

High Energy Radiation Processes

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Outline

- Introduction
- Particle distribution
- Efficiency of the radiation processes
- Klein-Nishina Regime
- Example

What this talk is about

Malcolm's Talk: Radiation Processes in High Energy Astrophysics

A Physical Approach with Applications

Bremsstrahlung, Synchrotron, inverse Compton (Thomson limit)

This talk: High Energy Radiation Processes

One Zone Modelling

Synchrotron, inverse Compton (Klein-Nishina limit)

Particle Distribution

Microscopical Description

$$dN(q_i, p_i, t) = f(q_i, p_i, t) dq_i dp_i$$

- f is the distribution function
- q_i and p_i are some coordinates in the phase space

$$f = \text{e.g. } \frac{dN}{dV} \quad \text{or} \quad \frac{dN}{d^3x d^3p}$$

- One Zone Modeling typically implies

$$f = \frac{dN}{dE}$$

Particle Distribution

Microscopical Description

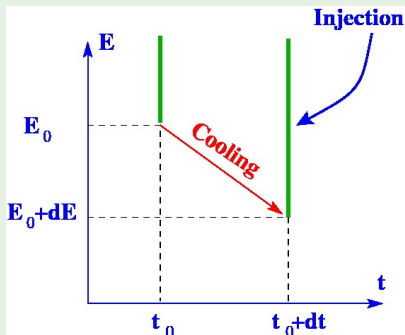
- Boltzmann Equation

$$\frac{\partial f}{\partial t} + \mathbf{v} \frac{\partial f}{\partial \mathbf{r}} + \mathbf{F} \frac{\partial f}{\partial \mathbf{p}} = \left[\frac{\partial f}{\partial t} \right]_{\text{col}}$$

- Collision integral $\left[\frac{\partial f}{\partial t} \right]_{\text{col}}$ accounts for many processes: *particle injection, acceleration, scattering, energy losses, etc*
- In the case of injection/cooling problems, the problem may be significantly simplified under the *continue loss approximation*

Significant simplification in the case of energy losses

Cont. Loss Approx.



Distribution function & Injection

$$dN = f(E, t)dE \quad dN = q(E, t)dEdt$$

$$F(E, t) = \int_E^{\infty} f(E', t)dE'$$

$$F(E + \dot{E}dt, t + dt) =$$

$$F(E, t) + dt \int_E^{\infty} q(E', t)dE'$$

Fokker-Planck Equation

$$\frac{\partial f}{\partial t} + \frac{\partial(\dot{E}f)}{\partial E} = q(E, t)$$

Significant simplification in the case of energy losses

$$F(E + \dot{E}dt, t + dt) = F(E, t) + dt \int_E^{\infty} q(E', t) dE'$$

$$F(E, t) + \frac{\partial F}{\partial E} \dot{E}dt + \frac{\partial F}{\partial t} dt = F(E, t) + dt \int_E^{\infty} q(E', t) dE'$$

$$\frac{\partial}{\partial E} \implies$$

accounting for $\frac{\partial F}{\partial E} = -f$ $\frac{\partial}{\partial E} \int_E^{\infty} q(E', t) dE' = -q$

$$\frac{\partial f}{\partial t} + \frac{\partial(\dot{E}f)}{\partial E} = q(E, t)$$

Particle Energy Distribution

Fokker-Planck Equation Solution

$$f(E, t) = \frac{1}{\dot{E}} \int_E^{E_{\text{eff}}} dE' q(E'), \quad \text{where} \quad t = \int_E^{E_{\text{eff}}} \frac{dE'}{\dot{E}'}$$

$$\dot{E} = \dot{E}_{\text{syn}} + \dot{E}_{\text{ic}} + \dot{E}_{\text{ad}} + \text{etc} / \dot{E}_{\text{syn}} + \dot{E}_{\text{pp}} + \dot{E}_{\text{p}\gamma} + \text{etc}$$

Fast Cooling (*Saturation*)

$$E_{\text{eff}} \rightarrow \infty$$

$$f(E) = \frac{1}{\dot{E}} \int_E^{\infty} dE' q(E')$$

Slow Cooling

$$t \ll E/\dot{E}$$

$$f(E, t) = q(E) \cdot t$$

Some Remarks

Used simplifications

- Acceleration and Losses are treated independently
 - High energy cut-off depends on loss rate
 - Some acceleration processes cannot be treated in this way, e.g. *converter mechanism by Derishev*
- Particles lose energy by small fractions, which is not true for some processes, e.g. IC in the Klein-Nishina regime

Transport Equation with Diffusion and Escape

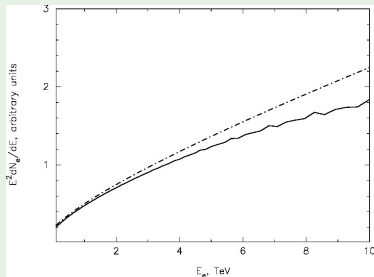
$$\frac{\partial f}{\partial t} + \frac{\partial(\dot{E}f)}{\partial E} + \nabla \cdot (D\nabla f) + \frac{f}{\tau} = q(E, t)$$

also can be solved analytically, see e.g. Ginzburg's "Astrophysics of Cosmic Rays"

Some Remarks

Klein-Nishina and Continues Loss approximation

- Particles lose energy by small fractions, which is not true for some processes, e.g. IC in the Klein-Nishina regime



Solid line: $c\sigma_{\text{ic}}f(\gamma) = q(\gamma) + c \int_{\gamma}^{\infty} d\gamma' f(\gamma') \frac{d\sigma}{dE_{\gamma}}(\gamma', \gamma' - \gamma)$

Dash-dotted line: $f(\gamma) = \frac{1}{E_{\text{ic}}} \int_{\gamma}^{\infty} d\gamma' q(\gamma')$

Some Remarks

High Acceleration Cut-Off

- Acceleration Time

$$t_{\text{acc}} = 0.1\eta E_{\text{TeV}} B_G^{-1} \text{s (where } \eta > 1)$$

- Cooling Time

$$t_{\text{cool}} = E/\dot{E}$$

$$t_{\text{acc}} < t_{\text{cool}}$$

- Dominant Synchrotron Losses

$$\gamma < 10^8 B_G^{-1/2} \eta^{-1/2}$$

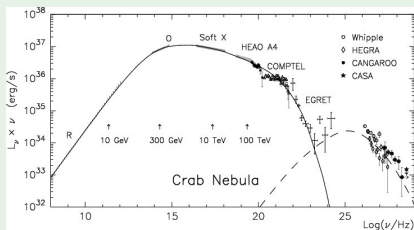
$$\hbar\omega < 100\eta^{-1} \text{MeV}$$

An Extreme Accelerator?

Crab Nebula



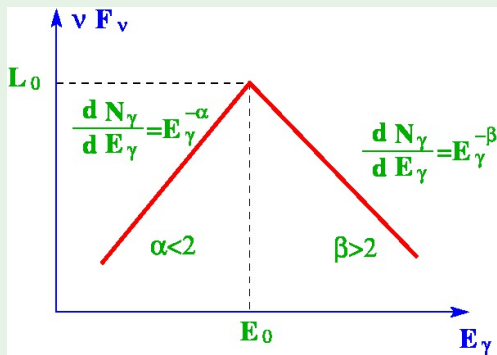
Broad Band Spectrum



νF_ν peak gives the luminosity

νF_ν peaking distribution

$$\nu F_\nu = E_\gamma^2 \frac{dN_\gamma}{dE_\gamma}$$



$$L_\gamma = \int dE_\gamma E_\gamma \frac{dN_\gamma}{dE_\gamma} =$$

$$\int_{E_{\min}}^{E_0} dE_\gamma E_\gamma^{1-\alpha} + \int_{E_0}^{E_{\max}} dE_\gamma E_\gamma^{1-\beta}$$

$$E_{\min} \ll E_0 \ll E_{\max}$$

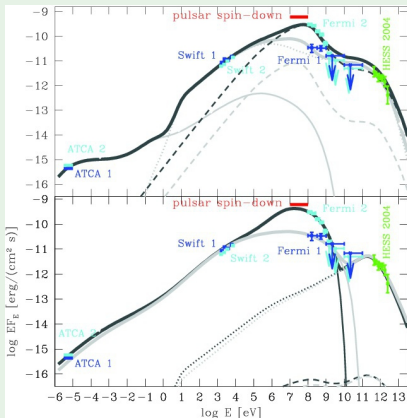
$$L_\gamma = L_0 \left(\frac{1}{2-\alpha} + \frac{1}{\beta-2} \right)$$

For $\alpha = 1.5$ and $\beta = 2.5$

$$L_\gamma = 4L_0$$

νF_ν peak gives order of magnitude estimate of the luminosity

Fermi/LAT observations of PSR B1259-63



Detailed information about the pulsar spin-down luminosity provides very precise information about the available energetics

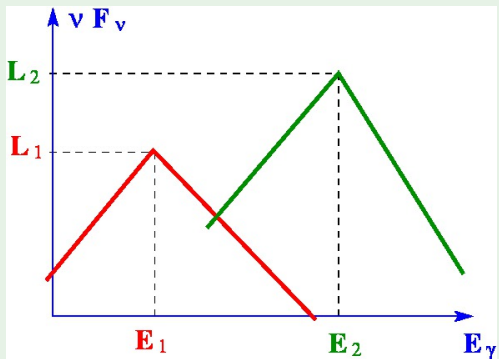
$$L_{\text{SD}} = 8.3 \times 10^{35} \text{ erg s}^{-1}$$

$$L_{\text{LAT}} = 8 \times 10^{35} \left(\frac{D}{2.3 \text{ kpc}} \right)^2 \text{ erg s}^{-1}$$

Even in this case, there are unavoidable uncertainties related to the distance to the source...

Radiation Production

Emission of a Particle (two channels)



Single particle spectra:

$$\frac{dN_i}{dE_\gamma} = K_i(E_\gamma, E_0)$$

Total luminosity:

$$L = \dot{E}_1 + \dot{E}_2$$

Luminosity per channel:

$$L_i = \frac{\dot{E}_i}{\dot{E}_1 + \dot{E}_2} L$$

Ratio of the humps:

$$\frac{L_1}{L_2} = \frac{\dot{E}_1}{\dot{E}_2}$$

Comparison of Radiation Mechanisms

Radiation Efficiency

- Escape Time: $t_{\text{esc}} = \min(t_{\text{diff}}, t_{\text{ad}})$

$$t_{\text{diff}} = \frac{R^2}{2D} \sim 2 \cdot 10^4 \zeta^{-1} R_{12}^2 B_1 E_1^{-1} \text{ s}, \quad \zeta = \frac{D}{D_{\text{Bohm}}}$$

$$t_{\text{ad}} = \frac{R}{V_{\text{bulk}}} \sim 10^2 R_{12} V_{10}^{-1} \text{ s}$$

- Energy Transfer: $\mu = \frac{E_\gamma}{E_0}$
- Radiation Efficiency: $\kappa = \mu \min(1, t_{\text{esc}}/t_{\text{int}})$

Radiation Mechanism in BS

Inverse Compton Scattering

- Cooling Time:

$$t_{\text{ic}} = 40 \left(\frac{L}{10^{38} \text{erg/s}} \right)^{-1} \left(\frac{R}{10^{12} \text{cm}} \right)^2 \left(\frac{T}{3 \cdot 10^4 \text{K}} \right)^{1.7} E_{\text{TeV}}^{0.7} \text{ s}$$

- Energy Transfer:

$$E_{\gamma} = \begin{cases} E_e, & \epsilon E \gg m^2 c^4 \\ \frac{\epsilon E_e^2}{m^2 c^4}, & \epsilon E \ll m^2 c^4 \end{cases}$$

- Radiation Efficiency

$$\kappa \sim 1$$

Radiation Mechanism in BS

Proton-proton interaction

- Cooling Time:

$$t_{pp} = 10^6 \left(\frac{n_p}{10^9 \text{cm}^{-3}} \right)^{-1} \text{ s}$$

- Energy Transfer:

$$E_\gamma \sim 0.1 E_p$$

- Radiation Efficiency

$$\kappa = 10^{-3} \frac{t_{\text{esc}}}{10^4 \text{s}} \frac{n_p}{10^9 \text{cm}^{-3}}$$

Radiation Mechanism in BS

Photo-meson production

- Cooling Time:

$$t_{p\gamma} = 3 \cdot 10^4 \left(\frac{L}{10^{38} \text{erg/s}} \right)^{-1} \left(\frac{R}{10^{12} \text{cm}} \right)^2 \left(\frac{T}{3 \cdot 10^4 \text{K}} \right) \text{s}$$

- Energy Transfer:

$$E_\gamma \sim 0.1 E_p$$

- Radiation Efficiency

$$\kappa = 0.03 \frac{t_{\text{esc}}}{10^4 \text{s}} \frac{L}{10^{38} \text{erg/s}} \left(\frac{R}{10^{12} \text{cm}} \right)^{-2} \left(\frac{T}{3 \cdot 10^4 \text{K}} \right)^{-1}$$

Radiation Mechanism in BS

Photo-disintegration (see Bosch-Ramon&Khangulyan, 2009)

- Cooling Time:

$$t_{\text{pd}} \sim 3 \cdot 10^3 \left(\frac{L}{10^{38} \text{erg/s}} \right)^{-1} \left(\frac{T}{3 \cdot 10^4 \text{K}} \right) \left(\frac{R}{10^{12} \text{cm}} \right)^2 \text{ s}$$

- Energy Transfer:

$$E_{\gamma} \sim 0.01 E_N$$

- Radiation Efficiency

$$\kappa = 0.03 \frac{t_{\text{esc}}}{10^4 \text{s}} \frac{L}{10^{38} \text{erg/s}} \left(\frac{R}{10^{12} \text{cm}} \right)^{-2} \left(\frac{T}{3 \cdot 10^4 \text{K}} \right)^{-1}$$

The most Favorable Emission Process in BS

Radiation Processes

Proc.	E_γ/E_0	κ
IC	1	1
pp	0.1	$10^{-3} \frac{t_{\text{esc}}}{10^4 \text{s}} \frac{n_p}{10^9 \text{cm}^{-3}}$
$p\gamma$	0.1	$0.03 \frac{t_{\text{esc}}}{10^4 \text{s}} \frac{L}{10^{38} \text{erg/s}} \left(\frac{R}{10^{12} \text{cm}}\right)^{-2} \left(\frac{T}{3 \cdot 10^4 \text{K}}\right)^{-1}$
Photo-des.	0.01	$0.03 \frac{t_{\text{esc}}}{10^4 \text{s}} \frac{L}{10^{38} \text{erg/s}} \left(\frac{R}{10^{12} \text{cm}}\right)^{-2} \left(\frac{T}{3 \cdot 10^4 \text{K}}\right)^{-1}$

Proton Synchrotron

Electrons

- Cooling: $t_{\text{cool}} = 400 E_{\text{TeV}}^{-1} B_G^{-2} \text{ s}$
- Photon Energy:
 $\hbar\omega = 20 E_{\text{TeV}}^2 B_G \text{ keV}$
- Highest Energy Cooling:
 $t_{\text{cool}} = 6\eta^{1/2} B_G^{-3/2} \text{ s}$
- Highest Energy Photons:
 $\hbar\omega = 100\eta^{-1} \text{ MeV}$

Protons

- Cooling:
 $t_{\text{cool}} = 400 E_{\text{TeV}}^{-1} B_G^{-2} \left(\frac{m_p}{m_e}\right)^4 \text{ s}$
- Photon Energy: $\hbar\omega = 20 E_{\text{TeV}}^2 B_G \left(\frac{m_e}{m_p}\right)^3 \text{ keV}$
- Highest Energy Cooling:
 $t_{\text{cool}} = 6\eta^{1/2} B_G^{-3/2} \left(\frac{m_p}{m_e}\right)^2 \text{ s}$
- Highest Energy Photons:
 $\hbar\omega = 100\eta^{-1} \left(\frac{m_p}{m_e}\right) \text{ MeV}$

Synchrotron-IC Model

Very similar processes

- Energy Losses

$$\dot{E}_{\text{IC}} = -\frac{4}{3} U_{\text{ph}} c \gamma^2$$

$$\dot{E}_{\text{syn}} = -\frac{4}{3} U_{\text{B}} c \gamma^2$$

- Mean Energy

$$\hbar\omega = \left(\frac{4}{3} \hbar\omega_0\right) \gamma^2$$

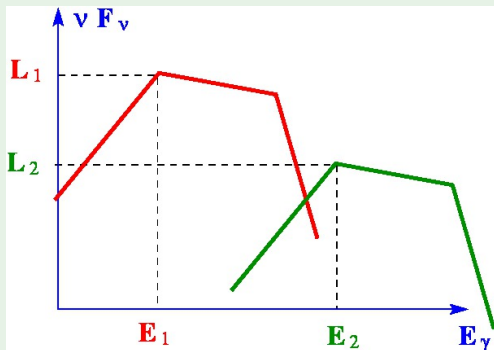
$$\hbar\omega = \left(\frac{eB\hbar}{2\pi m_e c}\right) \gamma^2$$

$$\frac{L_{\text{syn}}}{L_{\text{ic}}} = \frac{U_{\text{B}}}{U_{\text{ph}}}$$

$$\frac{\hbar\omega_{\text{syn}}}{\hbar\omega_{\text{ic}}} = \frac{\left(\frac{eB\hbar}{2\pi m_e c}\right)}{\left(\frac{4}{3} \hbar\omega_0\right)}$$

Synchrotron-IC Model

Two identical humps?



Ratio of the peaks

$$\frac{L_{\text{syn}}}{L_{\text{ic}}} = \frac{U_B}{U_{\text{ph}}}$$

Ratio of the energies

$$\frac{\hbar\omega_{\text{syn}}}{\hbar\omega_{\text{ic}}} = \frac{\left(\frac{eB\hbar}{2\pi m_e c}\right)}{\left(\frac{4}{3}\hbar\omega_0\right)}$$

Kein-Nishina Cut-off

Photon Energy < Electron Energy

$$\hbar\omega = \left(\frac{4}{3}\hbar\omega_0\right) \gamma^2 < \gamma m_e c^2$$

$$\gamma < \left(\frac{m_e c^2}{\frac{4}{3}\hbar\omega_0}\right)$$

$$\gamma < 5 \times 10^5 \omega_{0,\text{eV}}^{-1}$$

$$\hbar\omega = \left(\frac{eB\hbar}{2\pi m_e c}\right) \gamma^2 < \gamma m_e c^2$$

$$\gamma < \left(\frac{2\pi m_e^2 c^3}{eB\hbar}\right)$$

$$\gamma < 3 \times 10^{14} B_G^{-1}$$

Some Remarks

High Acceleration Cut-Off

- Acceleration Time

$$t_{\text{acc}} = 0.1\eta E_{\text{TeV}} B_G^{-1} \text{s (where } \eta > 1)$$

- Cooling Time

$$t_{\text{cool}} = E/\dot{E}$$

$$t_{\text{acc}} < t_{\text{cool}}$$

- Dominant Synchrotron Losses

$$\gamma < 10^8 B_G^{-1/2} \eta^{-1/2}$$

$$\hbar\omega < 100\eta^{-1} \text{MeV}$$

Kein-Nishina Cut-off

Photon Energy < Electron Energy

$$\hbar\omega = \left(\frac{4}{3}\hbar\omega_0\right)\gamma^2 < \gamma m_e c^2$$

$$\gamma < \left(\frac{m_e c^2}{\frac{4}{3}\hbar\omega_0}\right)$$

$$\gamma < 5 \times 10^5 \omega_{0,\text{eV}}^{-1}$$

$$\hbar\omega = \left(\frac{eB\hbar}{2\pi m_e c}\right)\gamma^2 < \gamma m_e c^2$$

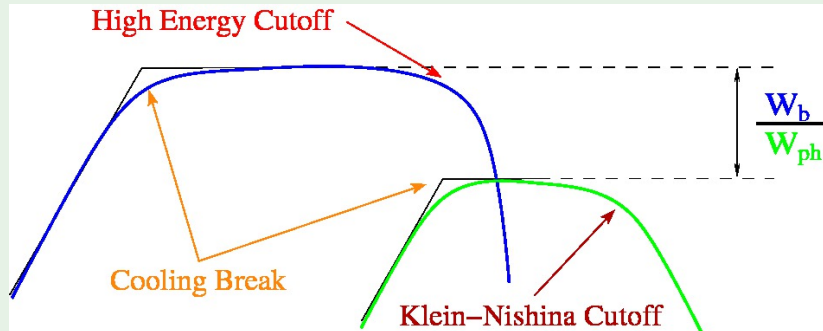
$$\gamma < \left(\frac{2\pi m_e^2 c^3}{eB\hbar}\right)$$

$$\gamma < 3 \times 10^{14} B_G^{-1}$$

$$B_G > 10^{12} \eta$$

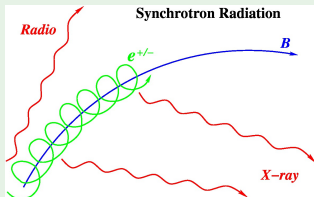
Leptonic Radiation Mechanisms

Typical SED



Synchrotron Radiation

Electrons can interact with B-field



- Energy Losses: $\dot{E}_{\text{syn}} = -\frac{4}{3} U_B c \gamma^2$
- Mean Energy: $\hbar\omega = \left(\frac{eB\hbar}{2\pi m_e c}\right) \gamma^2$
- Single Particle Spectrum:

$$\frac{dI_{\text{syn}}}{d\omega} = \frac{\sqrt{3}}{2\pi} \frac{e^3 B}{mc^2} F\left(\frac{\omega}{\omega_c}\right)$$

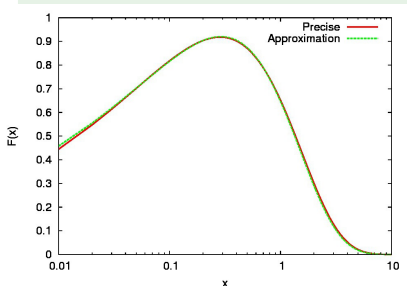
$$\text{where } \omega_c = \frac{3eB\gamma^2}{2mc}$$

- Useful approximation:

$$F(x) = x \int_x^\infty K_{5/3}(x') dx' = 1.76 x^{0.29} e^{-x}$$

Synchrotron Radiation

Approximation for the peak



- $x \gg 1$

$$F(x) = \left(\frac{\pi}{2}\right)^{1/2} x^{1/2} e^{-x}$$

- $x \ll 1$

$$F(x) = \frac{4\pi}{\sqrt{3}\Gamma(1/3)} x^{1/3}$$

- Useful approximation (but not an asymptotic):

$$F(x) = x \int_x^{\infty} K_{5/3}(x') dx' = 1.76 x^{0.29} e^{-x}$$

Inverse Compton Radiation

Electrons can interact with photon field

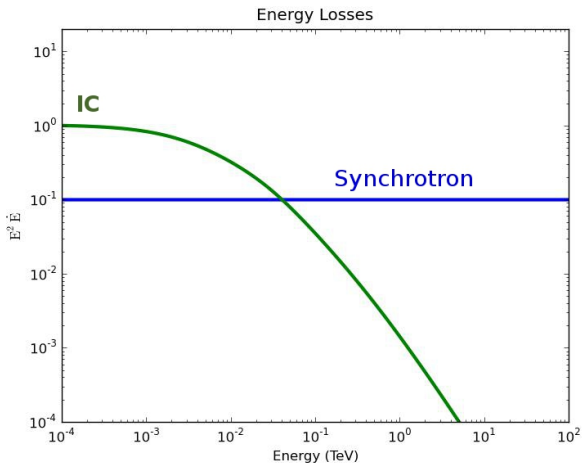
- Maximum Energy of Gamma Rays $E_\gamma < \frac{\gamma(1 - \frac{1}{4\gamma^2})}{1 + \frac{1}{4\gamma\epsilon}}$
- Single Particle Spectrum:

$$\frac{d\sigma_\gamma}{dE_\gamma} = \frac{\pi r_e^2 \epsilon^2 E_\gamma}{\gamma^3 (\gamma - E_\gamma)} \left[\ln \frac{E_\gamma}{\gamma \epsilon (\gamma - E_\gamma)} + (4\epsilon \gamma^2 - 4\gamma \epsilon E_\gamma - E_\gamma) \frac{(2\epsilon \gamma^2 - 2\gamma \epsilon E_\gamma + \epsilon E_\gamma^2 + E_\gamma)}{4E_\gamma \gamma \epsilon (\gamma - E_\gamma)} \right]$$

- Energy Losses for a Planckian photon field:

$$\dot{\gamma}_{IC} = 5.5 \times 10^{17} T_{mcc}^3 \gamma \frac{\ln(1 + 0.55\gamma T_{mcc})}{1 + 25T_{mcc}\gamma} \left(1 + \frac{1.4\gamma T_{mcc}}{1 + 12\gamma^2 T_{mcc}^2} \right) s^{-1},$$

Klein-Nishina Effect



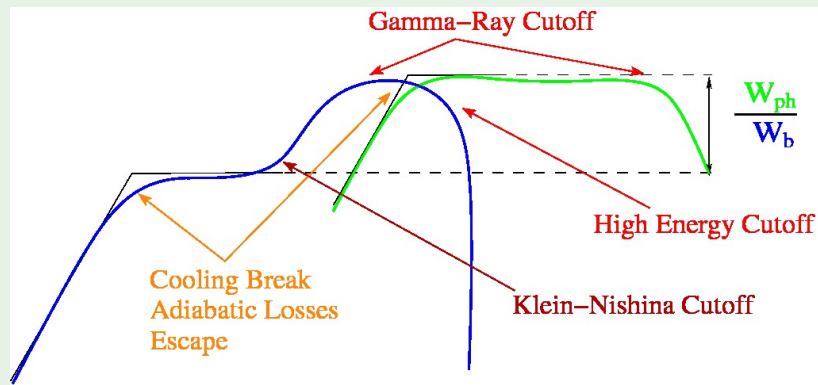
Klein-Nishina Effect

$$\frac{dN_e}{dE} = \frac{1}{\dot{E}} \int_E^{\infty} dE' Q(E) \quad \dot{E} = \dot{E}_{\text{syn}} + \dot{E}_{\text{ic}}$$

Klein-Nishina Effect

- X-ray: hardening
- γ -rays: no Klein-Nishina cutoff

Klein-Nishina Effect



Compton Scattering Spectrum

$$\frac{dN_\gamma}{dE_\gamma} = \int dE_e c(1 - \cos \theta) n_{\text{ph}} \frac{dN_e}{dE_e} \frac{d\sigma}{dE_\gamma}$$

$$\begin{aligned} \frac{d^2N(\theta, \omega)}{d\omega d\Omega} &= \frac{r_0^2}{2\omega_0 E^2} \left[1 + \frac{\omega^2}{2E(E - \omega)} - \frac{\omega}{\omega_0 E(E - \omega)(1 - \cos \theta)} + \right. \\ &\quad \left. + \frac{\omega^2}{2\omega_0^2 E^2 (E - \omega)^2 (1 - \cos \theta)^2} \right] \\ &\equiv \frac{r_0^2}{2\omega_0 E^2} \left[1 + \frac{z^2}{2(1 - z)} - \frac{2z}{b_\theta(1 - z)} + \frac{2z^2}{b_\theta^2(1 - z)^2} \right], \end{aligned}$$

where $b_\theta \equiv 2(1 - \cos \theta)\omega_0 E$, $z \equiv \omega/E$, and ω changes in the limits

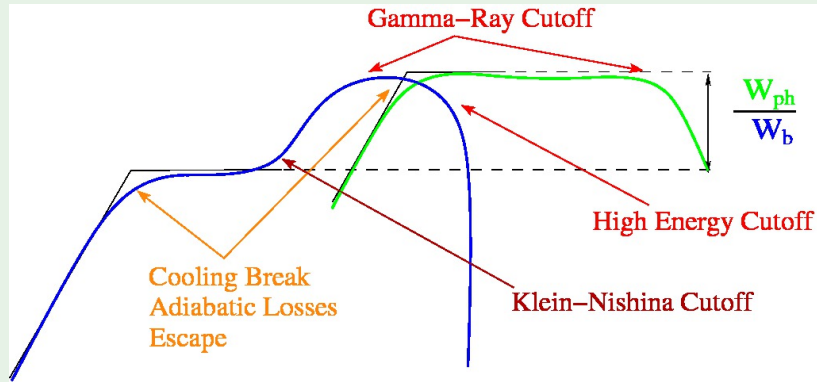
$$\omega_0 \ll \omega \leq \frac{b_\theta}{1 + b_\theta} E.$$

Aharonian&Atoyan, 1981

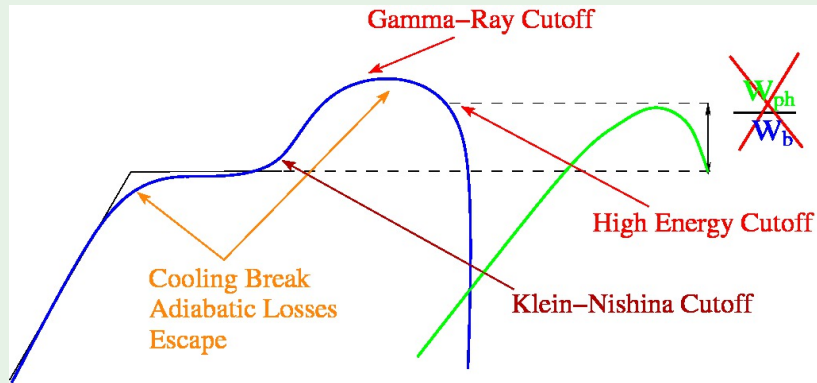
$$\frac{dN_\gamma}{dE_\gamma} = \int dE_e c(1 - \cos \theta) n_{\text{ph}} \frac{dN_e}{dE_e} \frac{d\sigma}{dE_\gamma}$$

Anisotropic inverse Compton

Klein-Nishina Effect



Klein-Nishina + Anisotropic IC

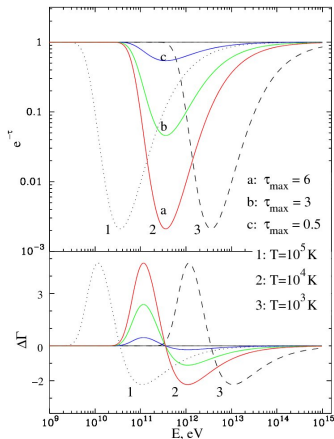


Gamma-Gamma Absorption

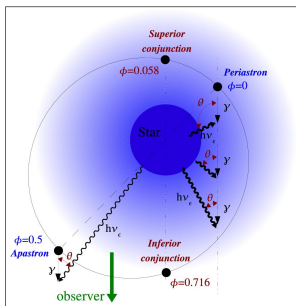
- The KN regime implies importance of γ - γ absorption

$$\gamma\epsilon > 1$$

- Does KN imply strong attenuation?
- Does strong attenuation implies EMC?



LS 5039

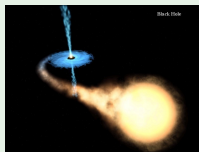


From Aharonian et al., 2006
 A general study of γ - and X-rays
 production in the leptonic scenario

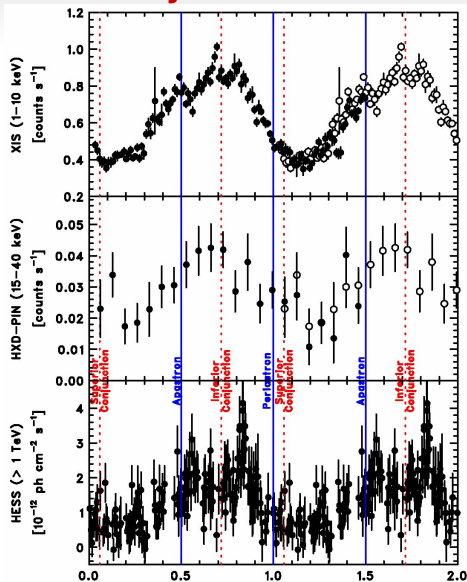
Binary Pulsar



Microquasar



X-ray and TeV emission from LS5039



- Variable/Periodic
- Apparent similarities in lightcurves
- Hard distributions of parent particles

Takahashi et al., 2009

X-ray and TeV emission from LS5039

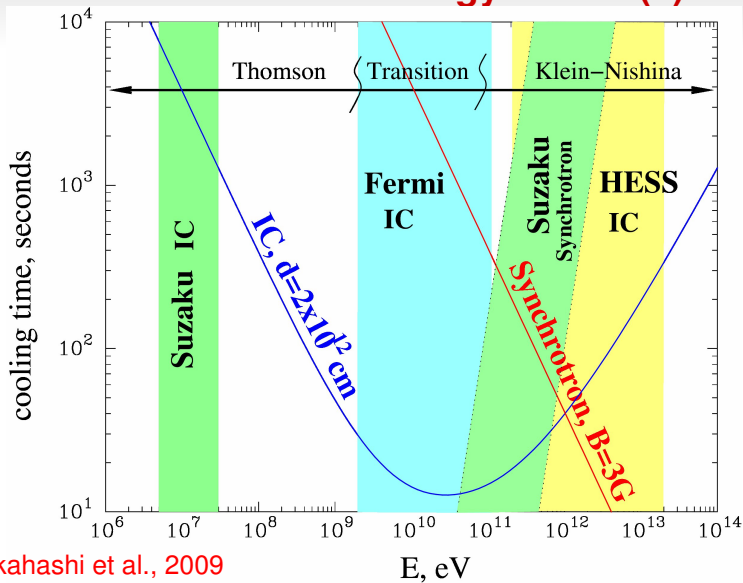
TeV (Aharonian et al., 2006)

- Variable
- Periodic
- Strong variability in flux level
- Significant variability in photon index
- SUPC: lower fluxes and steeper spectra
- INFC: higher fluxes and harder spectra
- Very hard spectra at INFC

X-ray (Takahashi et al., 2009)

- Variable
- Seems to be periodic
- Significant variability in flux level
- Minor variability in photon index
- SUPC: lower fluxes and steeper spectra
- INFC: higher fluxes and harder spectra
- Hard spectra

Time-scales and Energy Bands (II)



Takahashi et al., 2009

Modeling (results)

- Adiabatic cooling rate from X-ray data
- Good agreement with HESS fluxes
- Acceptable agreement with HESS spectral indexes
- Testable prediction for Fermi

