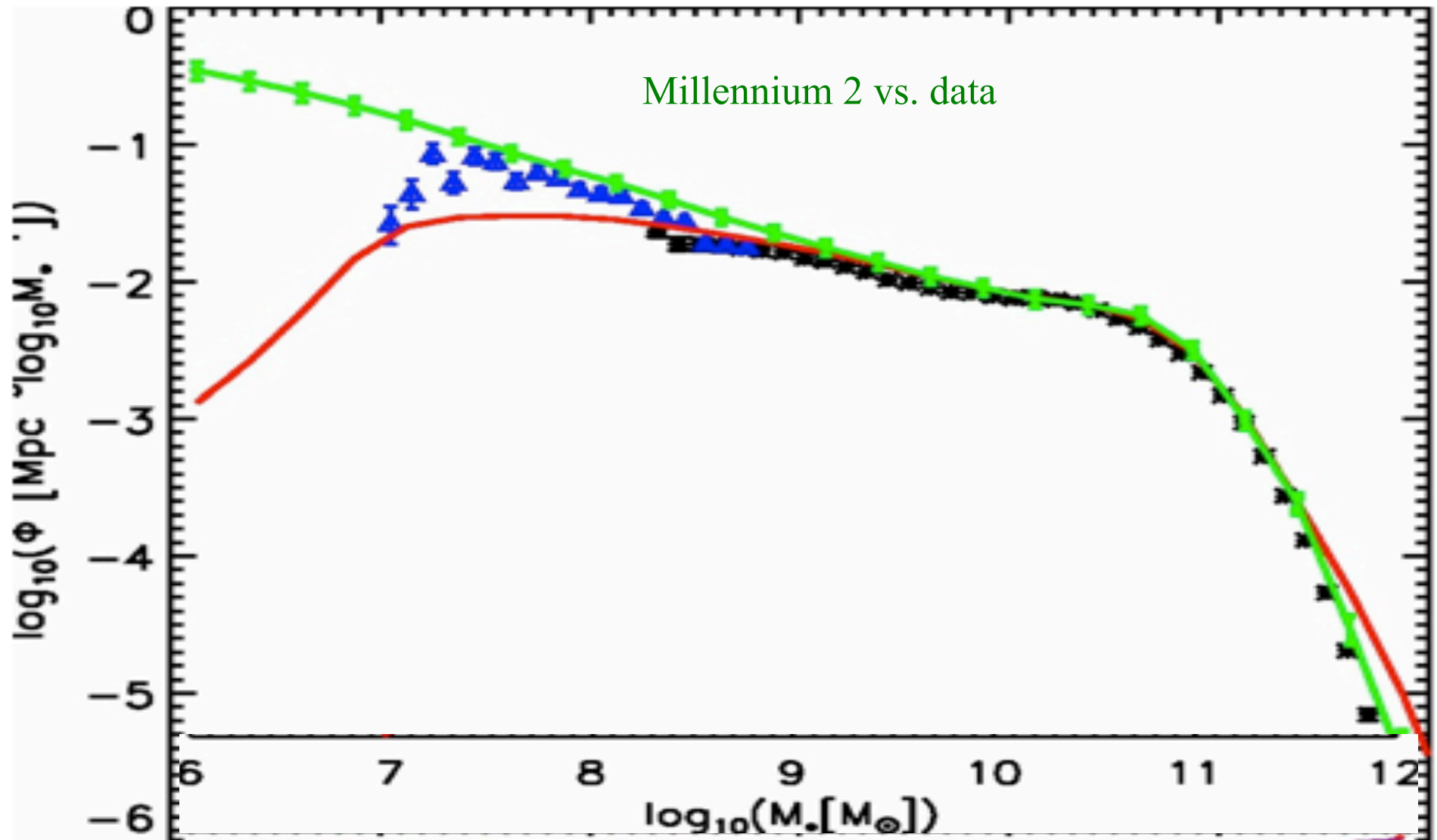
T = 1.00

T = 1.00

SNe feedback does not  
drive winds from  
massive galaxies



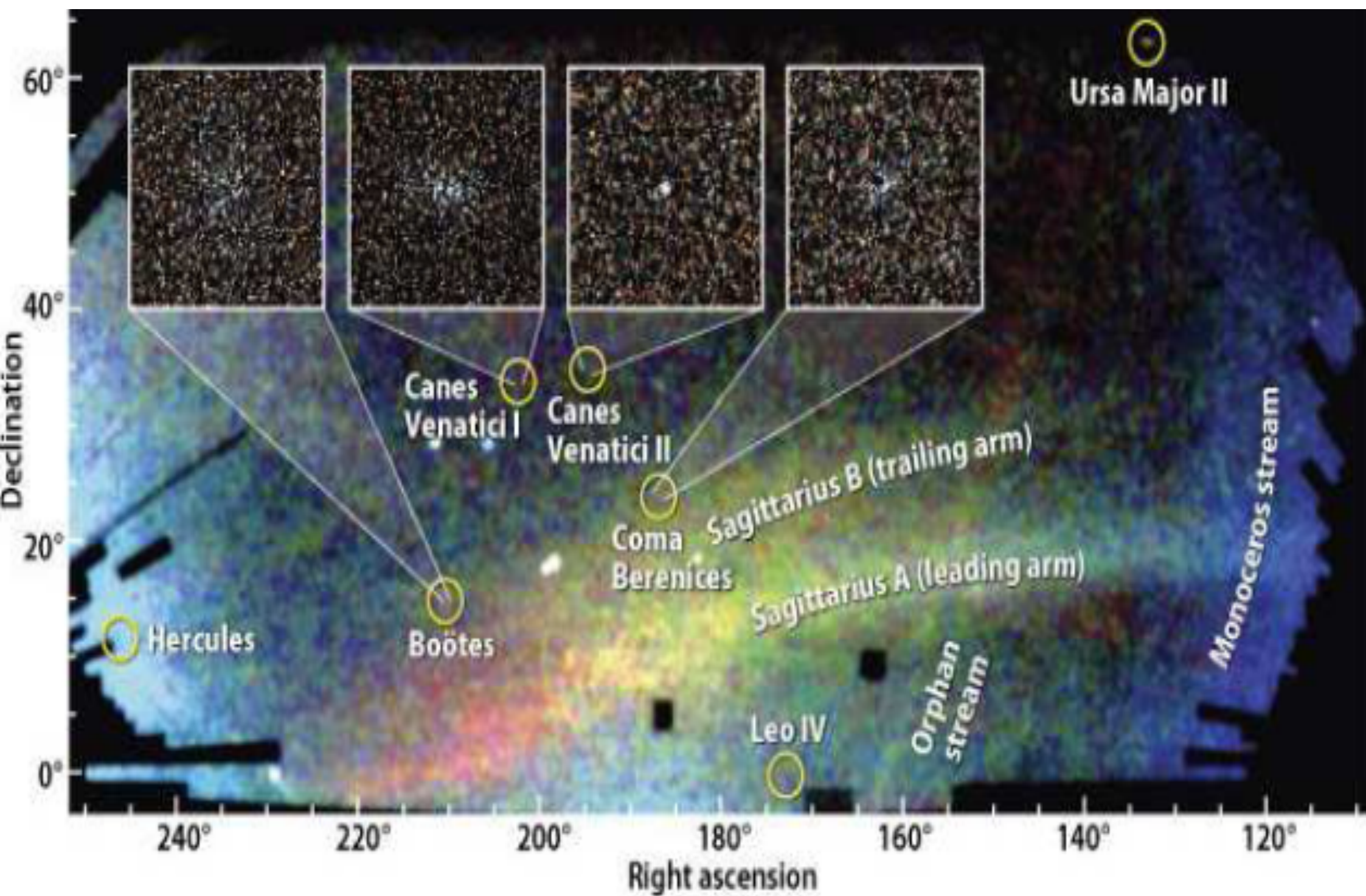
# Semi-analytical models or hydro simulations



Guo et al 2010

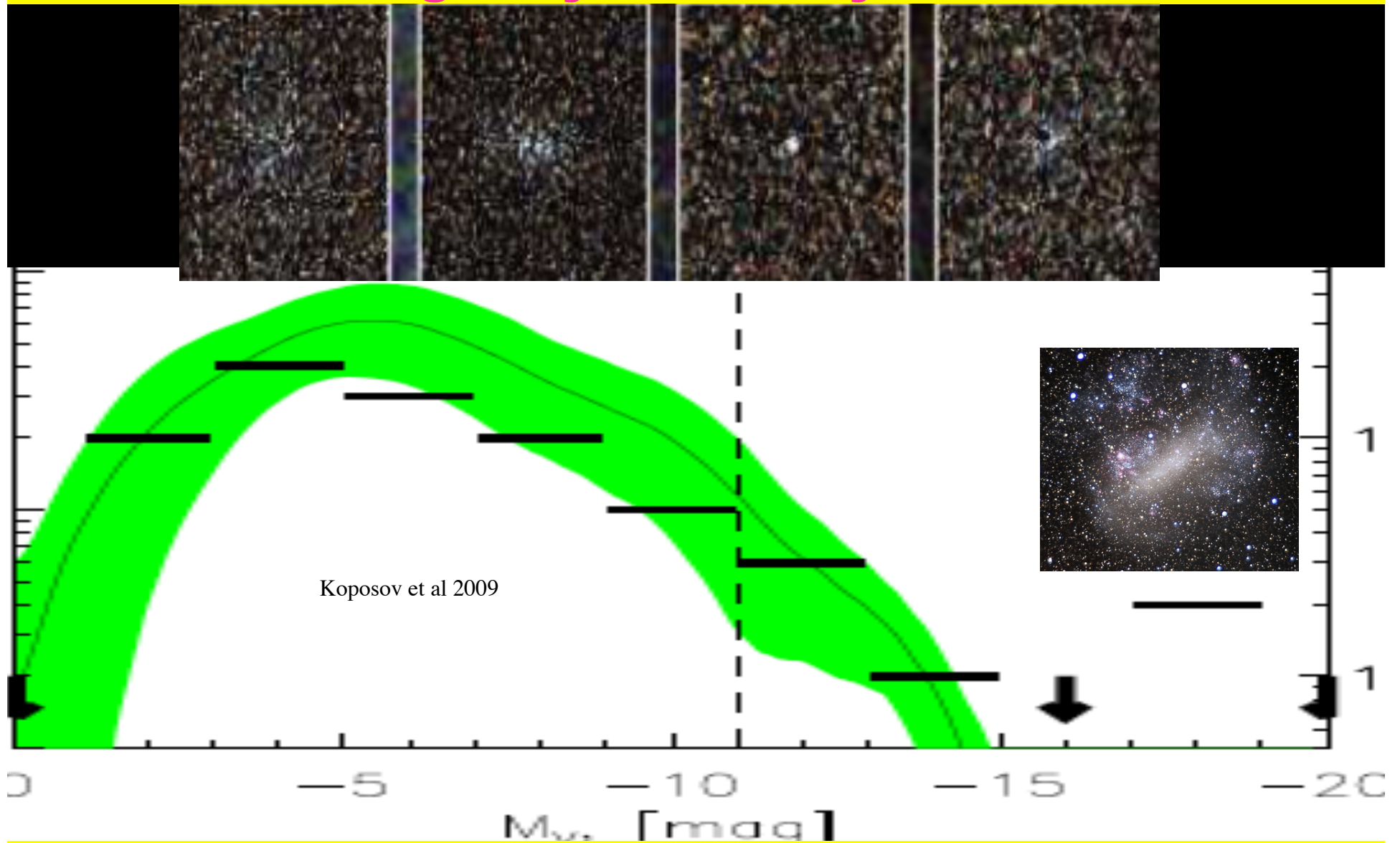
Galaxy luminosity function



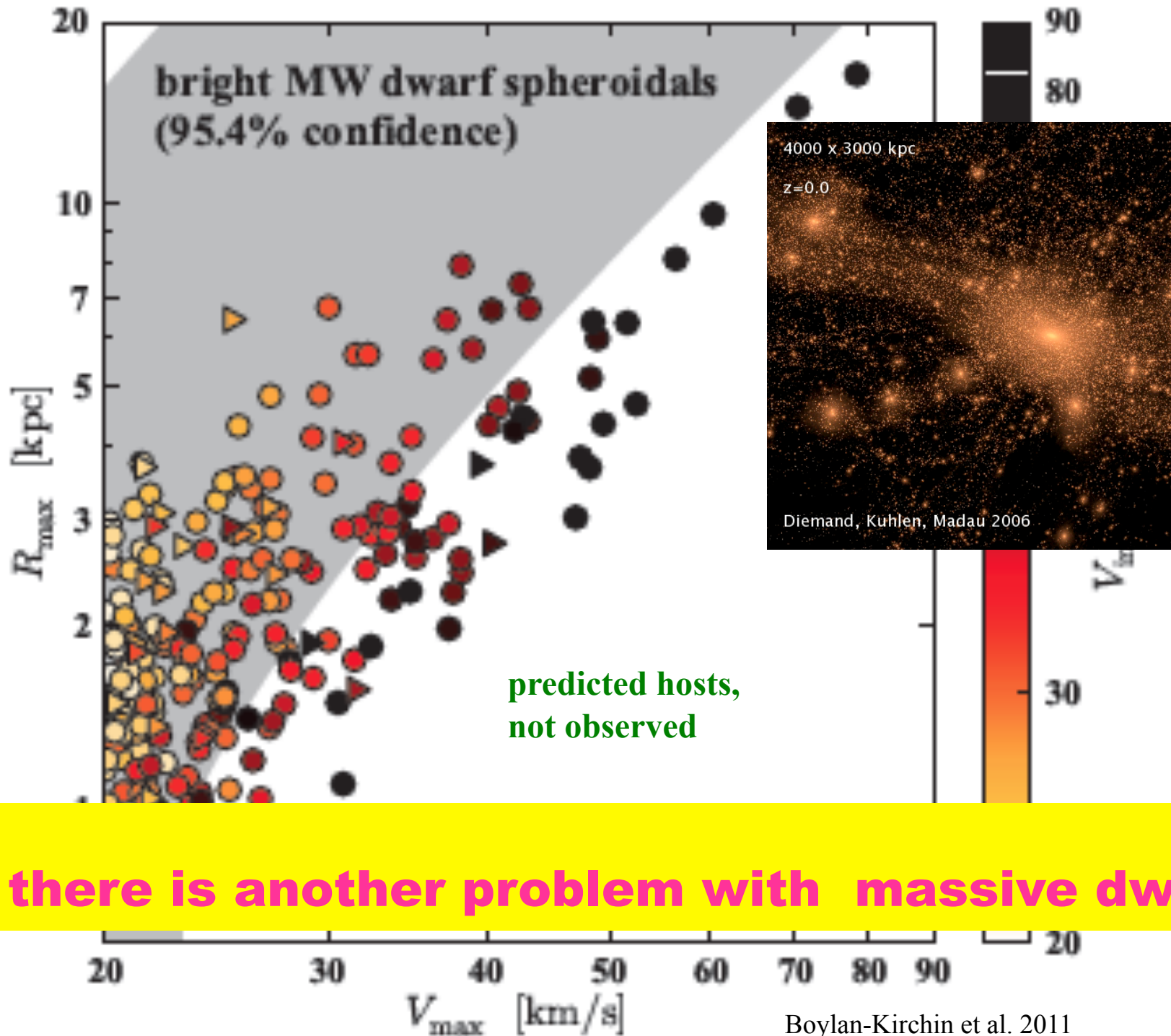




# the galaxy luminosity function

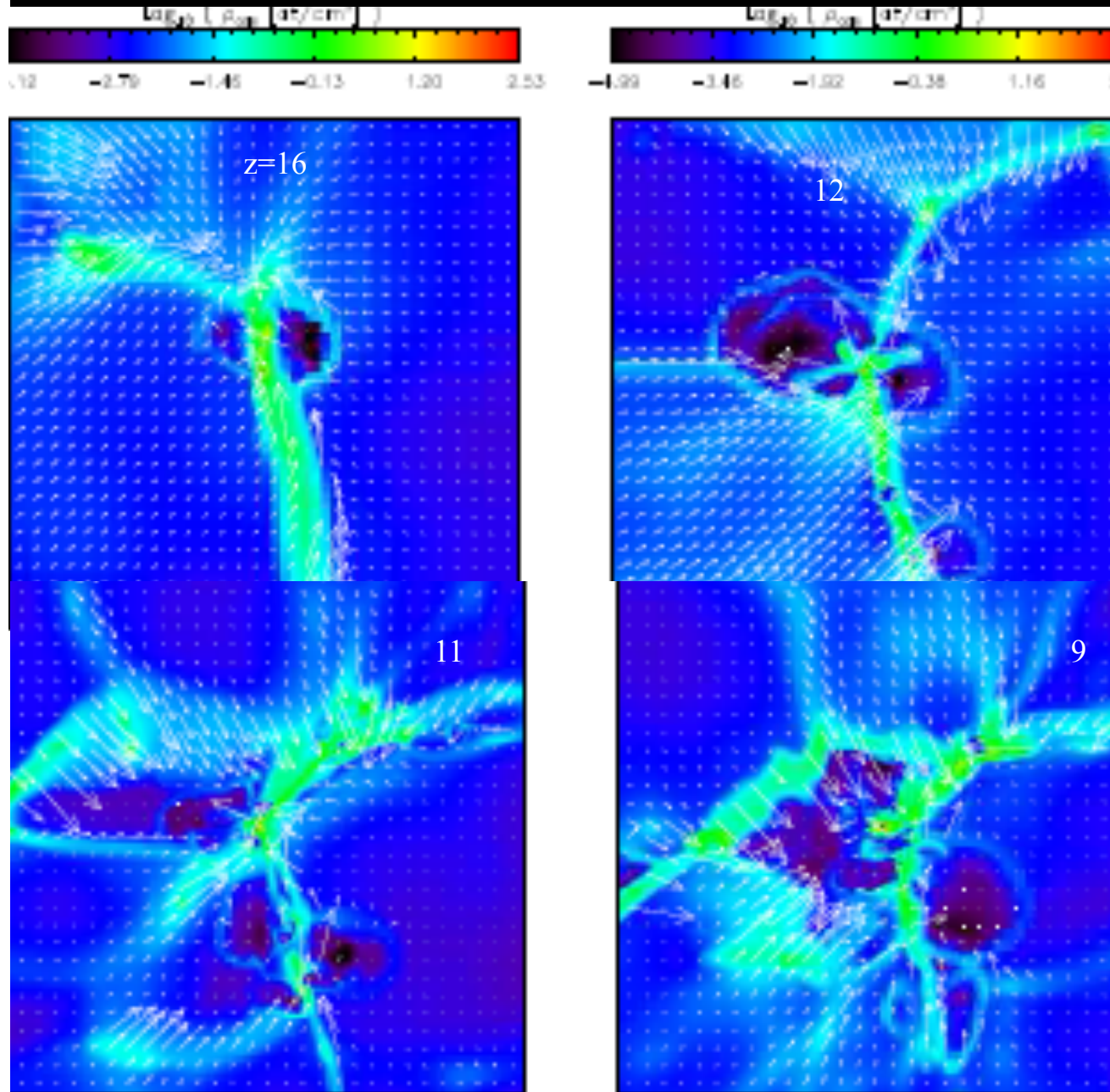


there is a problem with massive dwarfs

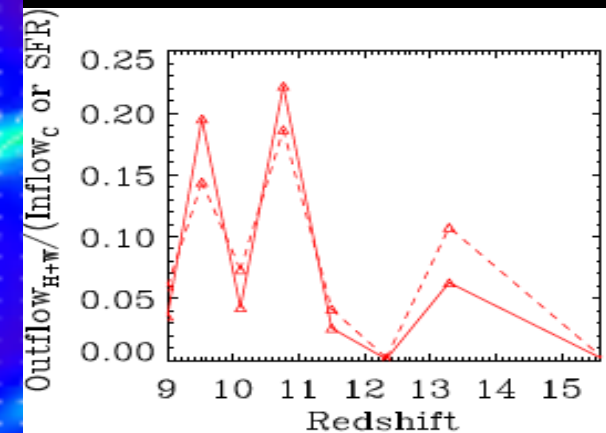


there is another problem with massive dwarfs

# Semi-analytical models or hydro simulations



SNe do not eject enough baryons even from dwarfs

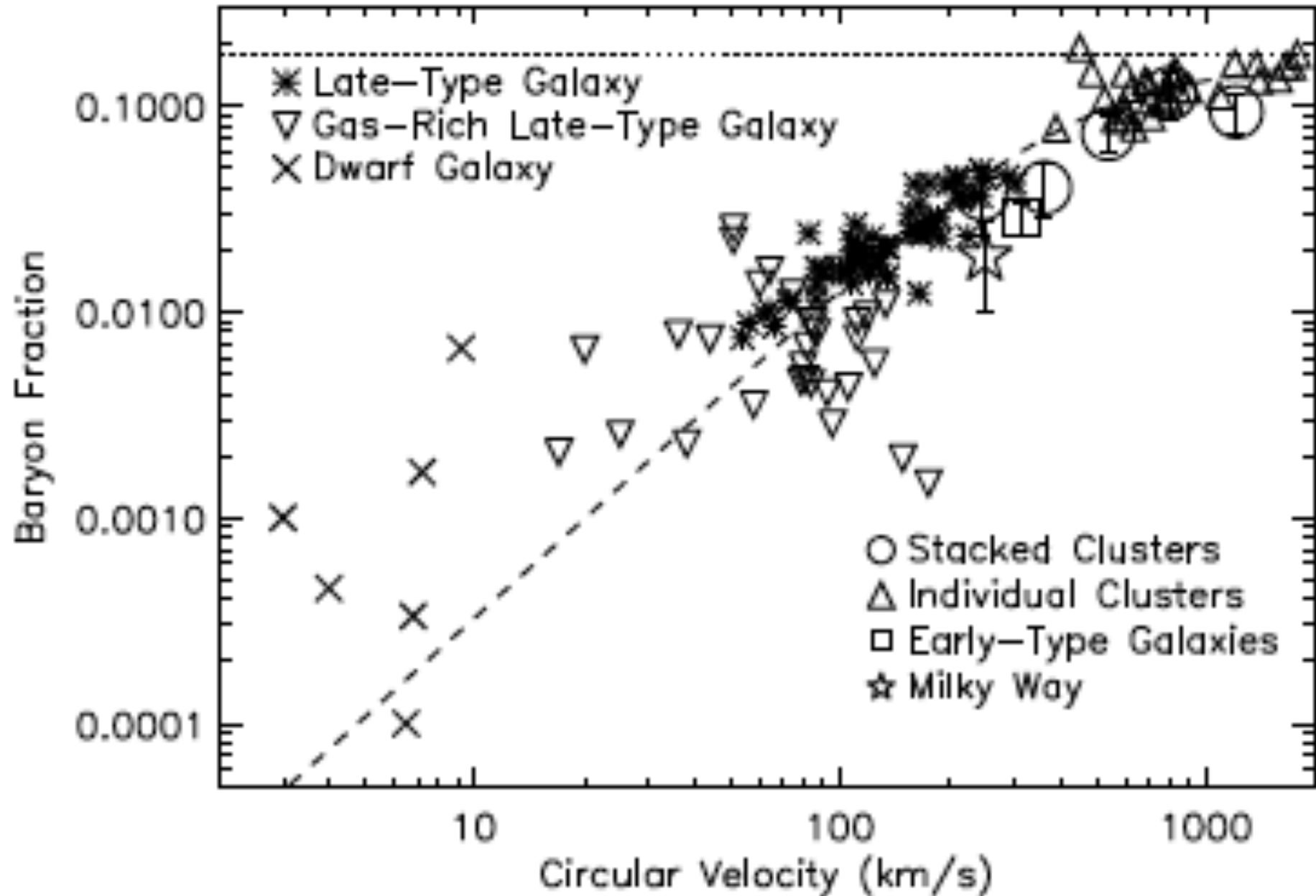


Powell et al 2011  
Fujita et al 2004



# BARYON FRACTION

Dai et al 2010



**Disk galaxies**

# feedback by massive stars

Cloud disruption locally controlled by  
OB stars: SFE= 2%

Cloud formation globally controlled by  
supernova-driven turbulence: SFE= 2%

motivated by gravitational instability of cold disks

$$\text{SFR} = \text{SFE} \cdot (\text{GAS DENSITY}) / t_{\text{dyn}}$$

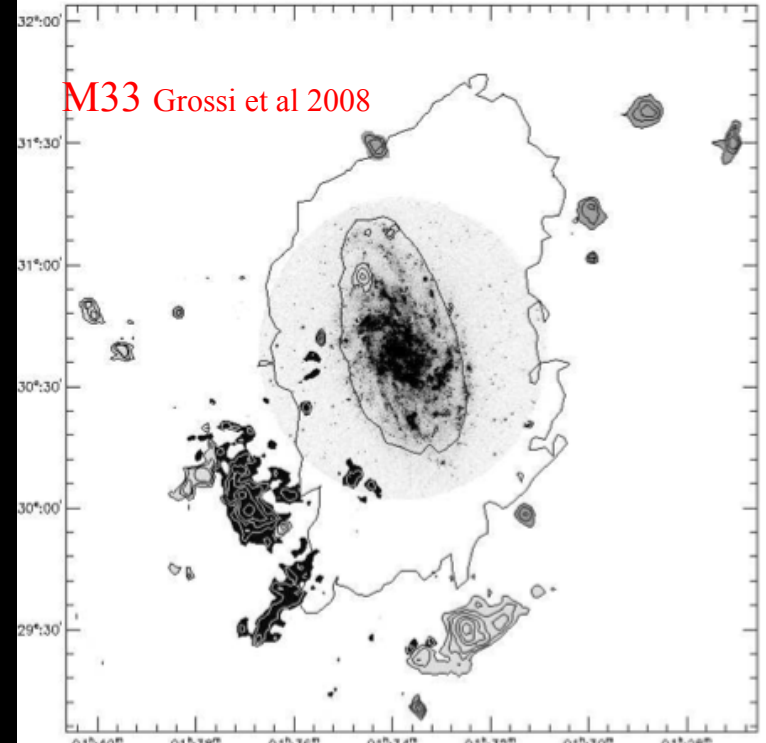
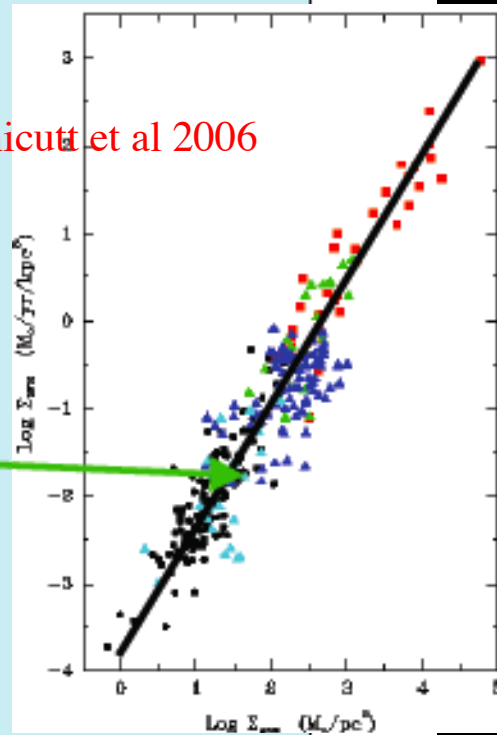
$$\text{SFE} = \frac{\sigma_{\text{gas}} v_{\text{cool}} m_{*,\text{SN}}}{E_{\text{SN}}} \approx 0.02$$



# A GLOBAL STAR FORMATION LAW



Kennicutt et al 2006

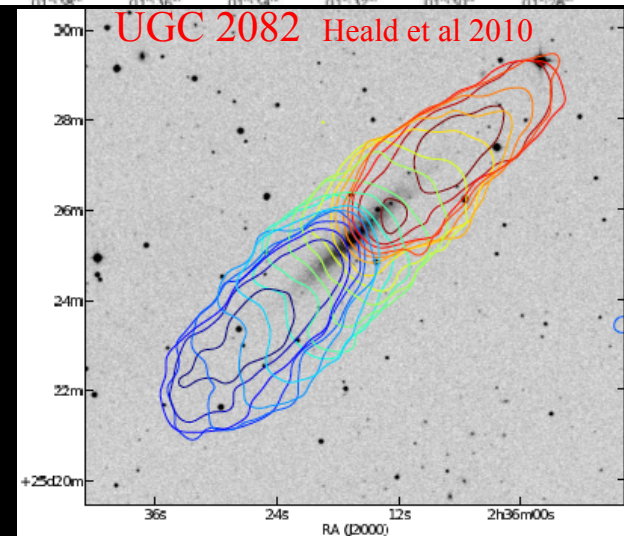


M33 Grossi et al 2008

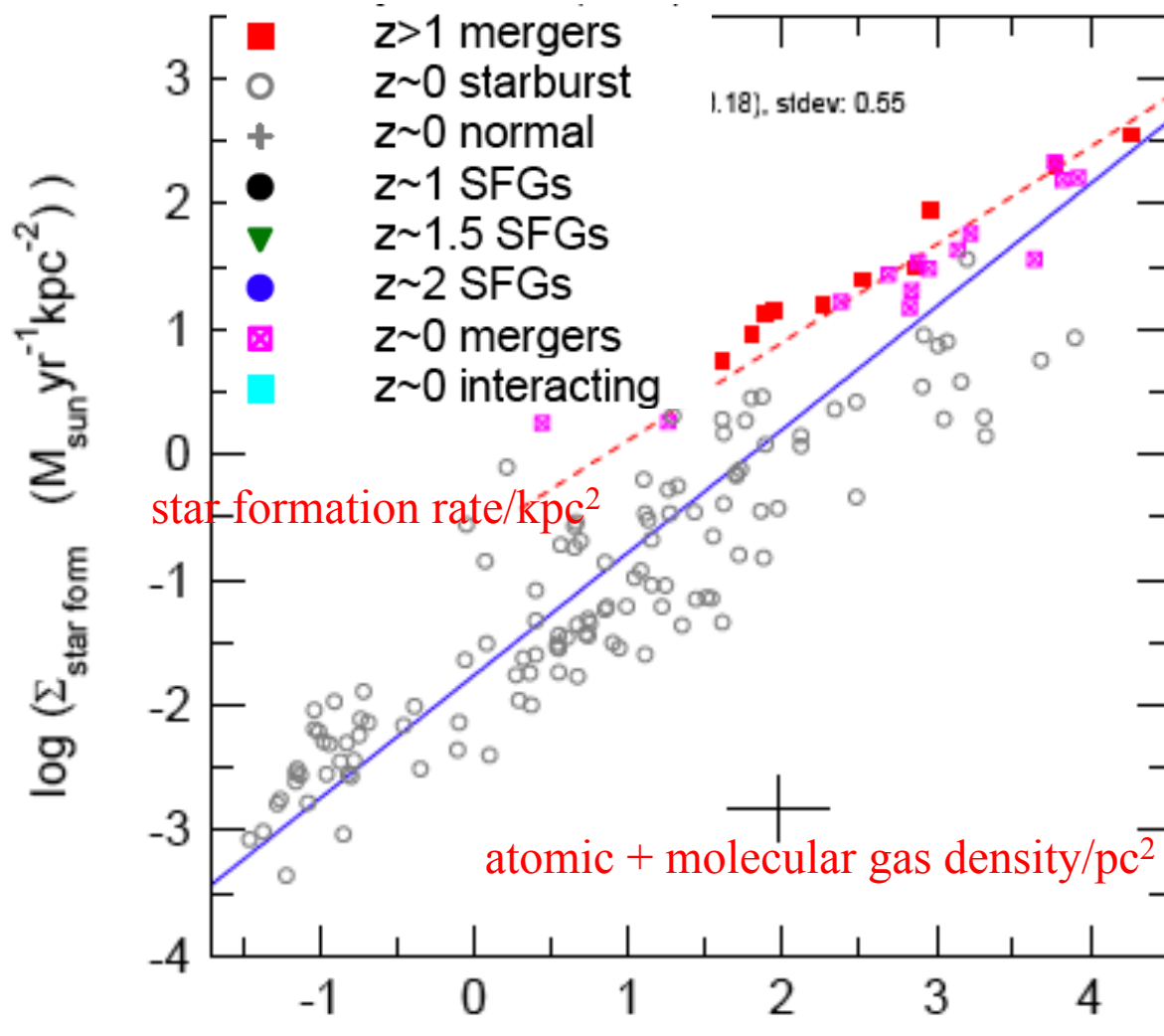
$$\text{SFR} = 0.02 (\text{GAS SURFACE DENSITY}) / t_{\text{dyn}}$$

NGC 6946 Boomsma et al 2008

low efficiency due to SN feedback  
+ cold gas accretion/global disk instability



UGC 2082 Heald et al 2010



Star Formation efficiency  $(M_{\text{sun}} \text{ kpc}^{-2} \text{ yr}^{-1})$   
 = SFR / GAS MASS x ROTATION TIME  
 = 2.5%

# Spheroidal galaxies

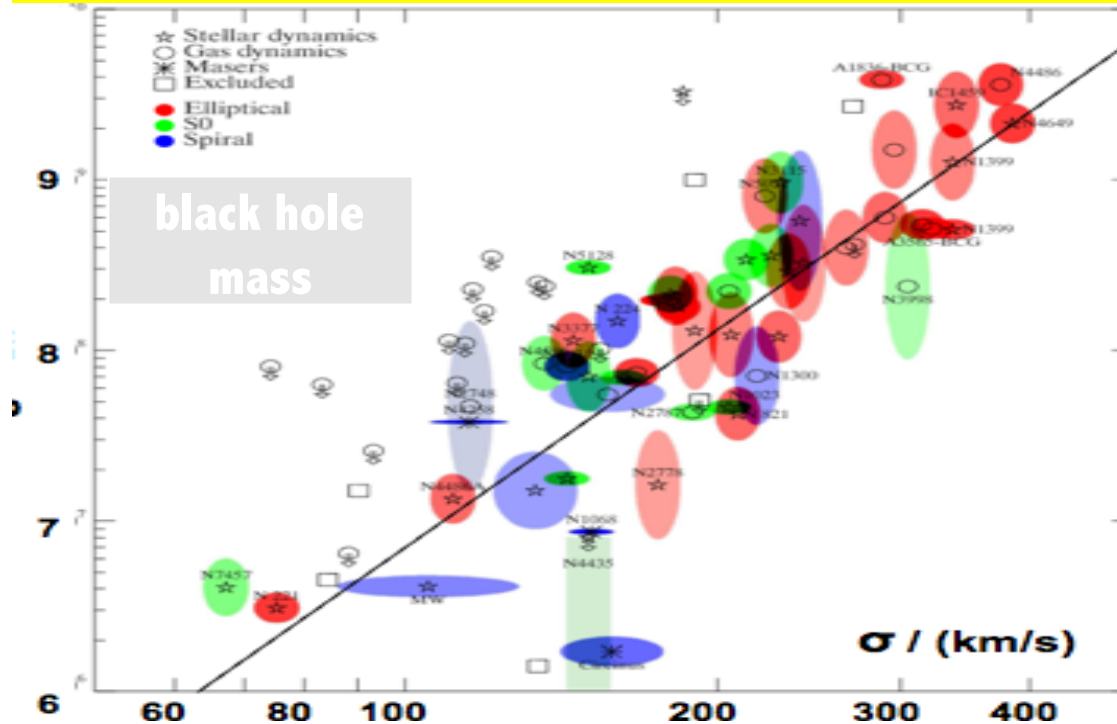
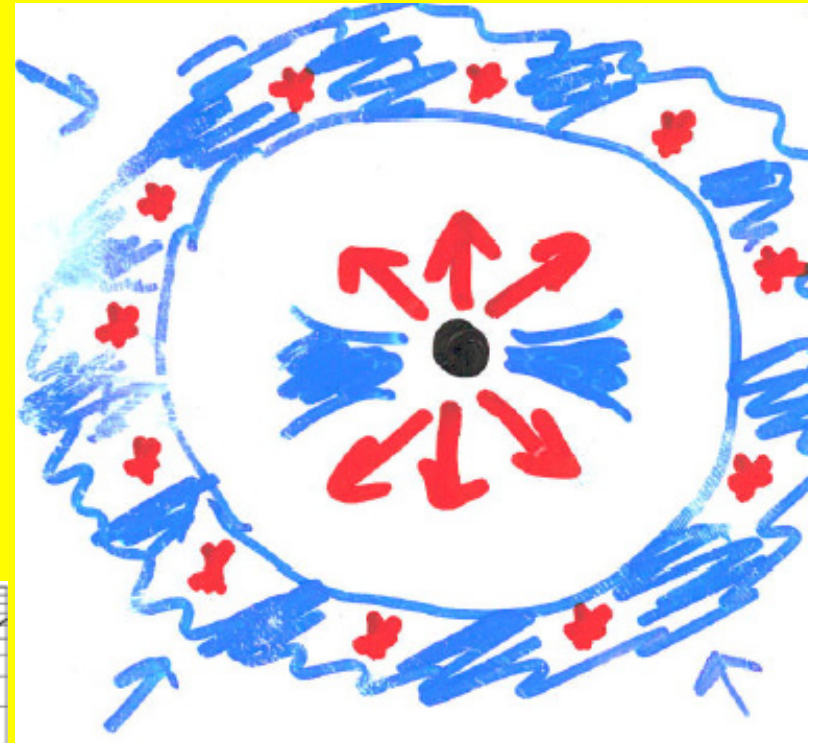


# Feedback by massive black holes

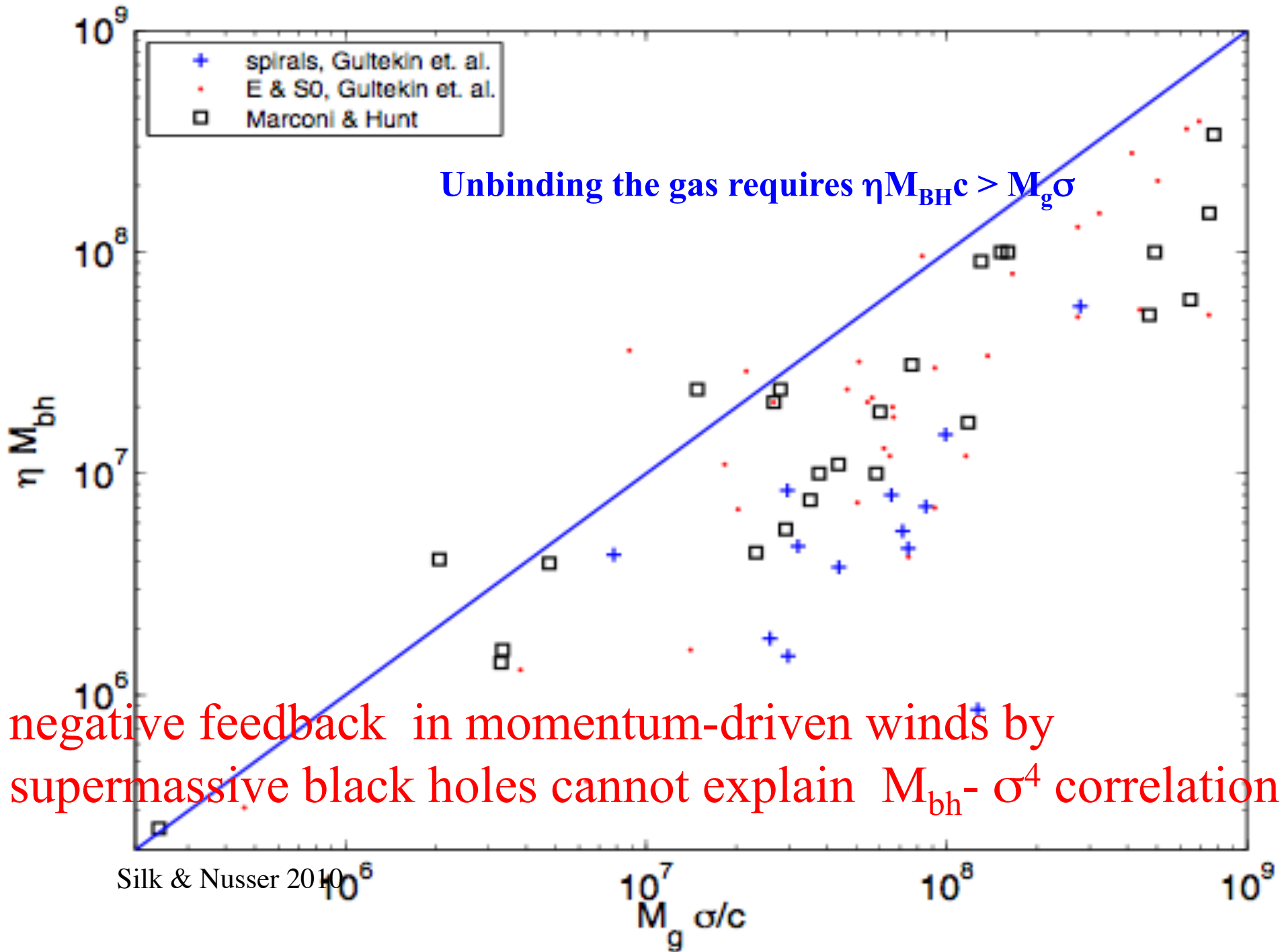
$$L_{\text{Edd}}/c = GMM_{\text{gas}}/r^2$$

$$M_{\bullet} = 3 \times 10^9 M_{\text{sun}} \left( \frac{\sigma}{300 \frac{\text{km}}{\text{s}}} \right)^4$$

Blowout occurs/star formation terminates  
when SMBH- $\sigma$  relation saturates



$$L_{\text{Edd}} = 4\pi cGM_{\text{BH}}m_p/\sigma_T$$



1) Porosity is a killer for SNe

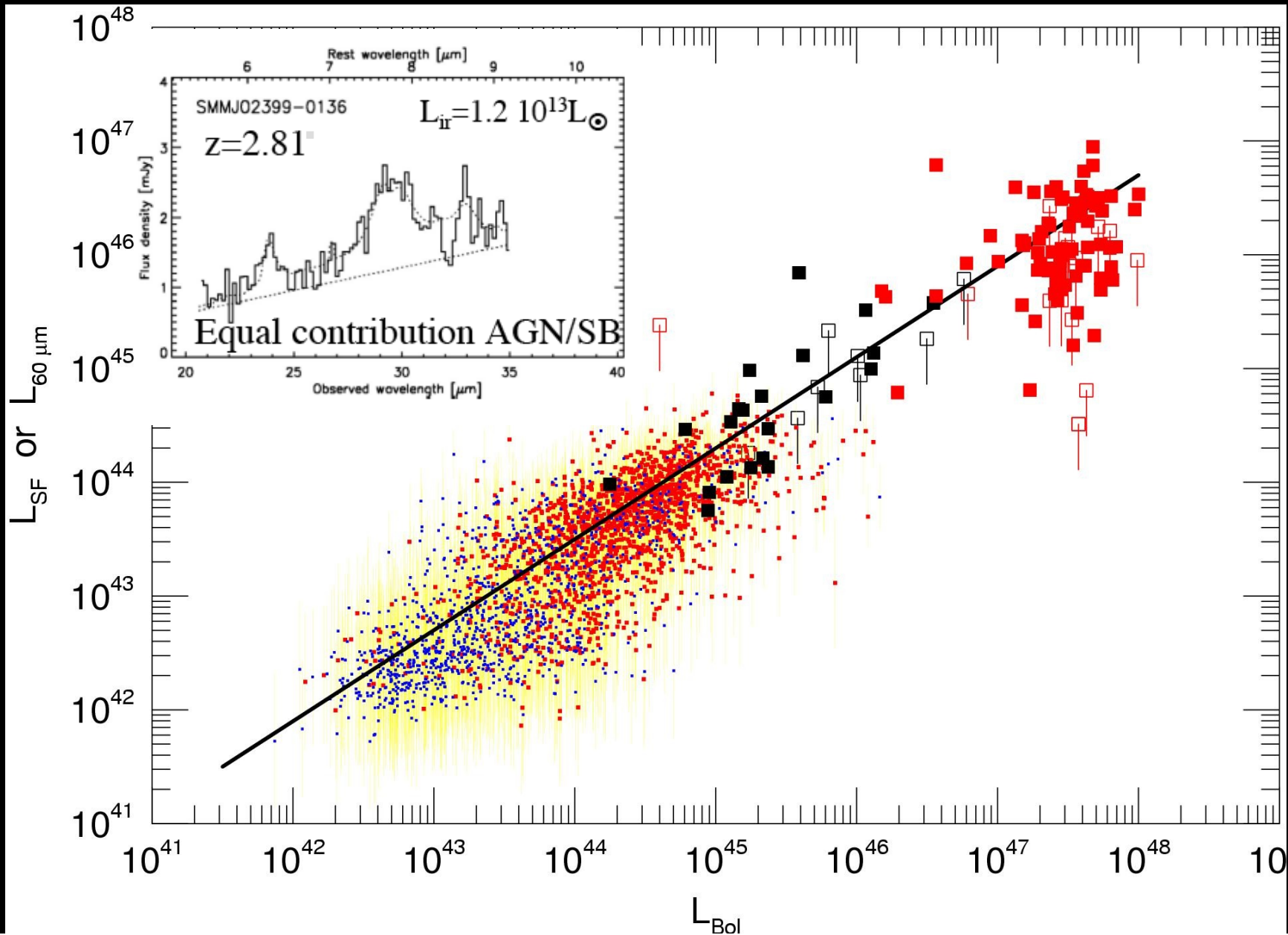
2) Its not AGN, momentum deficit

3) maybe its both! AGN

+ triggering of star formation



# connection between AGN and starbursts



# star formation rate is boosted by AGN

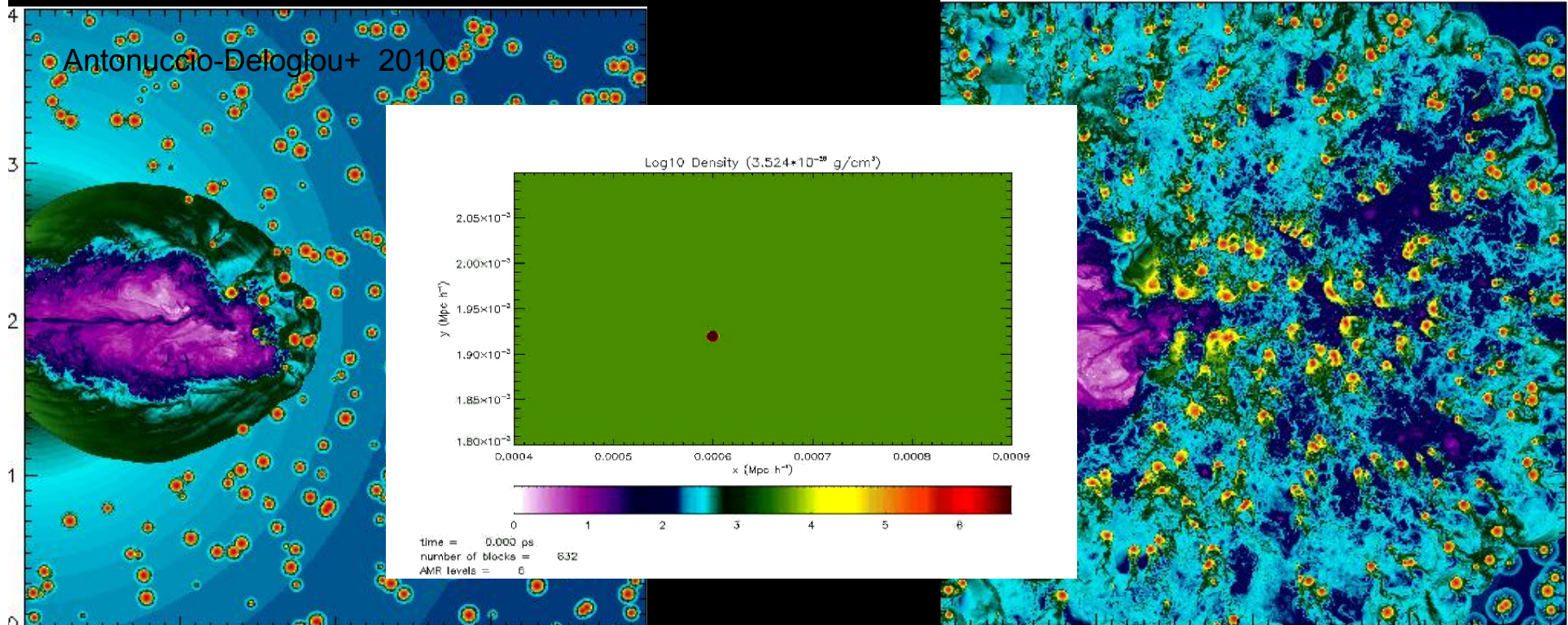
If AGN-driven outflows trigger star formation,

JS + C. Norman 2008

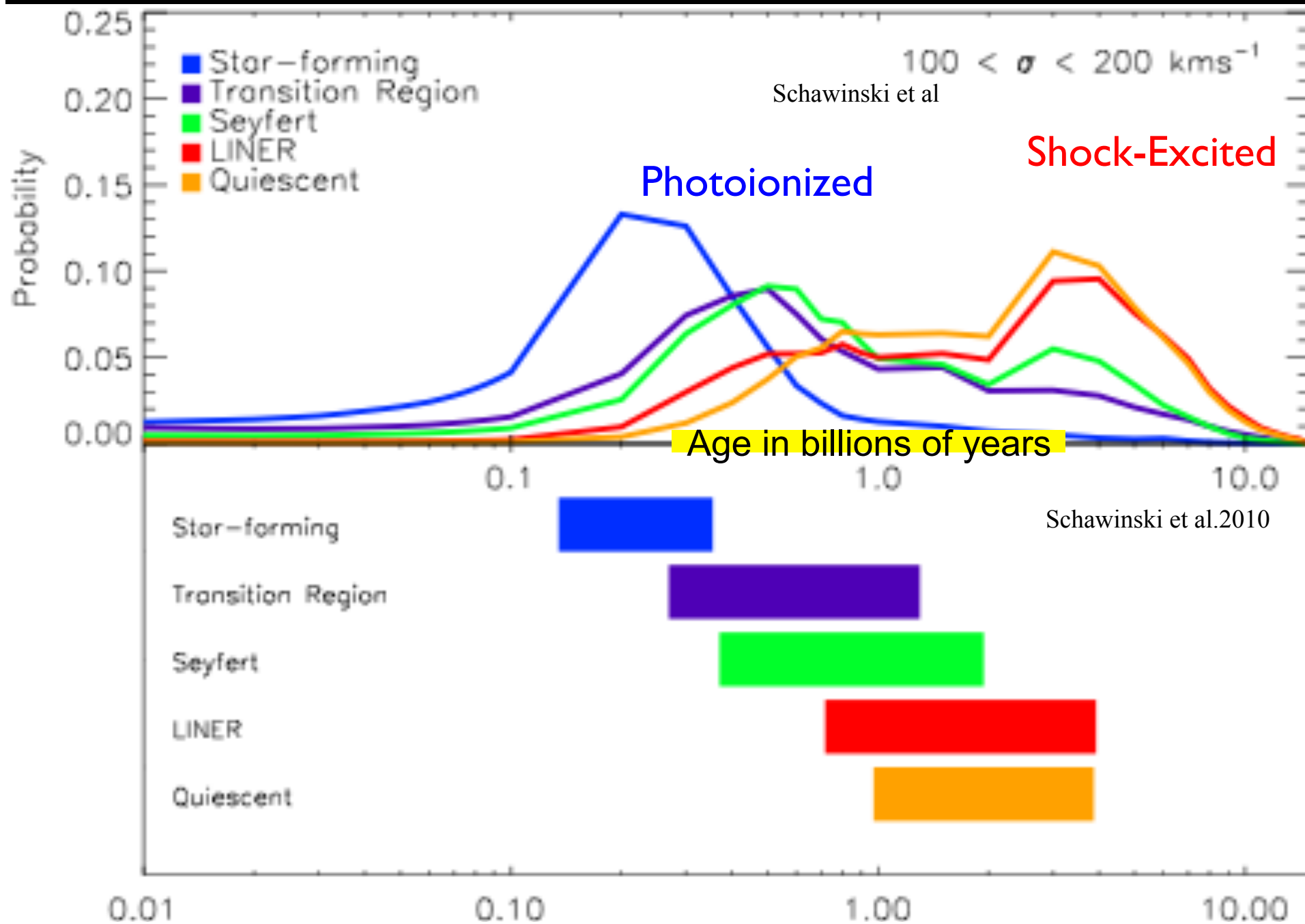
**star formation rate boost factor  $\sim v_{\text{cocoon}}/\sigma \sim 10-100$   
+ outflow momentum amplified by supernovae**

$$(p_{\text{AGN}}/p_g)^{1/2} \approx v_{\text{jet}}/\sigma$$

$$\dot{M}_* = (\epsilon_{\text{SN}}/\sigma) M_g (G p_g)^{1/2}$$



# AGN are observed to quench star formation....





# AGN jet-induced backflow feeds the SMBH

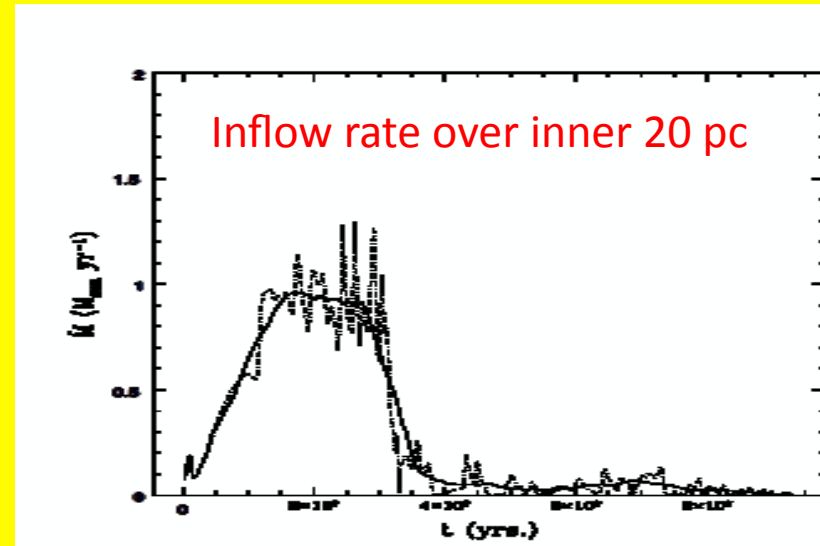
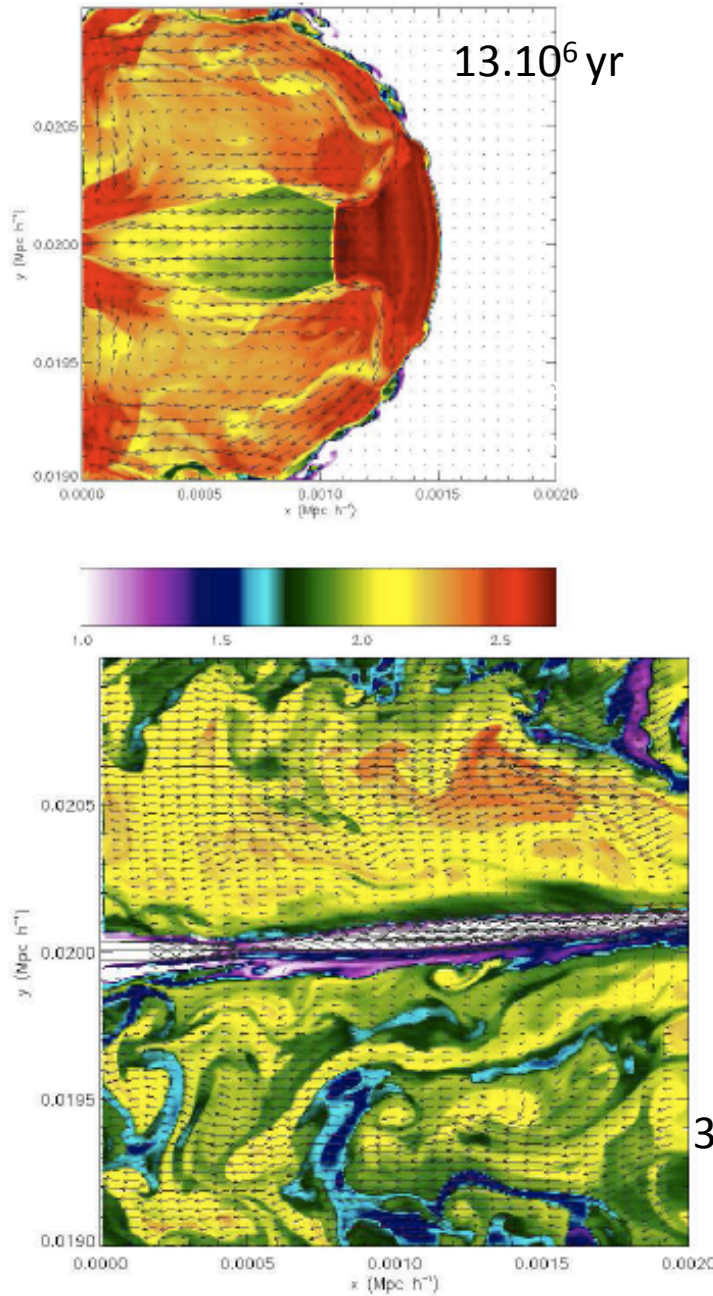
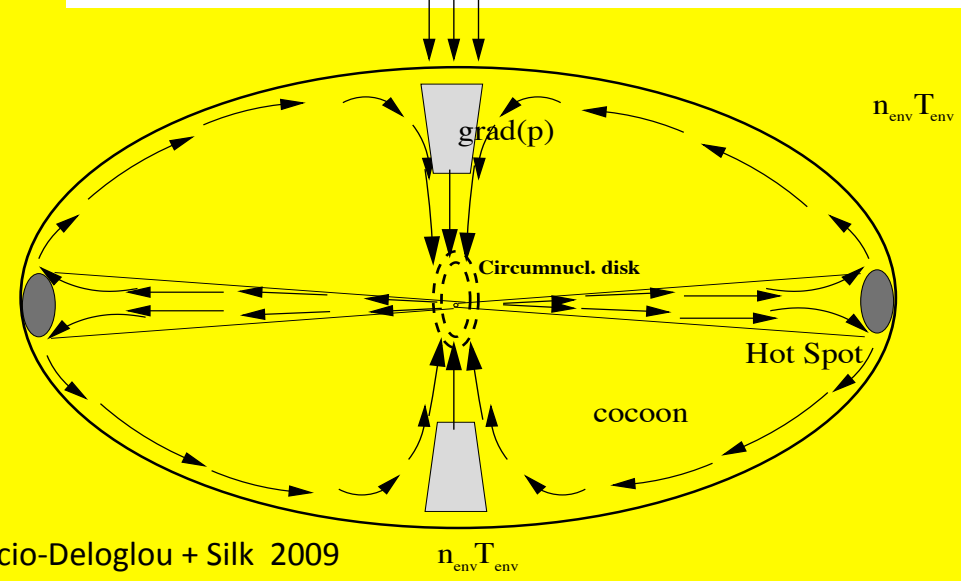


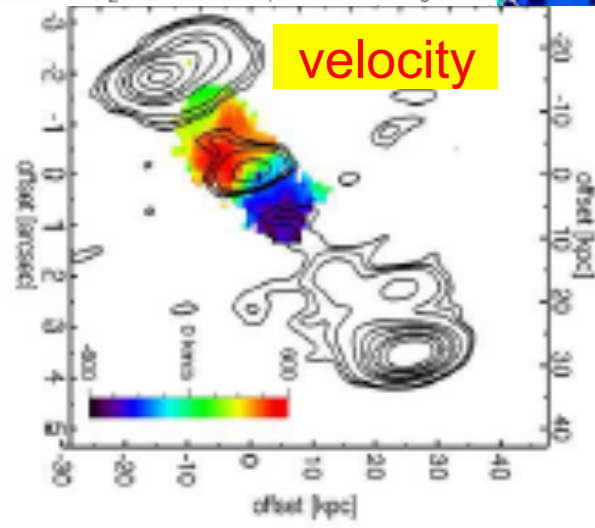
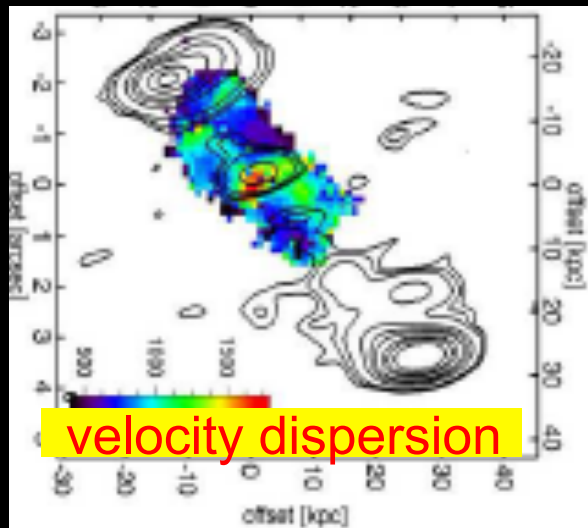
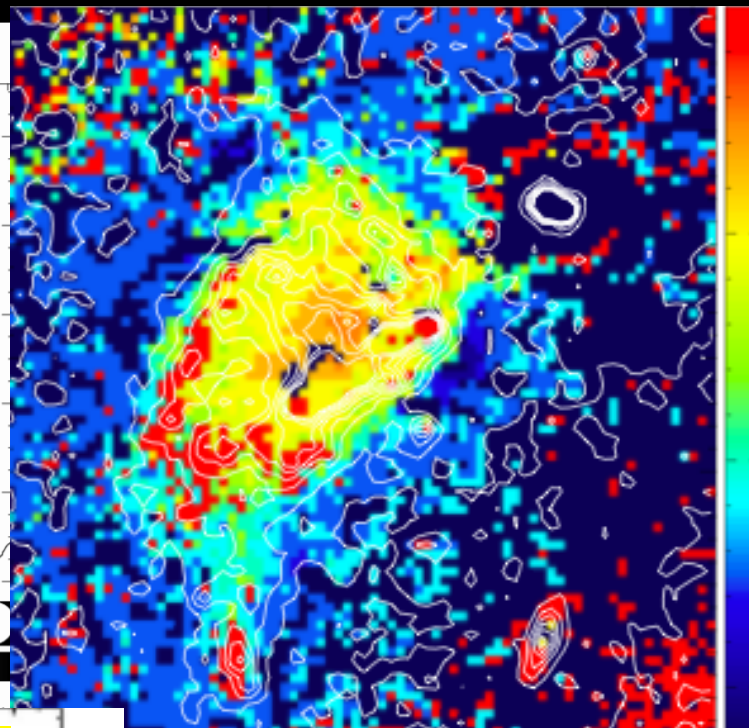
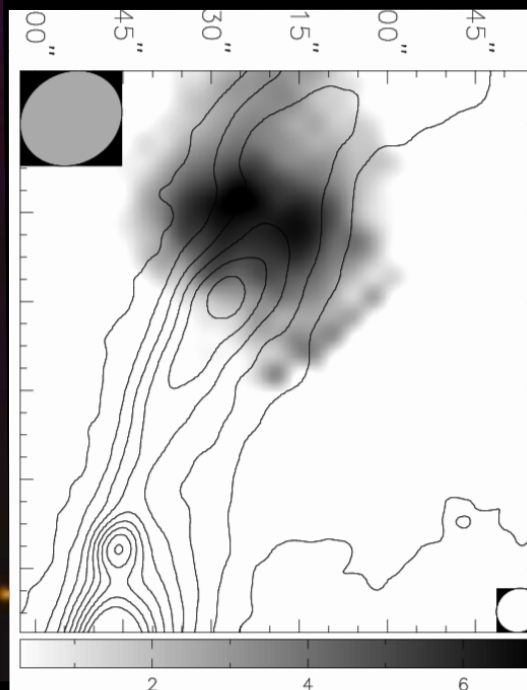
Figure 7. Mass flow in the circumnuclear region for run *sim500a*. We show the averaged flux (continuous line) and the instantaneous flux (dashed line) used by the intermittent behaviour of the flux inside the cocoon, during the evolved phase of the flow.



Antonuccio-Deloglou + Silk 2009

# TRIGGERING IS OBSERVED Minkowski's Object

Croft et al. 2006

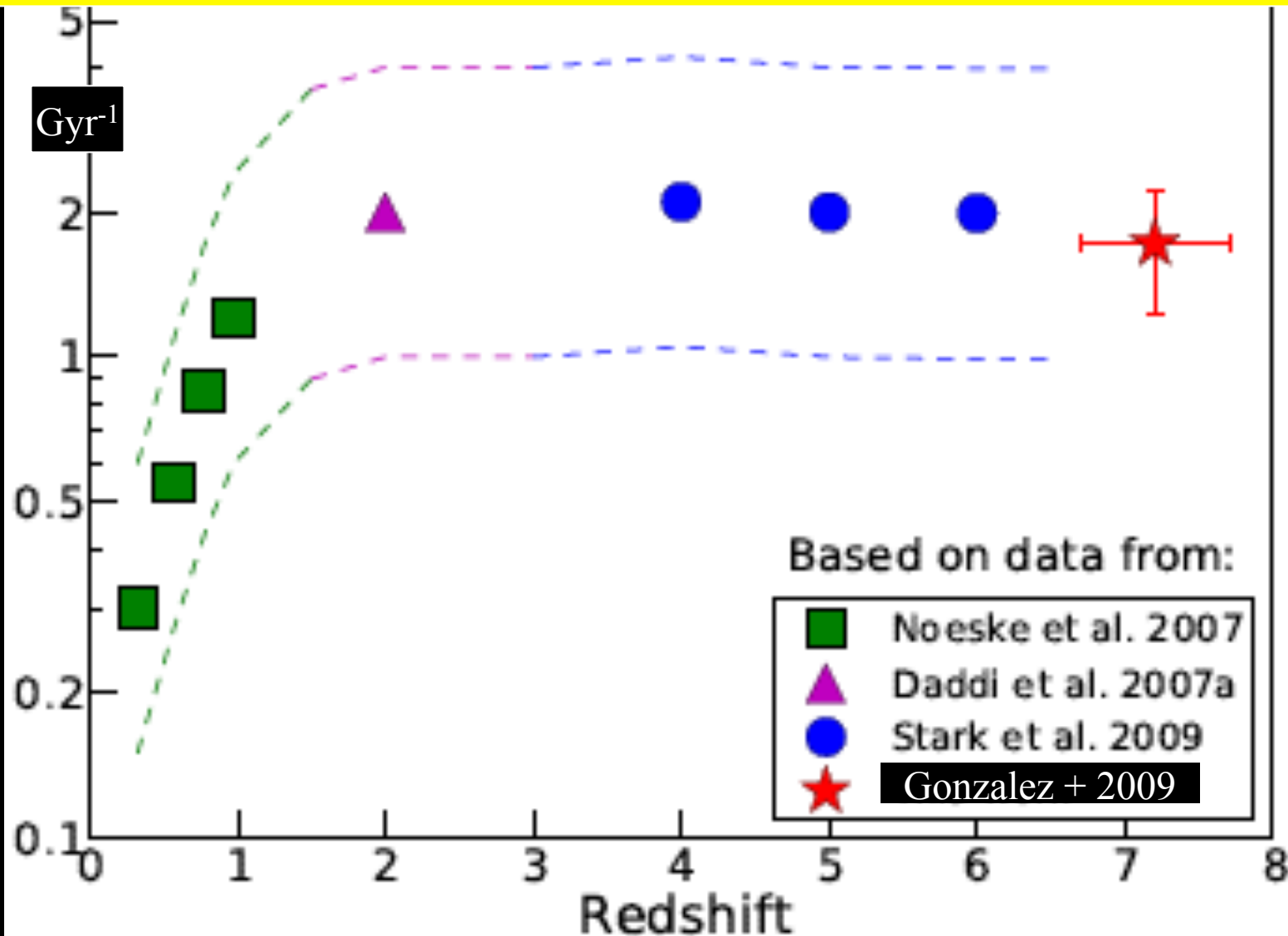


## A ULIRG

Nesvadba 2009

# PERHAPS WE NEED TRIGGERING AT HI z

specific star formation rate = SFR/stellar mass

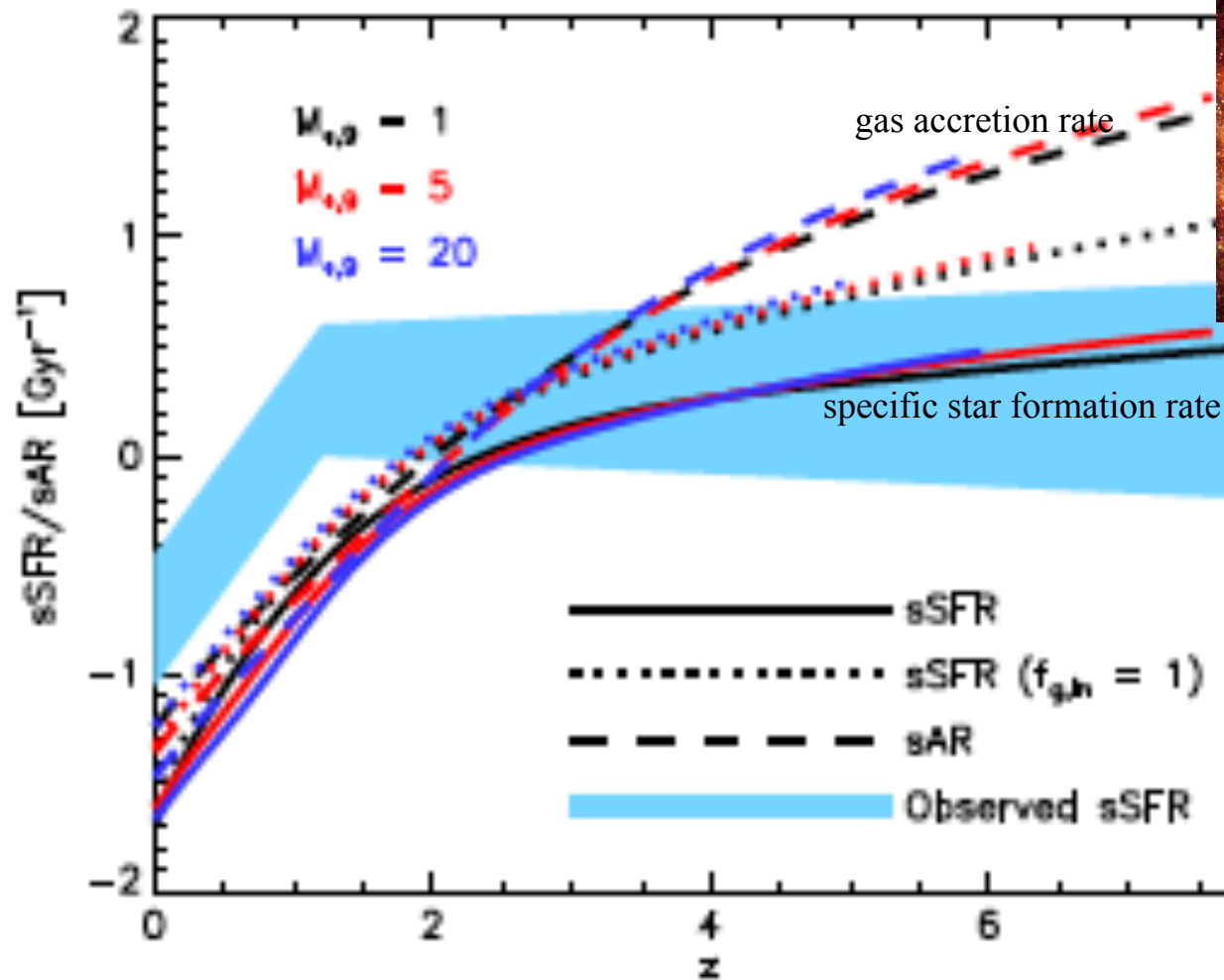
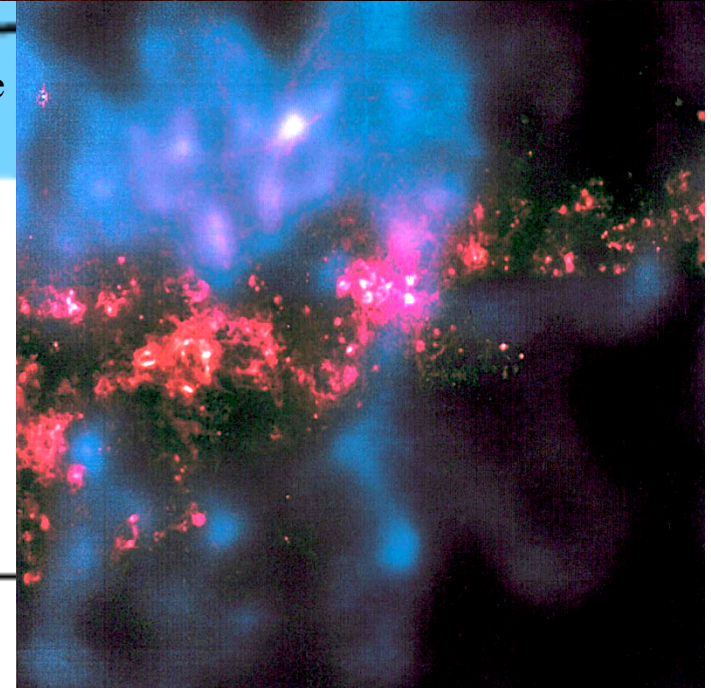




# Star formation quenching via $H_2$ and $Z(t)$

No ejection of baryons (& fails at low  $z$ )

Krumholz and Dekel 2011





star formation, gas  
accretion and gas ejection

two modes of star formation

A: without active galactic nuclei (SMBH)

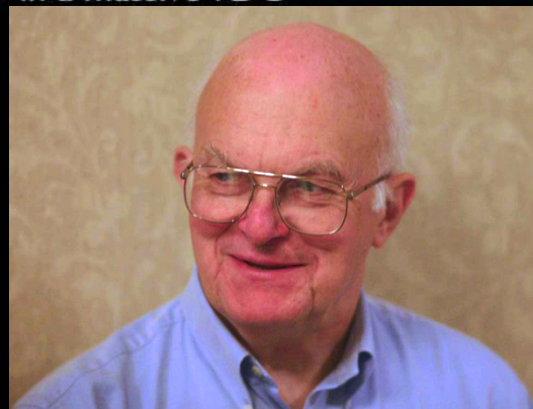
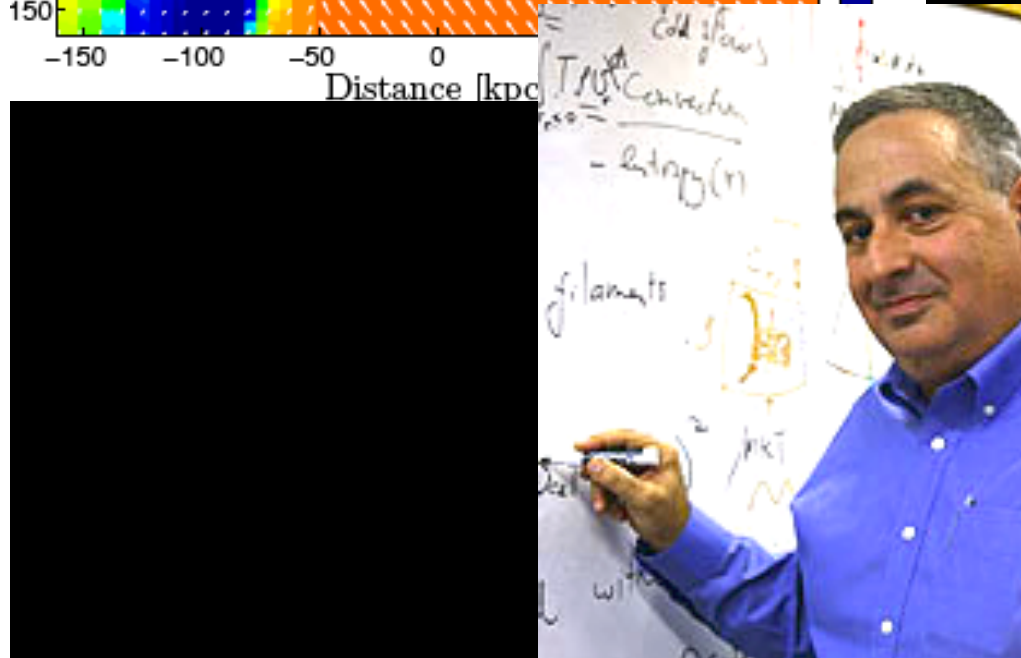
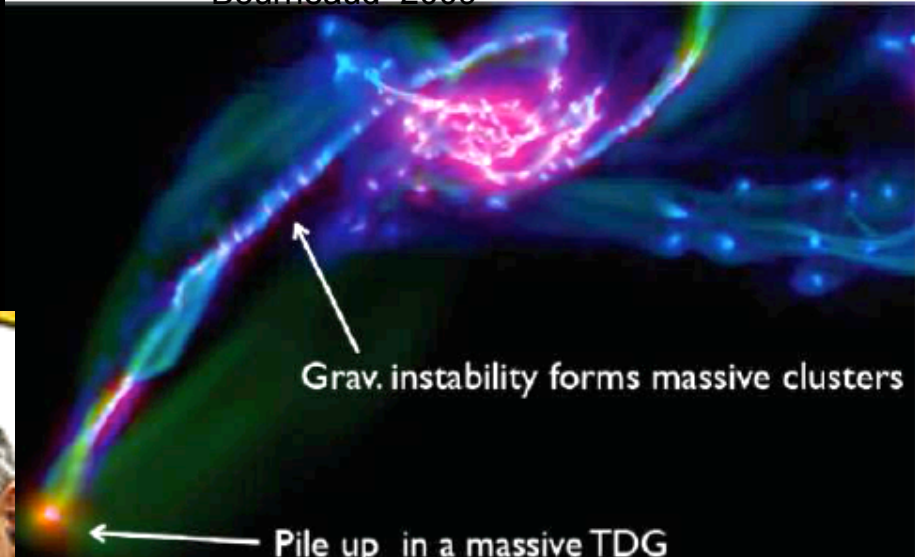
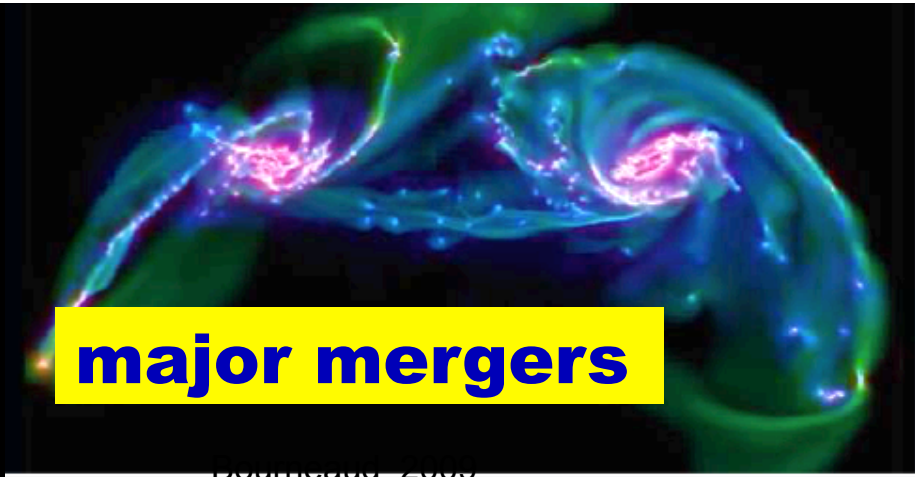
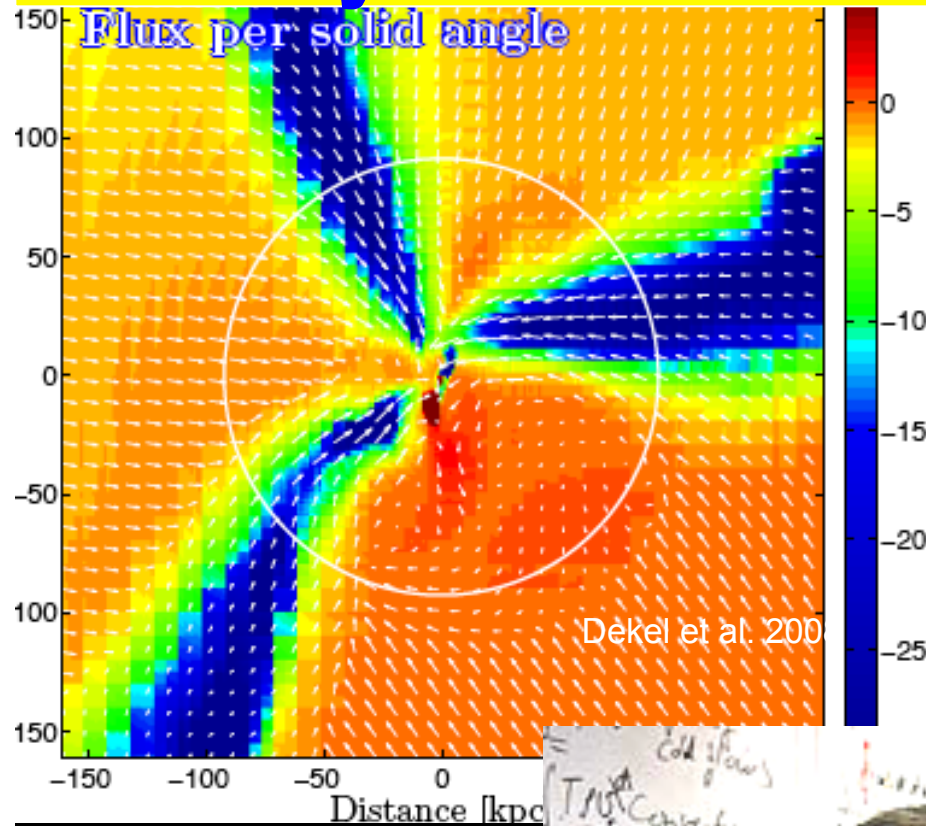
B: with active galactic nuclei

two modes of gas accretion:

A: cold streams/minor mergers

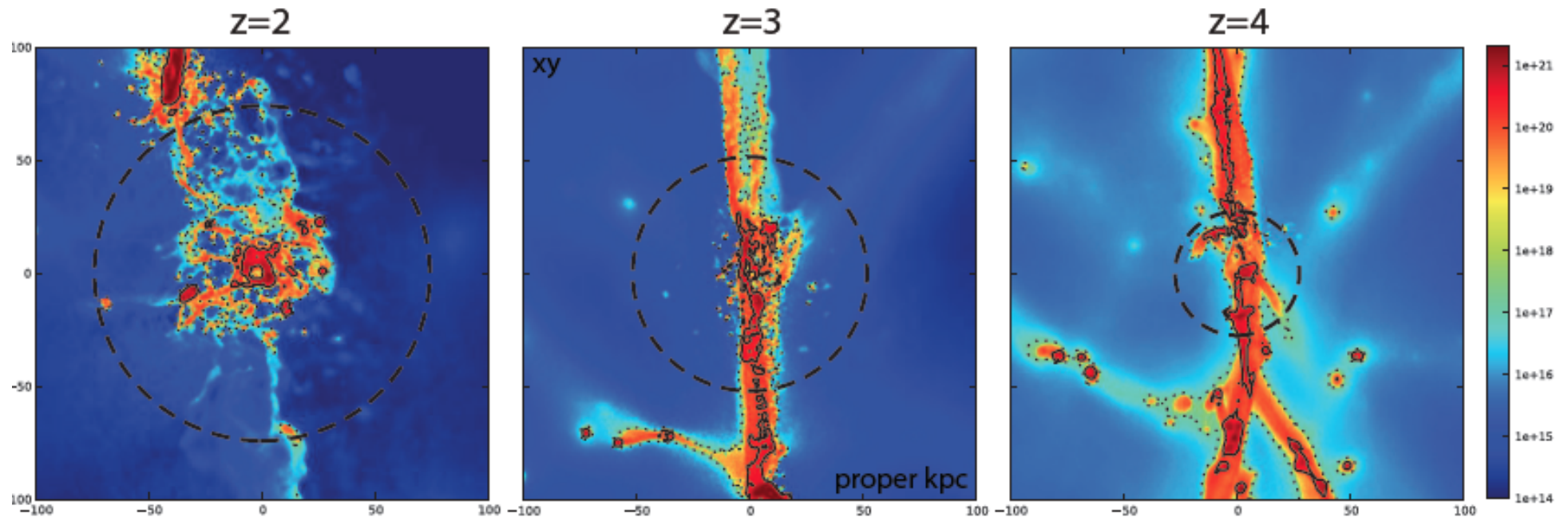
B: major mergers/cooling flows

# Infall by cold streams

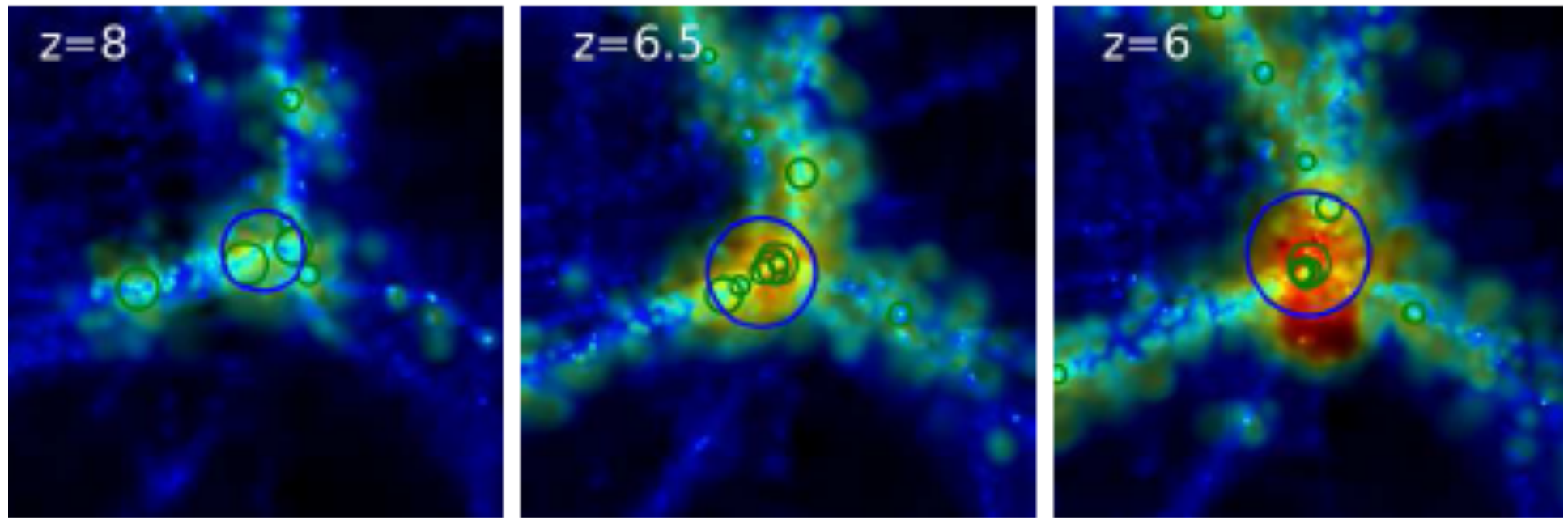


# Where are the cold flows?

Faucher-Giguier & Keres 2010



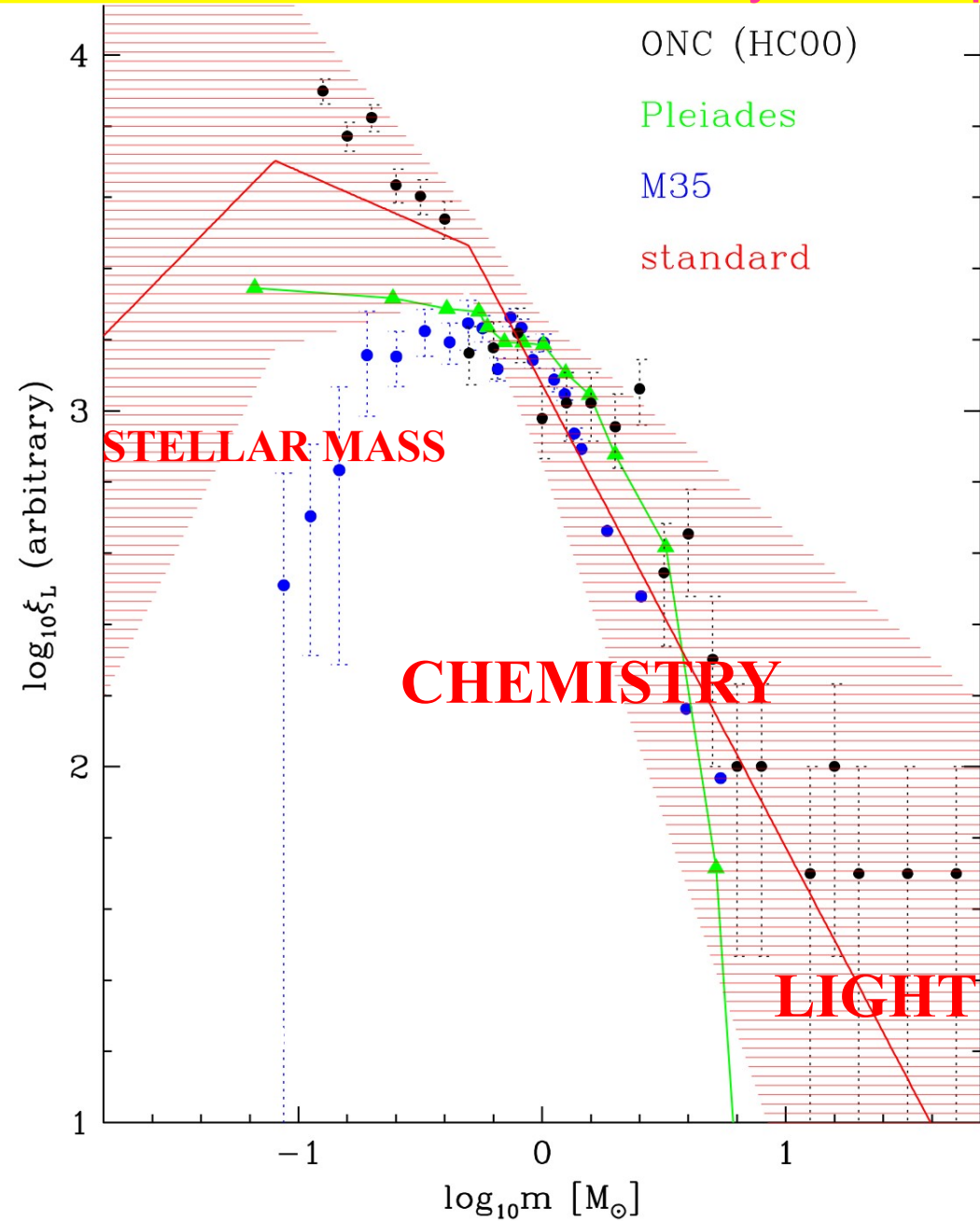
# Feeding the monster



Di Matteo et al. 2011



# The initial stellar mass function is a key assumption





imagine a physicist calculating on a cloud-bound planet and ending with the dramatic conclusion, "What 'happens' is the stars."

“We can imagine a **physicist** on a **cloud-bound** planet who has never heard tell of the stars calculating the ratio of radiation pressure to gas pressure for a series of globes of gas of various sizes, starting, say, with a globe of mass 10 gm., then 100 gm., 1000 gm., and so on, so that his  $n$ th globe contains  $10^n$  gm. . . . Regarded as a tussle between matter and aether (gas pressure and radiation pressure) the contest is overwhelmingly one-sided except between Nos. 33-35, where we may expect something interesting to happen.

What ‘happens’ is the stars.

We draw aside the veil of cloud beneath which our **physicist** has been working and let him look up at the sky. There he will find a thousand million globes of gas nearly all of mass between his 33rd and 35th globes – that is to say, between  $\frac{1}{2}$  and 50 times the sun’s mass.”

Sir **Arthur S. Eddington**: The Internal Constitution of the Stars, 1926



# The life of a star depends on its mass and composition

Gravity versus electromagnetic forces (pressure)

The dimensionless constant that controls the masses of stars

$$\alpha_g \equiv Gm_p^2 e^{-2} \approx 3.10^{-37}$$

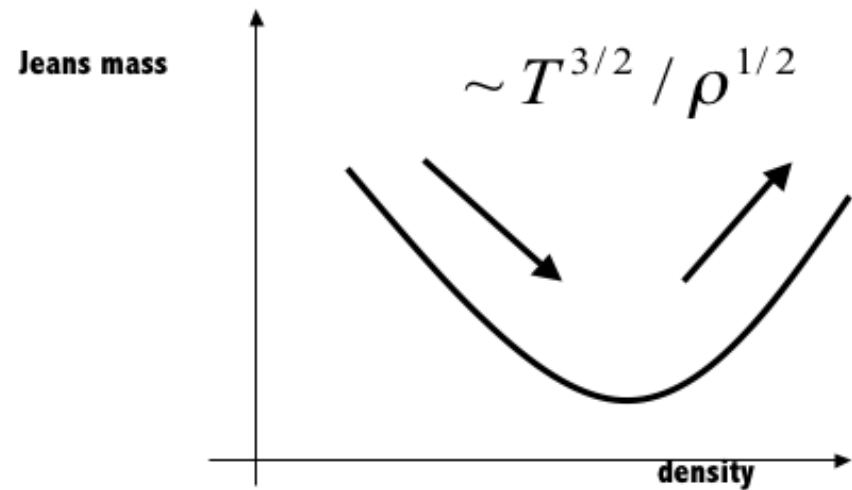
mass of the most massive star...the Eddington mass  $\alpha_g^{-5/3} \alpha^{2/3}$

mass of a white dwarf star...the Chandrasekhar mass  $\alpha_g^{-3/2} \alpha^{-3/2}$

G is Newton's constant,  $m_p$  is the mass of a proton,  $m_e$  is the mass of an electron



# Stars



- Fundamental theory applied to a diffuse interstellar cloud that is collapsing under self-gravity
- Minimum fragment mass

$$\approx \alpha_g^{-3/2} \alpha m_p \approx 0.01 M_{sun}$$

This is a robust but wrong result!

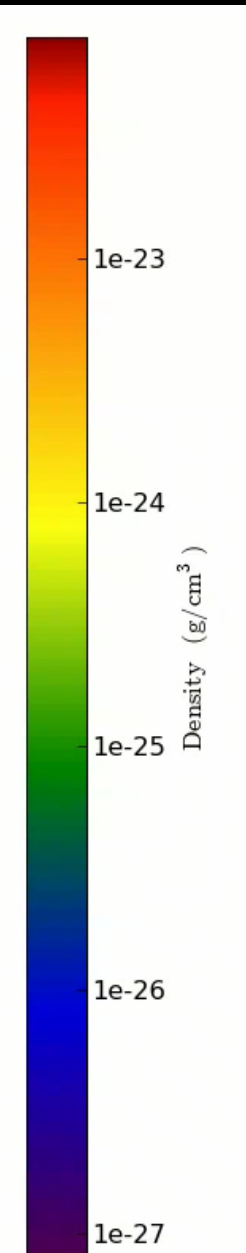
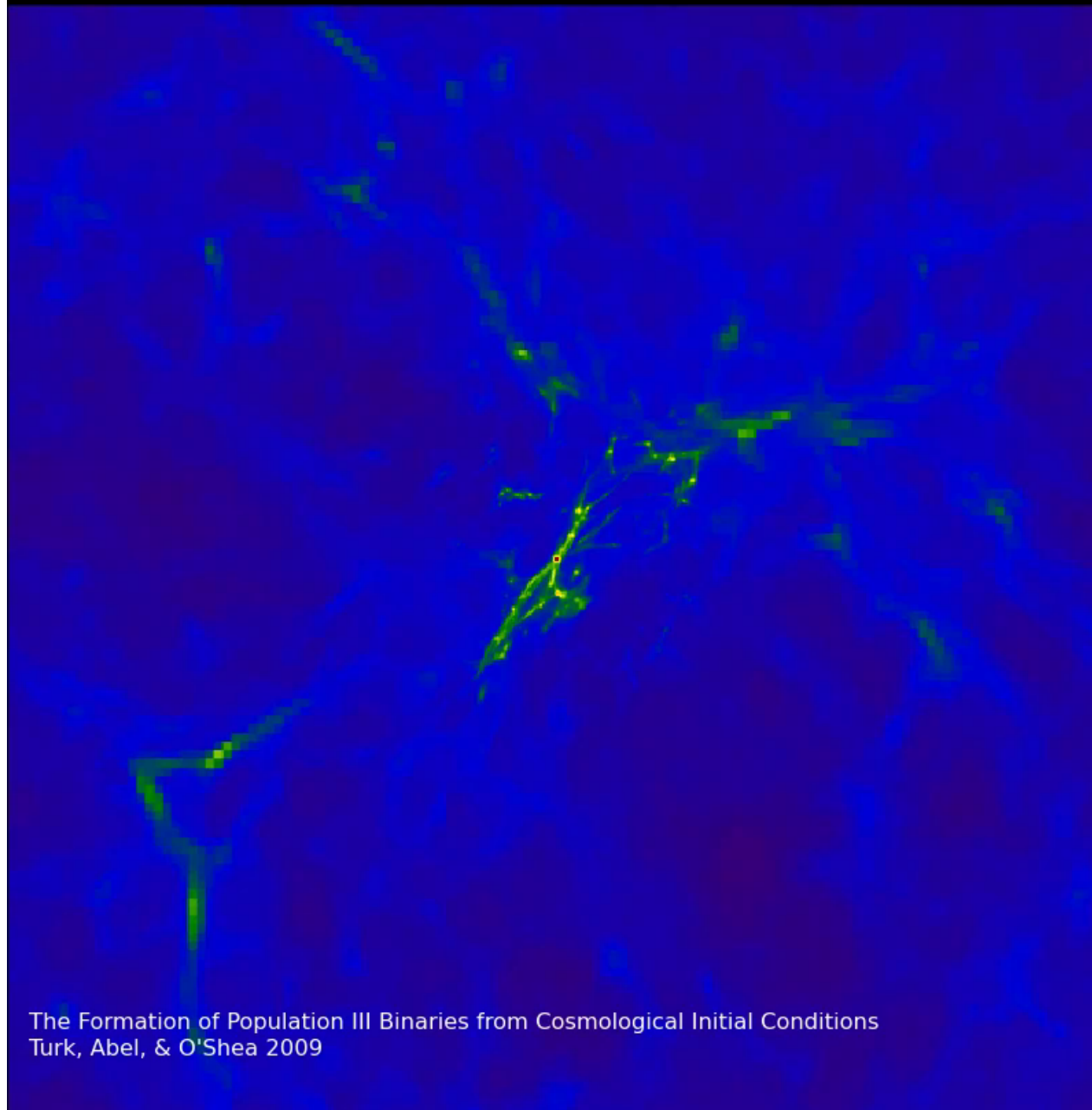
- Resolution: fragmentation + continuing accretion of cold gas, halted by feedback that taps stellar energy via magnetic turbulence
- accretion rate = (sound speed)<sup>3</sup>/G  
 $\Rightarrow$  first stars were massive

$\alpha$  is the fine-structure constant = 1/137

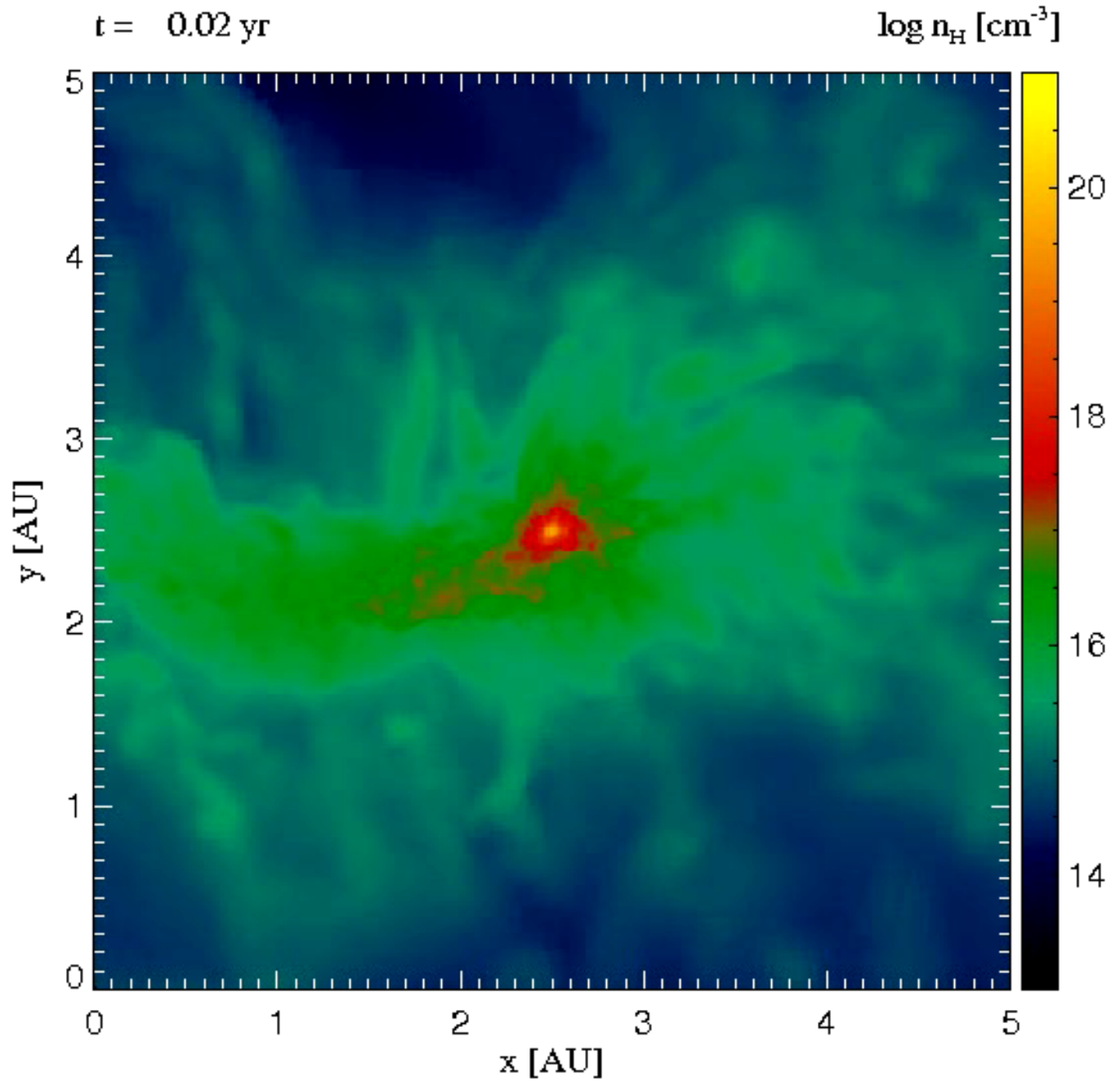
$m_p$  is the mass of a proton

$$\alpha_g \equiv G m_p^2 e^{-2} \approx 3.10^{-37}$$

# The first stars: fragmentation



The Formation of Population III Binaries from Cosmological Initial Conditions  
Turk, Abel, & O'Shea 2009



Greif 2011

# a hybrid model

cold gas flows via filaments/minor mergers  
lead to disk formation/pseudobulges

low efficiency

major mergers + hot infall + cooling  
forms massive spheroids

high efficiency

Is star formation mechanism the same?  
Is IMF universal?

AGN quenching of star formation

Intracluster gas heating by AGN

Baryon ejection: AGN role?

Triggering of star formation by AGN?

SMBH formation?

**improved resolution in theory  
& observation will help...**

