

DIFFUSIVE SHOCK ACCELERATION

Pasquale Blasi

Gran Sasso Science Institute

OUTLINE OF THE LECTURE

- *Principles of CR transport*
- *Second Order Fermi Acceleration*
- *Diffusive Shock Acceleration (DSA): test particle theory*
- *Diffusive Shock Re-acceleration*
- *Non linear theory of DSA*
 - ✓ *non linear dynamical reaction of accelerated particles*
 - ✓ *non linear B-field amplification due to accelerated particles*
 - ✓ *phenomenology of non linear DSA*
- *DSA in partially ionized media - test particle theory*
- *DSA in partially ionized media - non linear theory*
- *Phenomenology of DSA in partially ionized media*

COSMIC RAY TRANSPORT

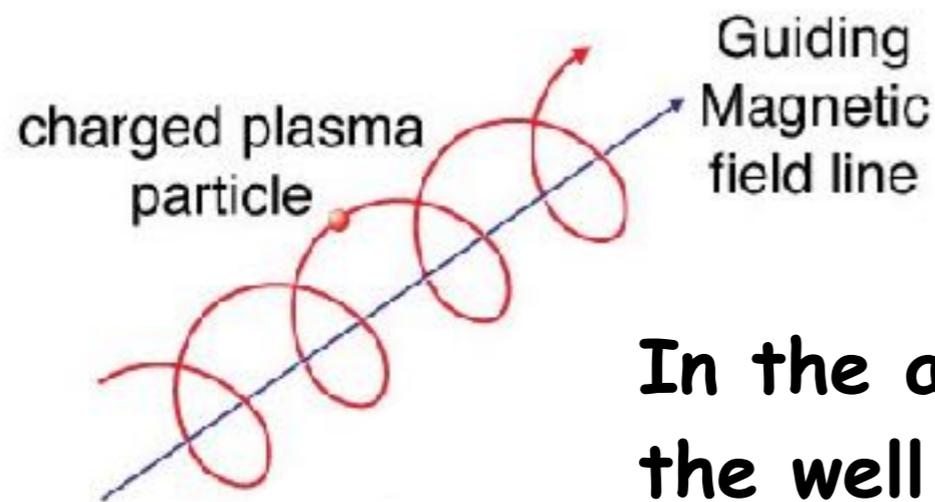
**CHARGED PARTICLES
IN A MAGNETIC FIELD**

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graph TD; A[CHARGED PARTICLES IN A MAGNETIC FIELD] --> B[DIFFUSIVE PARTICLE ACCELERATION]; A --> C[COSMIC RAY PROPAGATION IN THE GALAXY AND OUTSIDE];
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**DIFFUSIVE PARTICLE
ACCELERATION**

**COSMIC RAY
PROPAGATION IN THE
GALAXY AND OUTSIDE**

CHARGED PARTICLES IN A REGULAR B FIELD



$$\frac{d\vec{p}}{dt} = q \left[\vec{E} + \frac{\vec{v}}{c} \times \vec{B} \right]$$

In the absence of an electric field one obtains the well known solution:

$$p_z = \text{Constant}$$

$$v_x = V_0 \cos[\Omega t]$$

$$v_y = V_0 \sin[\Omega t]$$

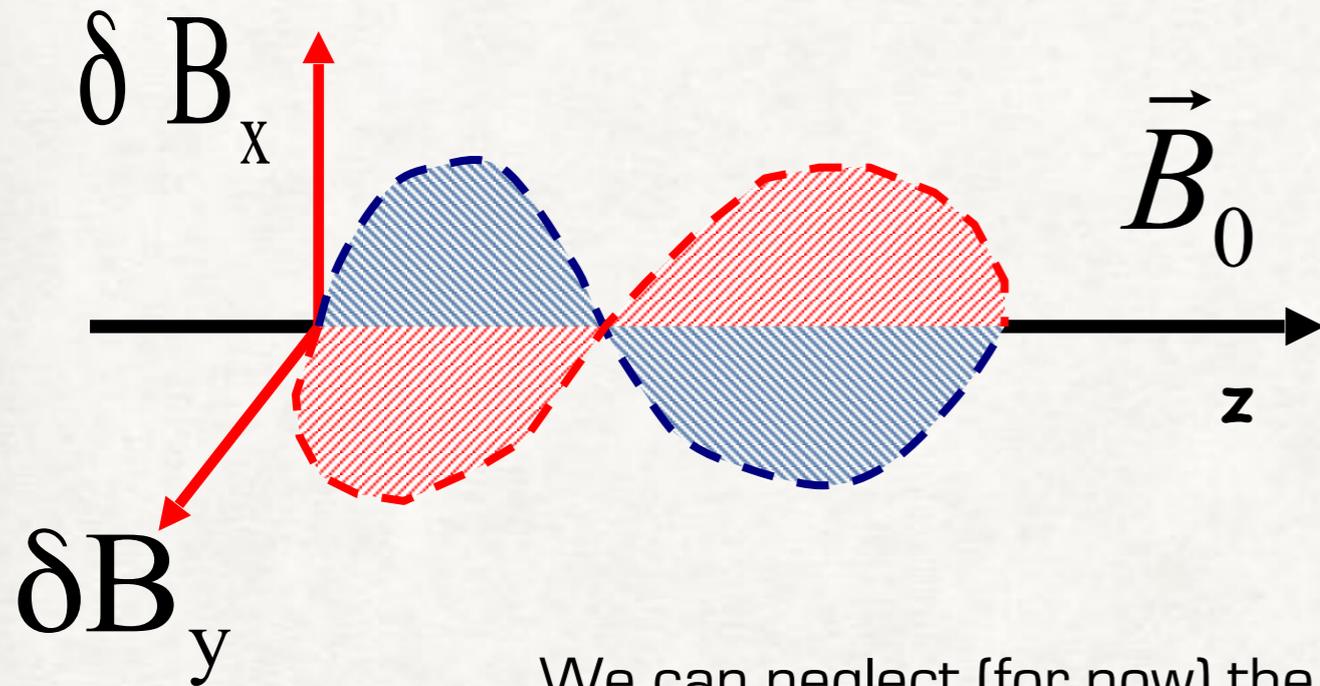
LARMOR FREQUENCY

$$\Omega = \frac{q B_0}{m c \gamma}$$

A FEW THINGS TO KEEP IN MIND

- THE MAGNETIC FIELD DOES NOT CHANGE PARTICLE ENERGY \rightarrow NO ACCELERATION BY B FIELDS
- A RELATIVISTIC PARTICLE MOVES IN THE Z DIRECTION ON AVERAGE AT $c/3$

MOTION OF A PARTICLE IN A WAVY FIELD



Let us consider an Alfvén wave propagating in the z direction:

$$\delta B \ll B_0 \quad \delta \vec{B} \perp \vec{B}_0$$

We can neglect (for now) the electric field associated with the wave, or in other words we can sit in the reference frame of the wave:

$$\frac{d\vec{p}}{dt} = q \frac{\vec{v}}{c} \times (\vec{B}_0 + \delta \vec{B})$$

THIS CHANGES ONLY THE X AND Y COMPONENTS OF THE MOMENTUM

THIS TERM CHANGES ONLY THE DIRECTION OF $P_z = P_\mu$

Remember that the wave typically moves with the Alfvén speed:

$$v_a = \frac{B}{(4\pi\rho)^{1/2}} = 2 \times 10^6 B_\mu n_1^{-1/2} \text{ cm/s}$$

Alfvén waves have frequencies \ll ion gyration frequency $\Omega_p = qB/m_p c$

It is therefore clear that for a relativistic particle these waves, in first approximation, look like static waves.

The equation of motion can be written as:

$$\frac{d\vec{p}}{dt} = \frac{q}{c} \vec{v} \times (\vec{B}_0 + \delta\vec{B})$$

If to split the momentum in parallel and perpendicular, the perpendicular component cannot change in modulus, while the parallel momentum is described by

$$\frac{dp_{\parallel}}{dt} = \frac{q}{c} |\vec{v}_{\perp} \times \delta\vec{B}| \quad p_{\parallel} = p \mu$$

$$\frac{d\mu}{dt} = \frac{q}{pc} v (1 - \mu^2)^{1/2} \delta B \cos(\Omega t - kx + \psi)$$

Wave form of the magnetic field with a random phase and frequency

$$\Omega = qB_0/mc\gamma \quad \text{Larmor frequency}$$

In the frame in which the wave is at rest we can write $x = v\mu t$

$$\frac{d\mu}{dt} = \frac{q}{pc} v (1 - \mu^2)^{1/2} \delta B \cos [(\Omega - kv\mu)t + \psi]$$

It is clear that the mean value of the pitch angle variation over a long enough time vanishes

$$\langle \Delta\mu \rangle_t = 0$$

We want to see now what happens to $\langle \Delta\mu \Delta\mu \rangle$

Let us first average upon the random phase of the waves:

$$\langle \Delta\mu(t') \Delta\mu(t'') \rangle_\psi = \frac{q^2 v^2 (1 - \mu^2) \delta B^2}{2c^2 p^2} \cos [(\Omega - kv\mu)(t' - t'')]]$$

And integrating over time:

$$\begin{aligned} \langle \Delta\mu \Delta\mu \rangle_t &= \frac{q^2 v^2 (1 - \mu^2) \delta B^2}{2c^2 p^2} \int dt' \int dt'' \cos [(\Omega - kv\mu)(t' - t'')]] \\ &= \frac{q^2 v (1 - \mu^2) \delta B^2}{c^2 p^2 \mu} \delta(k - \Omega/v\mu) \Delta t \end{aligned}$$


RESONANCE

Many waves

IN GENERAL ONE DOES NOT HAVE A SINGLE WAVE BUT RATHER A POWER SPECTRUM:

$$P(k) = B_k^2 / 4\pi$$

THEREFORE INTEGRATING OVER ALL OF THEM:

$$\left\langle \frac{\Delta\mu\Delta\mu}{\Delta t} \right\rangle = \frac{q^2(1-\mu^2)\pi}{m^2c^2\gamma^2} \frac{1}{v\mu} 4\pi \int dk \frac{\delta B(k)^2}{4\pi} \delta(k - \Omega/v\mu)$$

OR IN A MORE IMMEDIATE FORMALISM:

$$\left\langle \frac{\Delta\mu\Delta\mu}{\Delta t} \right\rangle = \frac{\pi}{2} \Omega (1-\mu^2) k_{\text{res}} F(k_{\text{res}})$$

$$k_{\text{res}} = \frac{\Omega}{v\mu}$$

RESONANCE!!!

DIFFUSION COEFFICIENT

THE RANDOM CHANGE OF THE PITCH ANGLE IS DESCRIBED BY A DIFFUSION COEFFICIENT

$$D_{\mu\mu} = \left\langle \frac{\Delta\theta\Delta\theta}{\Delta t} \right\rangle = \frac{\pi}{4} \Omega k_{\text{res}} F(k_{\text{res}})$$

FRACTIONAL POWER $(\delta B/B_0)^2 = G(k_{\text{res}})$

THE DEFLECTION ANGLE CHANGES BY ORDER UNITY IN A TIME:

PATHLENGTH FOR DIFFUSION $\sim VT$

$$\tau \approx \frac{1}{\Omega G(k_{\text{res}})} \longrightarrow \left\langle \frac{\Delta z \Delta z}{\Delta t} \right\rangle \approx v^2 \tau = \frac{v^2}{\Omega G(k_{\text{res}})}$$

SPATIAL DIFFUSION COEFF.

PARTICLE SCATTERING

- EACH TIME THAT A RESONANCE OCCURS THE PARTICLE CHANGES PITCH ANGLE BY $\Delta \theta \sim \delta B/B$ WITH A RANDOM SIGN
- THE RESONANCE OCCURS ONLY FOR RIGHT HAND POLARIZED WAVES IF THE PARTICLES MOVES TO THE RIGHT (AND VICEVERSA)
- THE RESONANCE CONDITION TELLS US THAT 1) IF $k \ll 1/rL$ PARTICLES SURF ADIABATICALLY AND 2) IF $k \gg 1/rL$ PARTICLES HARDLY FEEL THE WAVES

ACCELERATION OF NONTHERMAL PARTICLES

The presence of non-thermal particles is ubiquitous in the Universe (solar wind, Active galaxies, supernova remnants, gamma ray bursts, Pulsars, micro-quasars)

WHEREVER THERE ARE MAGNETIZED PLASMAS THERE ARE NON-THERMAL PARTICLES



PARTICLE ACCELERATION

BUT THERMAL PARTICLES ARE USUALLY DOMINANT, SO WHAT DETERMINES THE DISCRIMINATION BETWEEN THERMAL AND ACCELERATED PARTICLES?

INJECTION

ALL ACCELERATION MECHANISMS ARE ELECTROMAGNETIC
IN NATURE

MAGNETIC FIELD CANNOT MAKE WORK ON CHARGED
PARTICLES THEREFORE ELECTRIC FIELDS ARE NEEDED
FOR ACCELERATION TO OCCUR

REGULAR ACCELERATION
THE ELECTRIC FIELD IS LARGE
SCALE:

$$\langle \vec{E} \rangle \neq 0$$

STOCHASTIC ACCELERATION
THE ELECTRIC FIELD IS SMALL
SCALE:

$$\langle \vec{E} \rangle = 0 \quad \langle \vec{E}^2 \rangle \neq 0$$

STOCHASTIC ACCELERATION

$$\langle \vec{E} \rangle = 0 \quad \langle \vec{E}^2 \rangle \neq 0$$

Most acceleration mechanisms that are operational in astrophysical environments are of this type. We have seen that the action of random magnetic fluctuations is that of scattering particles when the resonance is achieved. In other words, the particle distribution is isotropized in the reference frame of the wave.

Although in the reference frame of the waves the momentum is conserved (B does not make work) in the lab frame the particle momentum changes by

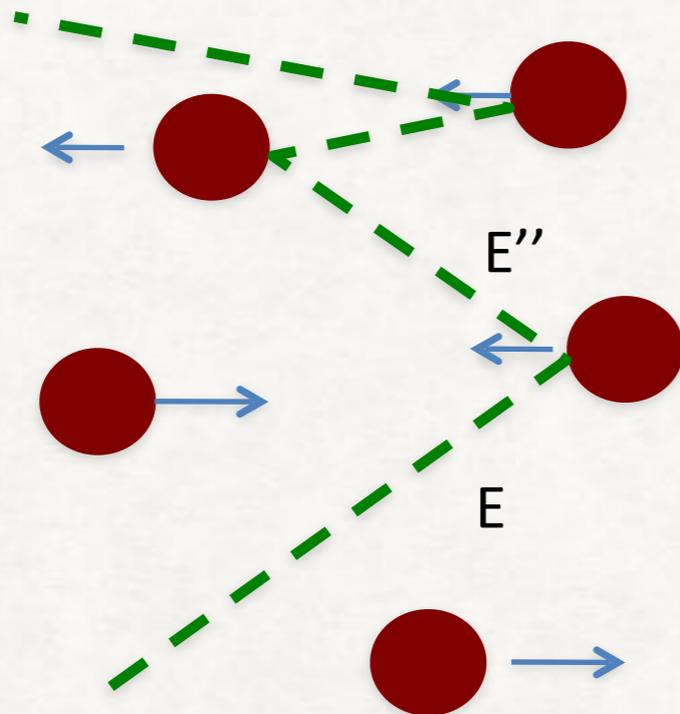
$$\Delta p \sim p \frac{v_A}{c}$$

In a time T which is the diffusion time as found in the last lecture. It follows that

$$D_{pp} = \left\langle \frac{\Delta p \Delta p}{\Delta t} \right\rangle \sim p^2 \frac{1}{T} \left(\frac{v_A}{c} \right)^2 \rightarrow \tau_{pp} = \frac{p^2}{D_{pp}} T \left(\frac{c}{v_A} \right)^2 \gg T$$

THE MOMENTUM CHANGE IS A SECOND ORDER PHENOMENON !!!

SECOND ORDER FERMI ACCELERATION



We inject a particle with energy E . In the reference frame of a cloud moving with speed β the particle energy is:

$$E' = \gamma E + \beta \gamma p \mu$$

and the momentum along x is:

$$p'_x = \beta \gamma E + \gamma p \mu$$

Assuming that the cloud is very massive compared with the particle, we can assume that the cloud is unaffected by the scattering, therefore the particle energy in the cloud frame does not change and the momentum along x is simply inverted, so that after 'scattering' $p'_x \rightarrow -p'_x$. The final energy in the Lab frame is therefore:

$$E'' = \gamma E' + \beta \gamma p'_x =$$

$$\gamma^2 E \left(1 + \beta^2 + 2\beta \mu \frac{p}{E} \right)$$

$$\frac{p}{E} = \frac{mv\gamma}{m\gamma} = v$$

Where v is now the dimensionless particle velocity

It follows that: $E'' = \gamma^2 E (1 + \beta^2 + 2\beta\mu v)$

and: $\frac{E'' - E}{E} = \gamma^2 (1 + 2\beta v\mu + \beta^2) - 1$

and finally, taking the limit of non-relativistic clouds $\gamma \rightarrow 1$:

$$\frac{E'' - E}{E} \approx 2\beta^2 + 2\beta v\mu$$

We can see that the fractional energy change can be both positive or negative, which means that particles can either gain or lose energy, depending on whether the particle-cloud scattering is head-on or tail-on.

We need to calculate the probability that a scattering occurs head-on or Tail-on. The scattering probability along direction μ is proportional to the Relative velocity in that direction:

$$P(\mu) = Av_{rel} = A \frac{\beta\mu + v}{1 + v\beta\mu} \xrightarrow{v \rightarrow 1} \approx A(1 + \beta\mu)$$

The condition of normalization to unity:

$$\int_{-1}^1 P(\mu) d\mu = 1$$

leads to $A=1/2$. It follows that the mean fractional energy change is:

$$\left\langle \frac{\Delta E}{E} \right\rangle = \int_{-1}^1 d\mu P(\mu) (2\beta^2 + 2\beta\mu) = \frac{8}{3} \beta^2$$

NOTE THAT IF WE DID NOT ASSUME RIGID REFLECTION AT EACH CLOUD BUT RATHER ISOTROPIZATION OF THE PITCH ANGLE IN EACH CLOUD, THEN WE WOULD HAVE OBTAINED $(4/3) \beta^2$ INSTEAD OF $(8/3) \beta^2$

THE FRACTIONAL CHANGE IS A SECOND ORDER QUANTITY IN $\beta \ll 1$. This is the reason for the name SECOND ORDER FERMI ACCELERATION

The acceleration process can in fact be shown to become more important in the relativistic regime where $\beta \rightarrow 1$

THE PHYSICAL ESSENCE CONTAINED IN THIS SECOND ORDERDEPENDENCE IS THAT IN EACH PARTICLE-CLOUD SCATTERING THE ENERGY OF THE PARTICLE CAN EITHER INCREASE OR DECREASE \rightarrow WE ARE LOOKING AT A PROCESS OF DIFFUSION IN MOMENTUM SPACE

THE REASON WHY ON AVERAGE THE MEAN ENERGY INCREASES IS THAT HEAD-ON COLLISIONS ARE MORE PROBABLE THAN TAIL-ON COLLISIONS

WHAT IS DOING THE WORK?

We just found that particles propagating in a magnetic field can change their momentum (in modulus and direction)...

BUT MAGNETIC FIELDS CANNOT CHANGE THE MOMENTUM MODULUS... ONLY ELECTRIC FIELDS CAN

WHAT IS THE SOURCE OF THE ELECTRIC FIELDS???

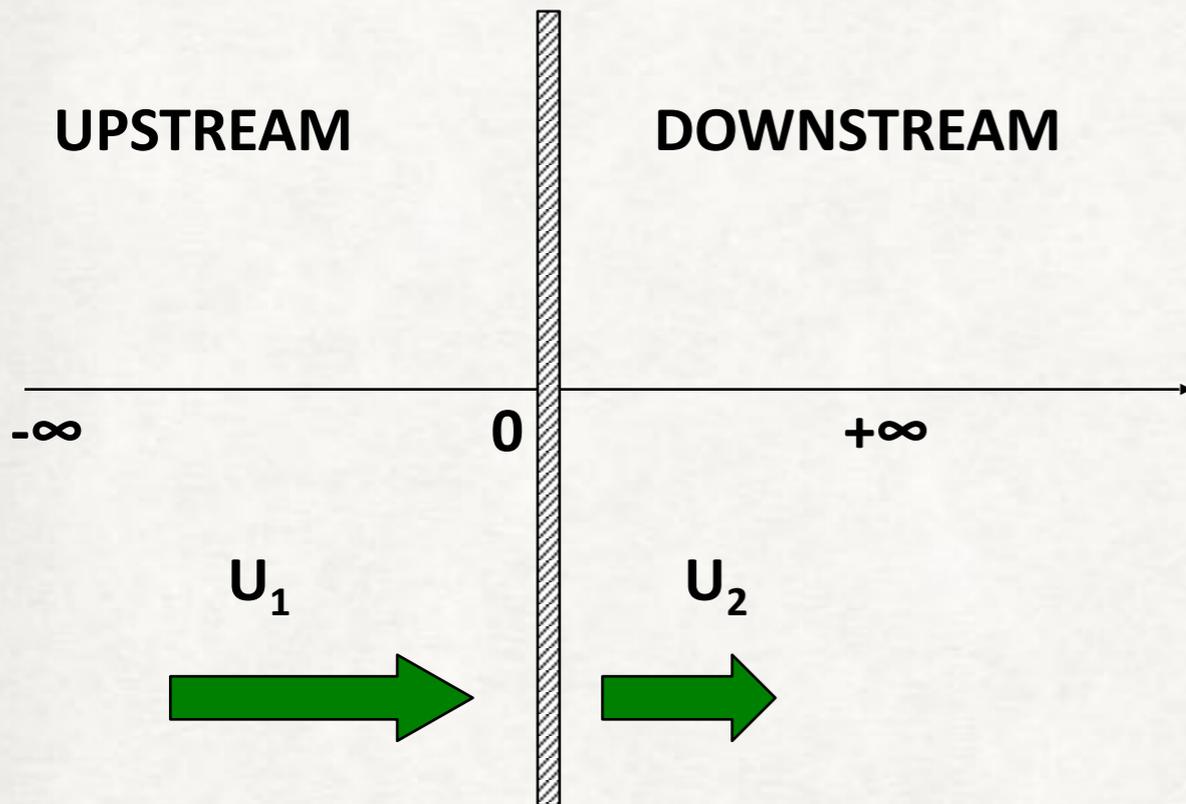
Moving Magnetic Fields

The induced electric field is responsible for this first instance of particle acceleration

The scattering leads to momentum transfer, but to WHAT?

Recall that particles isotropize in the reference frame of the waves...

SHOCK SOLUTIONS



Let us sit in the reference frame in which the shock is at rest and look for stationary solutions

$$\frac{\partial}{\partial x} (\rho u) = 0$$

$$\frac{\partial}{\partial x} (\rho u^2 + P) = 0$$

$$\frac{\partial}{\partial x} \left(\frac{1}{2} \rho u^3 + \frac{\gamma}{\gamma - 1} u P \right) = 0$$

It is easy to show that aside from the trivial solution in which all quantities remain spatially constant, there is a discontinuous solution:

$$\frac{\rho_2}{\rho_1} = \frac{u_1}{u_2} = \frac{(\gamma + 1)M_1^2}{(\gamma - 1)M_1^2 + 2}$$

$$\frac{p_2}{p_1} = \frac{2\gamma M_1^2}{\gamma + 1} - \frac{\gamma - 1}{\gamma + 1}$$

$$\frac{T_2}{T_1} = \frac{[2\gamma M_1^2 - \gamma(\gamma - 1)][(\gamma - 1)M_1^2 + 2]}{(\gamma + 1)^2 M_1^2}$$

M_1 is the upstream
Fluid Mach number

STRONG SHOCKS $M_1 \gg 1$

In the limit of strong shock fronts these expressions get substantially simpler and one has:

$$\frac{\rho_2}{\rho_1} = \frac{u_1}{u_2} = \frac{\gamma + 1}{\gamma - 1}$$

$$\frac{p_2}{p_1} = \frac{2\gamma M_1^2}{\gamma + 1}$$

$$\frac{T_2}{T_1} = \frac{2\gamma(\gamma - 1)}{(\gamma + 1)^2} M_1^2, \quad T_2 = 2 \frac{\gamma - 1}{(\gamma + 1)^2} m u_1^2$$

ONE CAN SEE THAT SHOCKS BEHAVE AS VERY EFFICIENT HEATING MACHINES IN THAT A LARGE FRACTION OF THE INCOMING RAM PRESSURE IS CONVERTED TO INTERNAL ENERGY OF THE GAS BEHIND THE SHOCK FRONT...

COLLISIONLESS SHOCKS

While shocks in the terrestrial environment are mediated by particle-particle collisions, astrophysical shocks are almost always of a different nature. The pathlength for ionized plasmas is of the order of:

$$\lambda \simeq \frac{1}{n\sigma} = 3.2Mpc n_1^{-1} \left(\frac{\sigma}{10^{-25}cm^2} \right)^{-1}$$

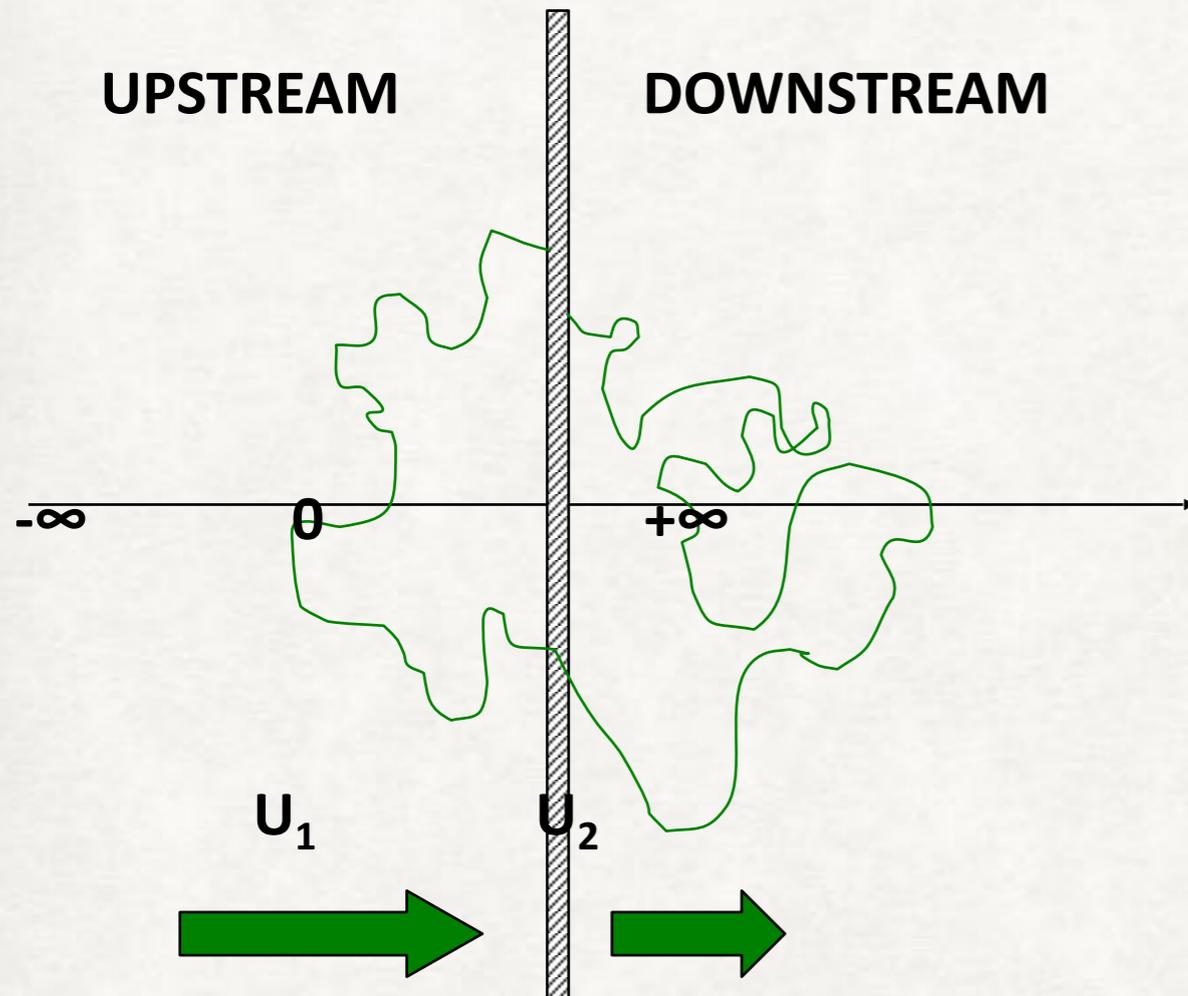
Absurdly large compared with any reasonable length scale. It follows that astrophysical shocks can hardly form because of particle-particle scattering but **REQUIRE** the mediation of magnetic fields. In the downstream gas the Larmor radius of particles is:

$$r_{L,th} \approx 10^{10} B_{\mu} T_8^{1/2} cm$$

The slowing down of the incoming flow and its isotropization (thermalization) is due to the action of magnetic fields in the shock region (**COLLISIONLESS SHOCKS**)

**DIFFUSIVE SHOCK ACCELERATION
OR
FIRST ORDER FERMI ACCELERATION**

BOUNCING BETWEEN APPROACHING MAGNETIC MIRRORS



Let us take a relativistic particle with energy $E \sim p$ upstream of the shock. In the downstream frame:

$$E_d = \gamma E (1 + \beta \mu) \quad 0 \leq \mu \leq 1$$

where $\beta = u_1 - u_2 > 0$. In the downstream frame the direction of motion of the particle is isotropized and reapproaches the shock with the same energy but pitch angle μ'

$$E_u = \gamma E_d - \beta E_d \gamma \mu' = \gamma^2 E (1 + \beta \mu) (1 - \beta \mu')$$

$$-1 \leq \mu' \leq 0$$

In the non-relativistic case the particle distribution is, at zeroth order, isotropic
Therefore:

TOTAL FLUX

$$J = \int_0^1 d\Omega \frac{N}{4\pi} v\mu = \frac{Nv}{4} \quad \longrightarrow \quad P(\mu)d\mu = \frac{ANv\mu}{\frac{Nv}{4}} d\mu = 2\mu d\mu$$

The mean value of the energy change is therefore:

$$\left\langle \frac{E_u - E}{E} \right\rangle = - \int_0^1 d\mu 2\mu \int_{-1}^0 d\mu' 2\mu' [\gamma^2 (1 + \beta\mu)(1 - \beta\mu') - 1] \approx \frac{4}{3}\beta = \frac{4}{3}(u_1 - u_2)$$

A FEW IMPORTANT POINTS:

- I. There are no configurations that lead to losses
- II. The mean energy gain is now first order in β
- III. The energy gain is basically independent of any detail on how particles scatter back and forth!

THE TRANSPORT EQUATION APPROACH

$$\frac{\partial f}{\partial t} = \frac{\partial}{\partial x} \left[D \frac{\partial f}{\partial x} \right] - u \frac{\partial f}{\partial x} + \frac{1}{3} \frac{du}{dx} p \frac{\partial f}{\partial p} + Q(x, p, t)$$

DIFFUSION

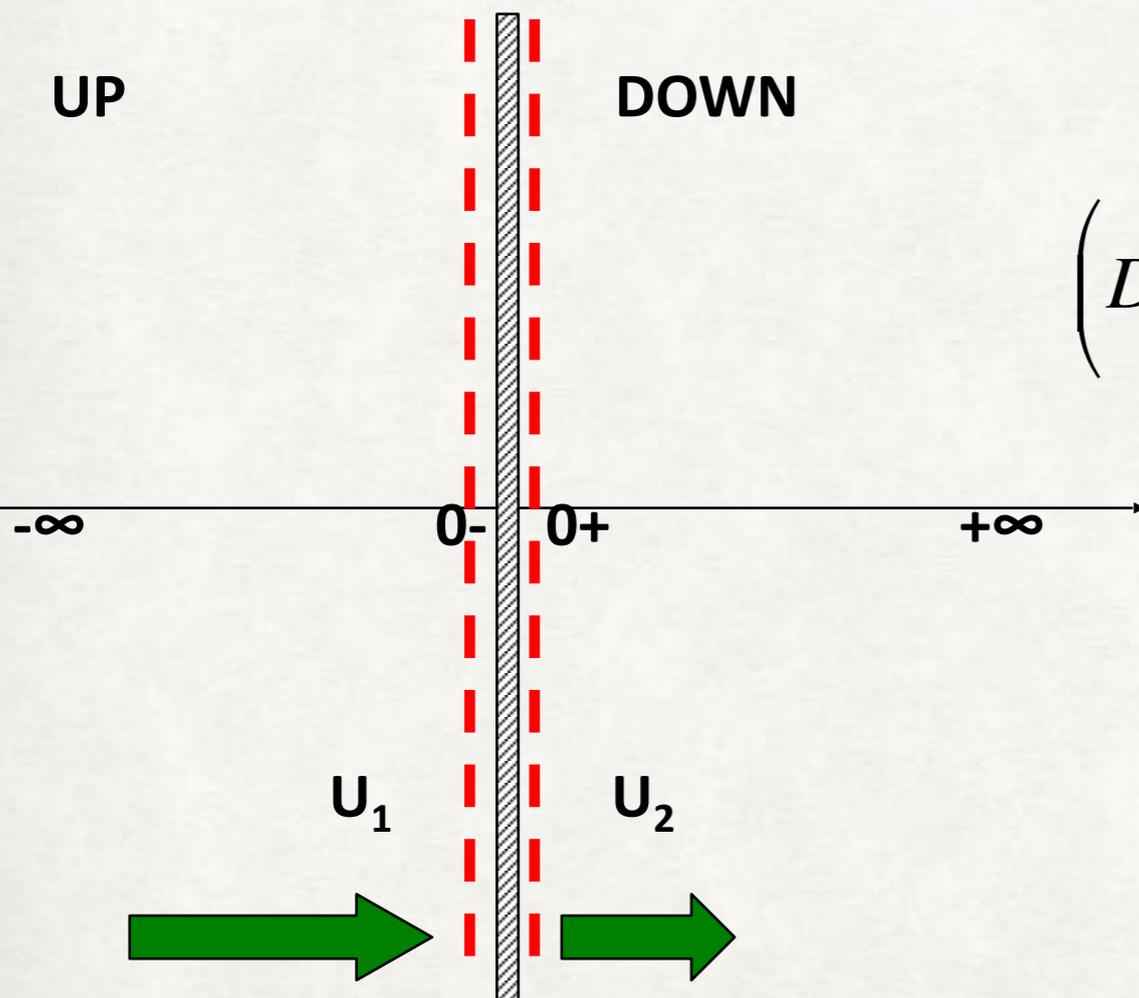
ADVECTION

COMPRESSION

INJECTION

UP

DOWN



Integrating around the shock:

$$\left(D \frac{\partial f}{\partial x} \right)_2 - \left(D \frac{\partial f}{\partial x} \right)_1 + \frac{1}{3} (u_2 - u_1) p \frac{df_0(p)}{dp} + Q_0(p) = 0$$

Integrating from upstr. infinity to 0-:

$$\left(D \frac{\partial f}{\partial x} \right)_1 = u_1 f_0$$

and requiring homogeneity downstream:

$$p \frac{df_0}{dp} = \frac{3}{u_2 - u_1} (u_1 f_0 - Q_0)$$

THE TRANSPORT EQUATION APPROACH

INTEGRATION OF THIS SIMPLE EQUATION GIVES:

$$f_0(p) = \frac{3u_1}{u_1 - u_2} \frac{N_{inj}}{4\pi p_{inj}^2} \left(\frac{p}{p_{inj}} \right)^{\frac{-3u_1}{u_1 - u_2}}$$

DEFINE THE COMPRESSION FACTOR
 $r = u_1/u_2 \rightarrow 4$ (strong shock)

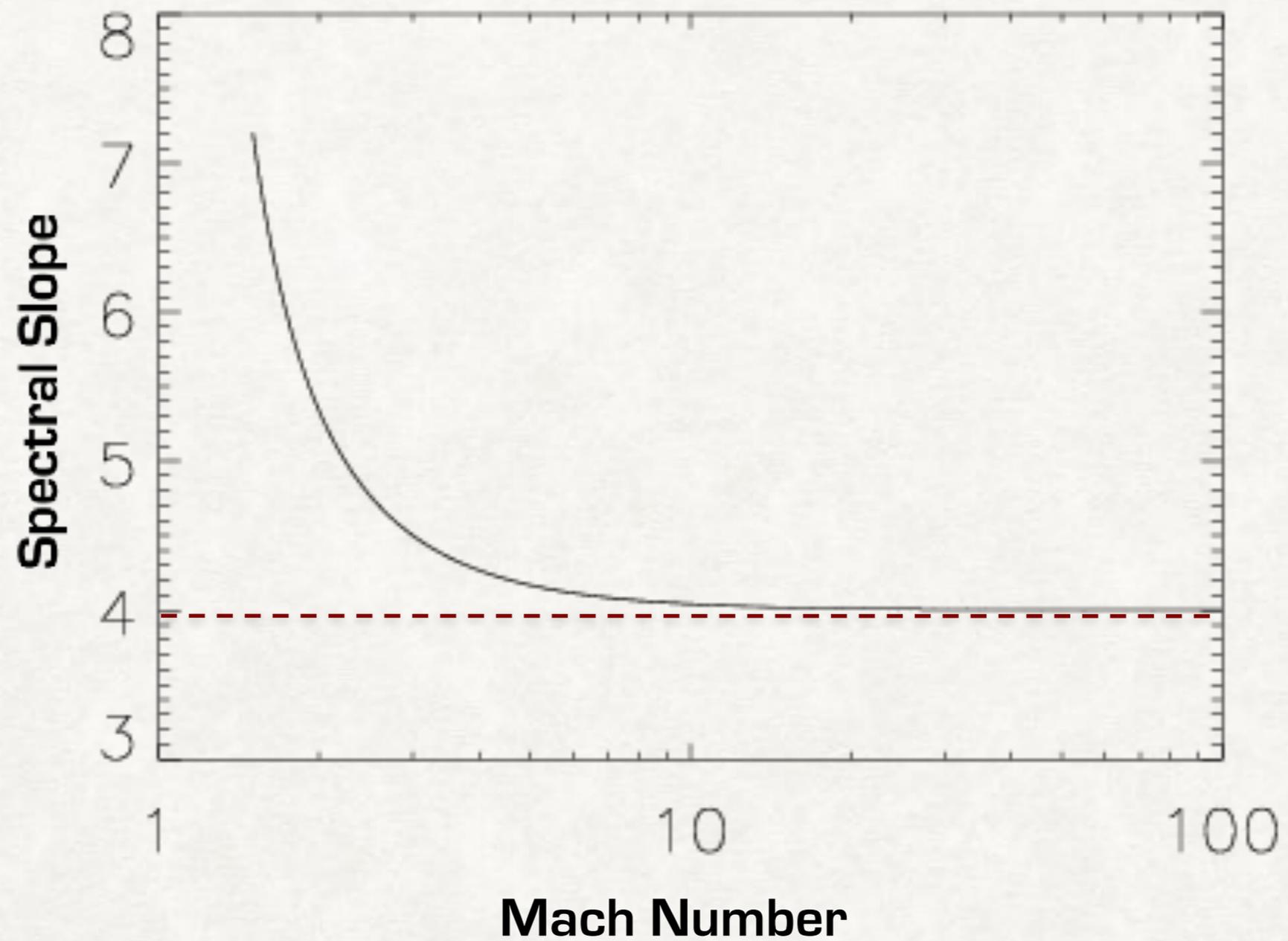
THE SLOPE OF THE SPECTRUM IS

$$\frac{3u_1}{u_1 - u_2} = \frac{3}{1 - 1/r} \rightarrow 4 \quad \text{if } r \rightarrow 4$$

NOTICE THAT: $N(p)dp = 4\pi p^2 f(p)dp \rightarrow N(p) \propto p^{-2}$

1. THE SPECTRUM OF ACCELERATED PARTICLES IS A POWER LAW IN MOMENTUM EXTENDING TO INFINITE MOMENTA
2. THE SLOPE DEPENDS **UNIQUELY ON THE COMPRESSION FACTOR** AND IS INDEPENDENT OF THE DIFFUSION PROPERTIES
3. NO DEPENDENCE UPON DIFFUSION (MICRO-PHYSICS) —- BUT E_{MAX}

TEST PARTICLE SPECTRUM



REACCELERATION VS ACCELERATION

SHOCKS ARE BLIND TO THE NATURE OF THE CHARGED PARTICLES

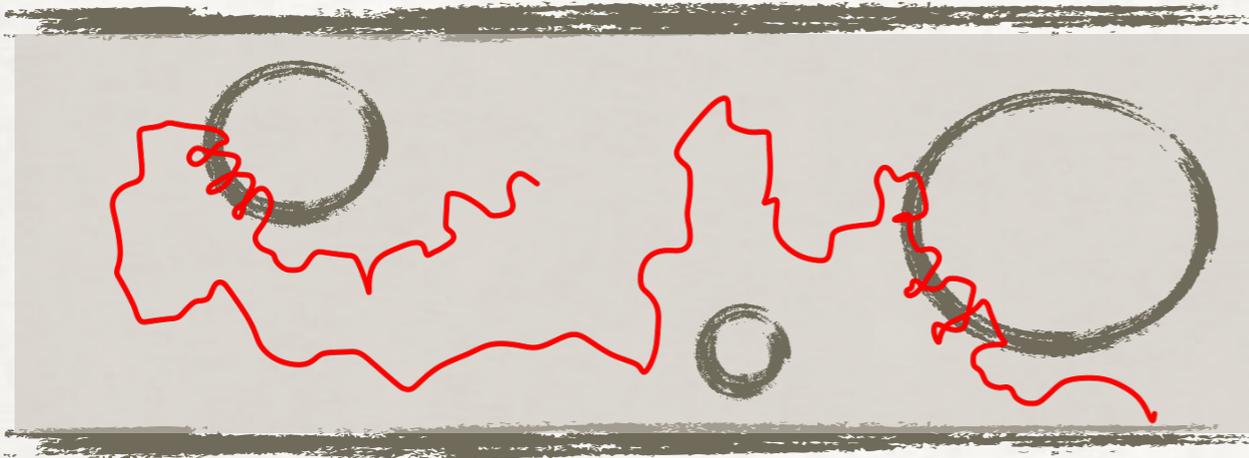
SEED CR ARE ACCELERATED

IF THEIR SPECTRUM IS STEEPER THAN THE ONE THAT IS ASSOCIATED WITH THE SHOCK MACH NUMBER \rightarrow THEIR SPECTRUM GETS HARDER

IF THEIR SPECTRUM IS HARDER THAN THE ONE THAT IS ASSOCIATED WITH THE SHOCK MACH NUMBER \rightarrow THEIR SPECTRUM REMAINS THE SAME

IN BOTH CASES ENERGY IS ADDED BUT THE TOTAL NUMBER OF PARTICLES IS CONSERVED

SHOCK ACCELERATION OF SECONDARY NUCLEI



SECONDARY NUCLEI (AS WELL AS PRIMARY) OCCASIONALLY ENCOUNTER A SN SHOCK AND GET ACCELERATED AT IT — SHOCK IS BLIND TO THE NATURE OF PARTICLES

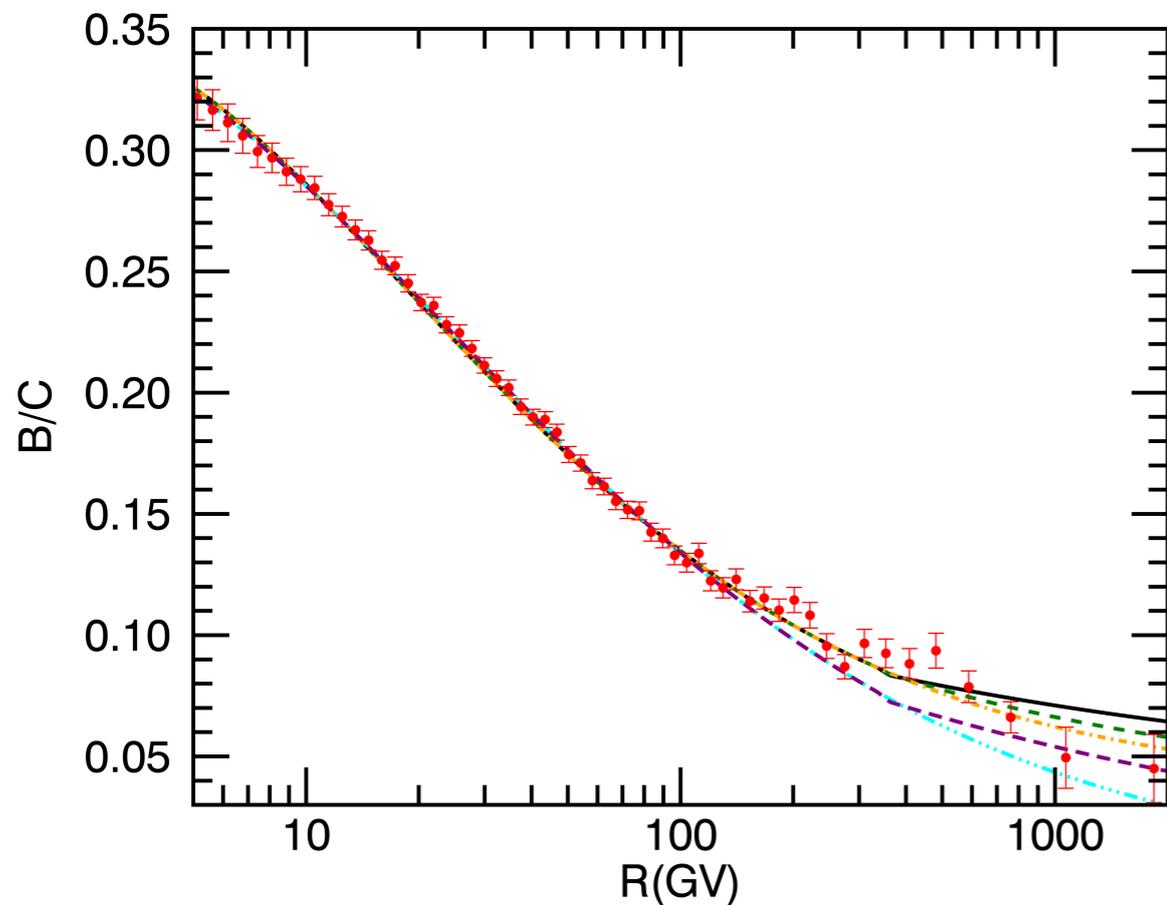
PRIMARY NUCLEI
thermal seeds \rightarrow E- γ

SECONDARY NUCLEI
E- γ - δ \rightarrow E- γ

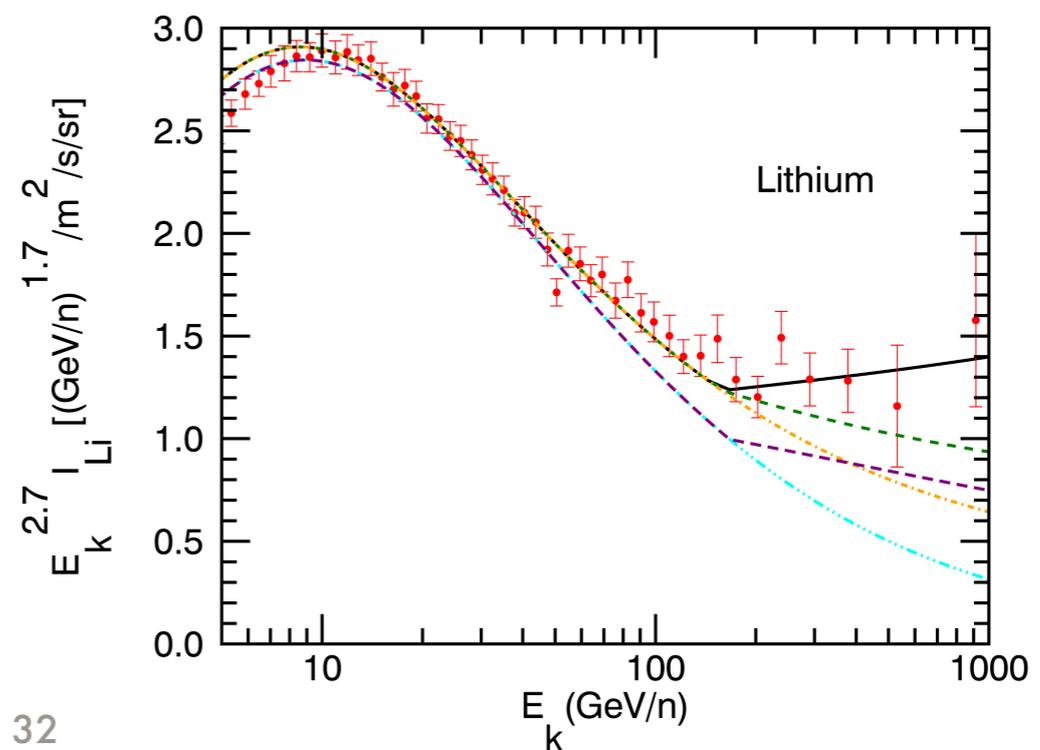
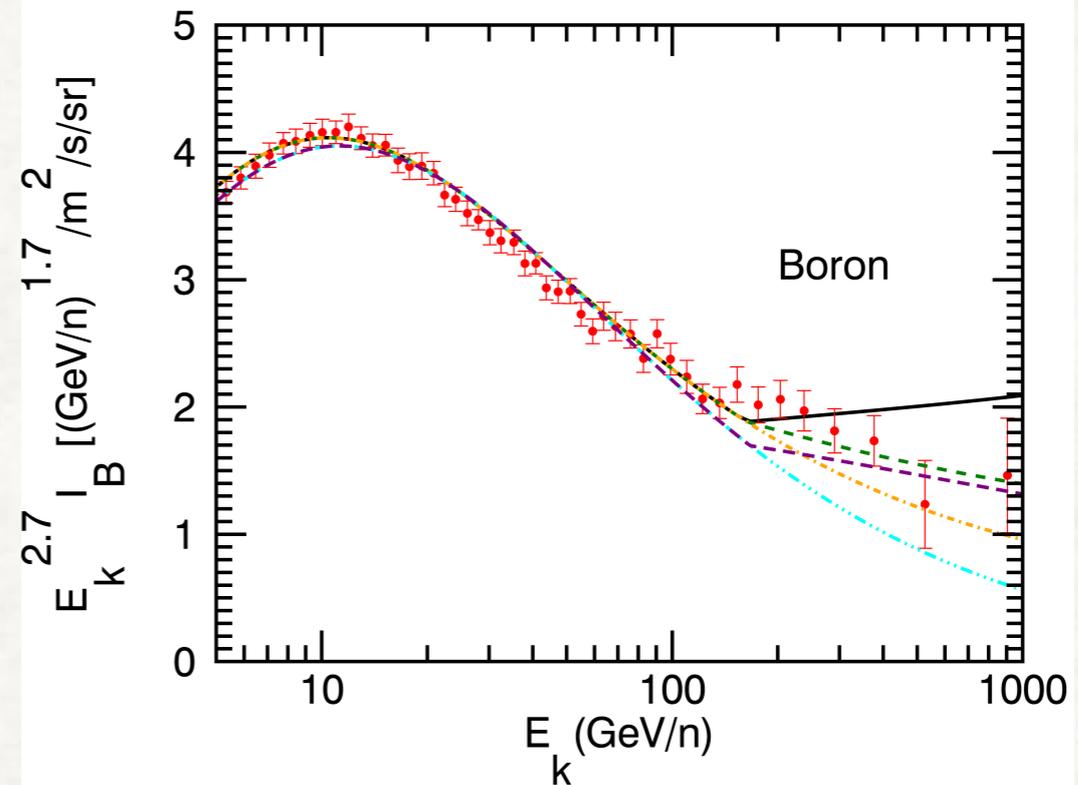
IT IS CLEAR THAT THE OCCASIONAL ACCELERATION OF SECONDARY NUCLEI MUST BE THE MAIN CONTRIBUTION AT SUFFICIENTLY HIGH E, TYPICALLY ABOVE TeV (PB 2017)

SHOCK ACCELERATION OF SECONDARY NUCLEI

PB 2017



CLEARLY NOT AN ATTEMPT TO MAKE A DETAILED PREDICTION, BUT RATHER DISCUSSION OF A NEW EFFECT



SOME IMPORTANT COMMENTS

- **THE STATIONARY PROBLEM DOES NOT ALLOW TO HAVE A MAX MOMENTUM!**
- **THE NORMALIZATION IS ARBITRARY THEREFORE THERE IS NO CONTROL ON THE AMOUNT OF ENERGY IN CR**
- **AND YET IT HAS BEEN OBTAINED IN THE TEST PARTICLE APPROXIMATION**
- **THE SOLUTION DOES NOT DEPEND ON WHAT IS THE MECHANISM THAT CAUSES PARTICLES TO BOUNCE BACK AND FORTH**
- **FOR STRONG SHOCKS THE SPECTRUM IS UNIVERSAL AND CLOSE TO E^{-2}**
- **IT HAS BEEN IMPLICITELY ASSUMED THAT WHATEVER SCATTERS THE PARTICLES IS AT REST (OR SLOW) IN THE FLUID FRAME**

MAXIMUM ENERGY

The maximum energy in an accelerator is determined by either the age of the accelerator compared with the acceleration time or the size of the system compared with the diffusion length $D(E)/u$. The hardest condition is the one that dominates.

Using the diffusion coefficient in the ISM derived from the B/C ratio:

$$D(E) \approx 3 \times 10^{28} E_{GeV}^{1/3} \text{ cm}^2 / \text{s}$$

and the velocity of a SNR shock as $u=5000$ km/s one sees that:

$$t_{acc} \sim D(E)/u^2 \sim 4 \times 10^3 E_{GeV}^{1/3} \text{ years}$$

Too long for any useful acceleration → **NEED FOR ADDITIONAL TURBULENCE**

$$t_{acc}(p) = \langle t \rangle = \frac{3}{u_1 - u_2} \int_{p_0}^p \frac{dp'}{p'} \left[\frac{D_1(p')}{u_1} + \frac{D_2(p')}{u_2} \right]$$

Drury 1983

ENERGY LOSSES AND ELECTRONS

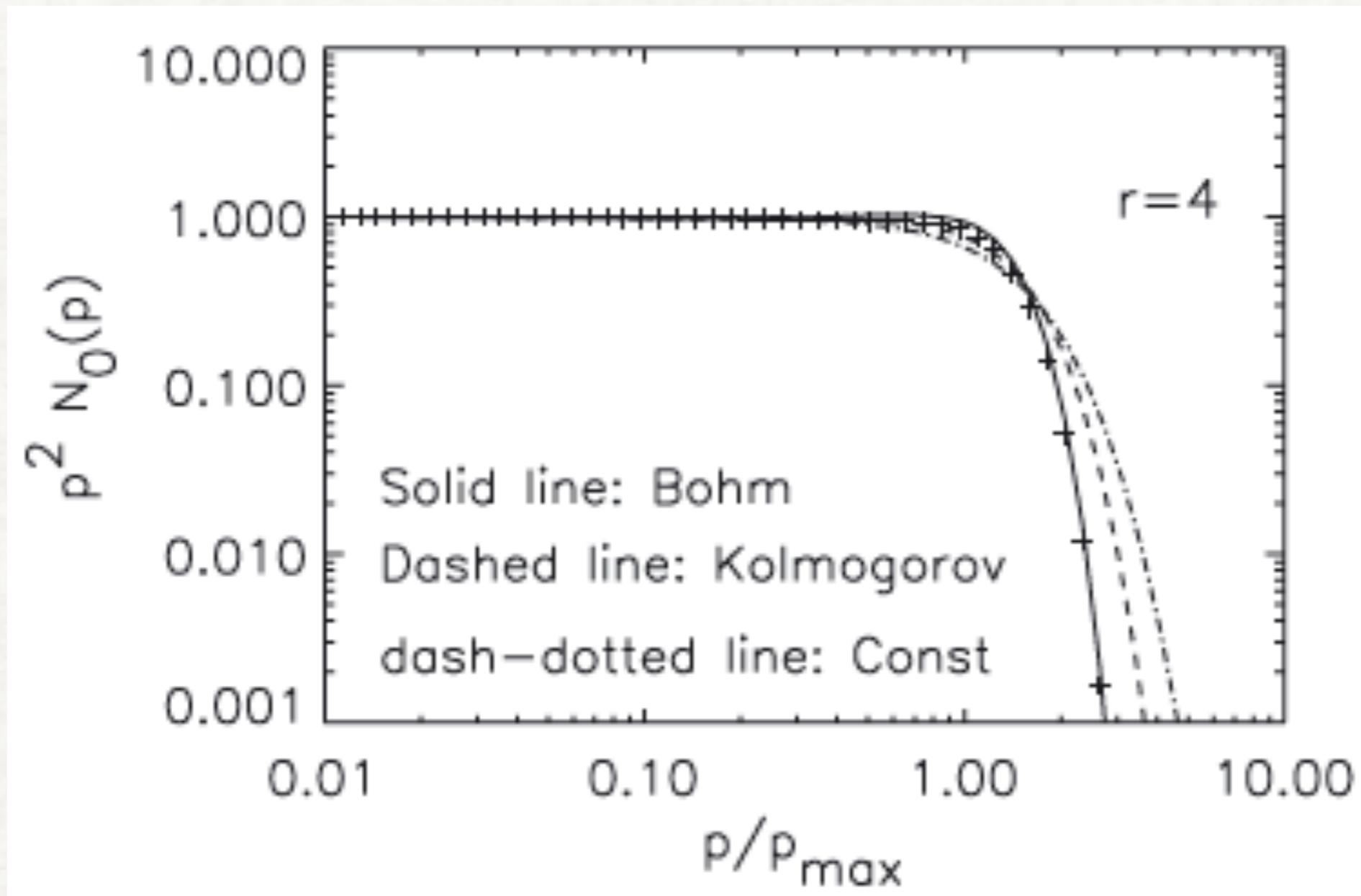
For electrons, energy losses make acceleration even harder.

The maximum energy of electrons is determined by the condition:

$$t_{acc} \leq \text{Min} [Age, \tau_{loss}]$$

Where the losses are mainly due to synchrotron and inverse Compton Scattering.

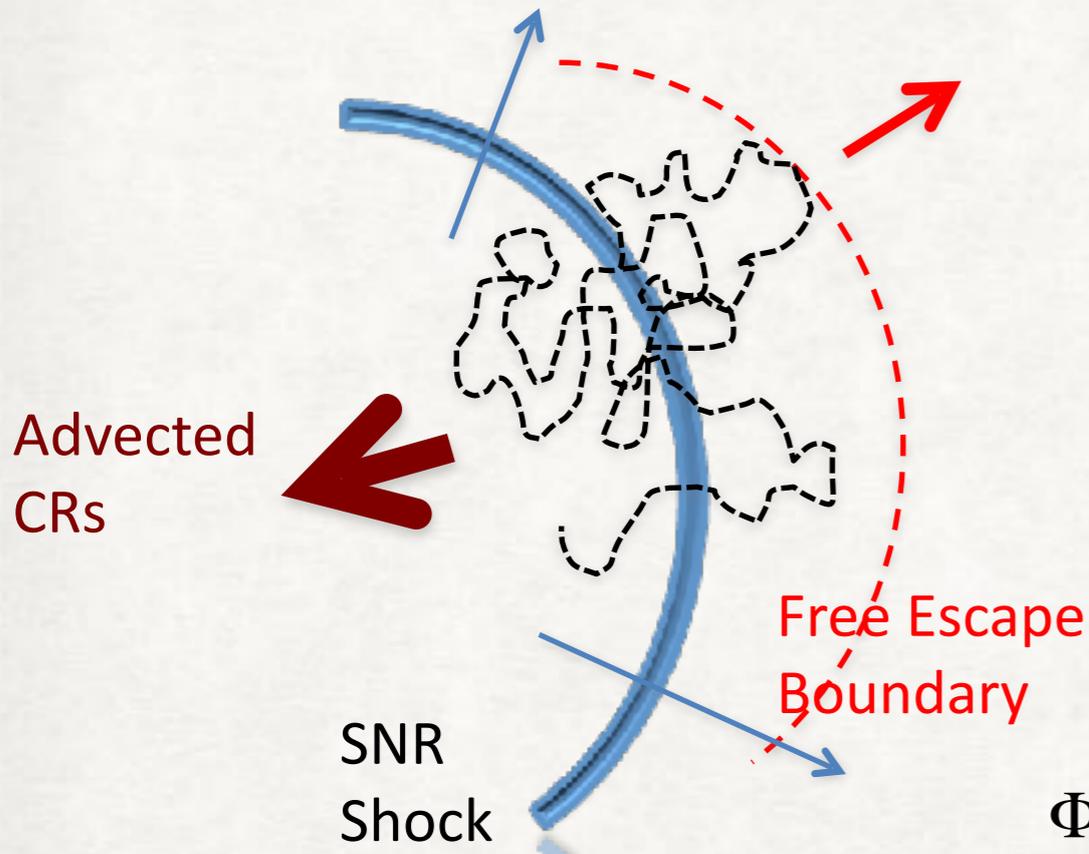
ELECTRONS IN ONE SLIDE



PB 2010

Zirakashvili&Aharonian 2007

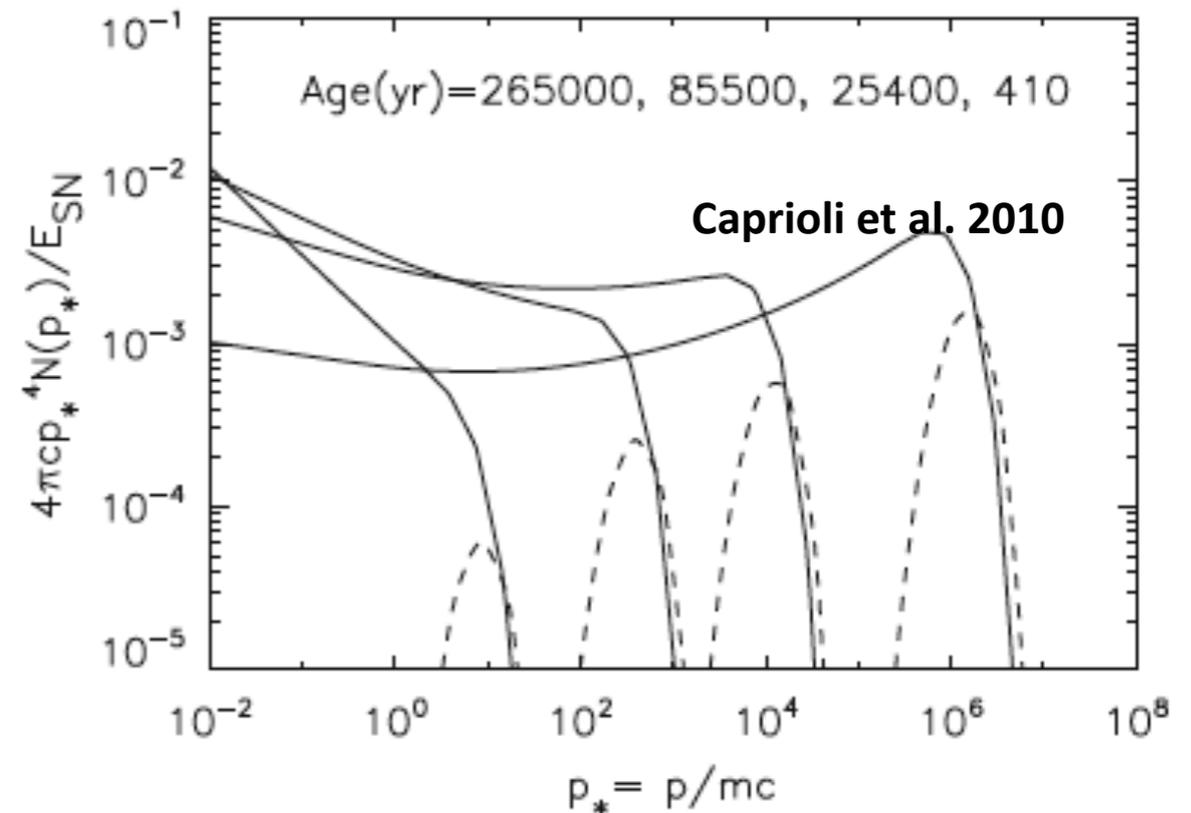
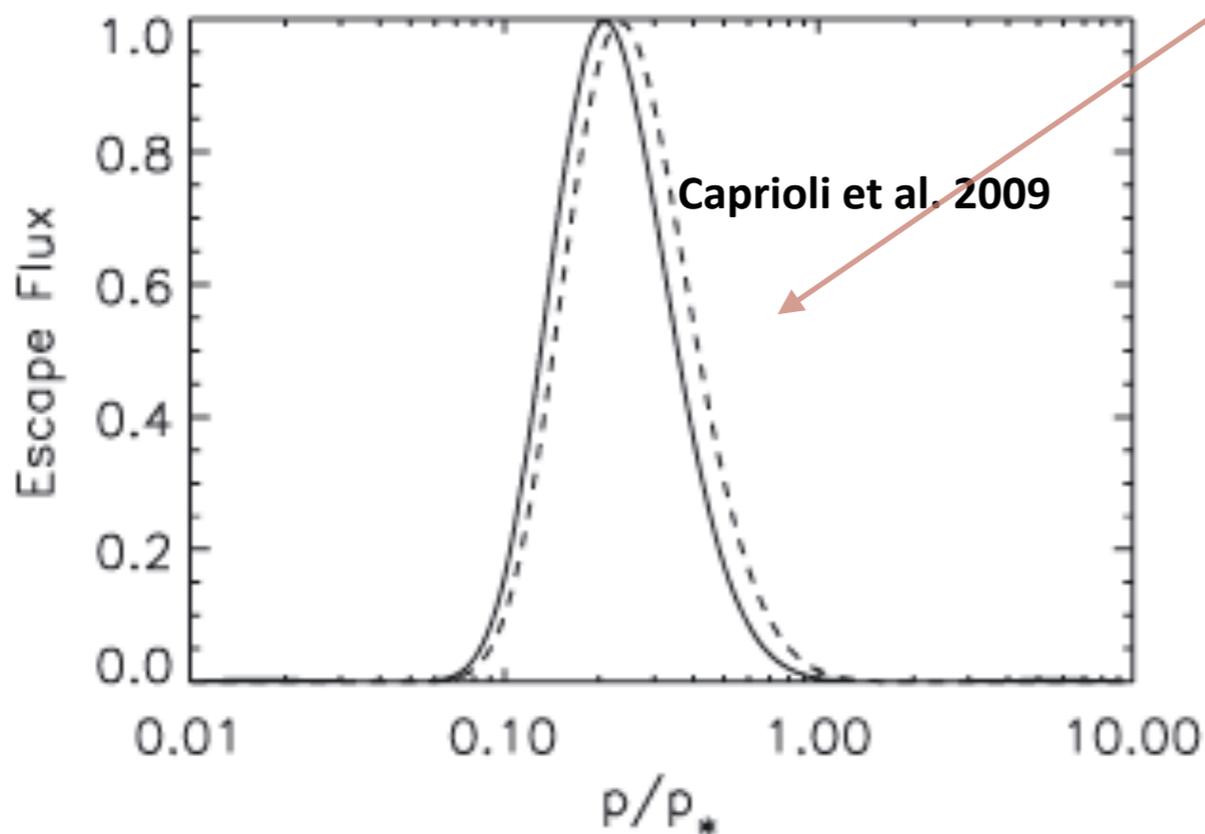
THE PROBLEM OF ESCAPE FROM THE ACCELERATOR



IN STANDARD DSA THERE IS NO ESCAPE FROM UPSTREAM

ESCAPE CAN BE FORCED BY A IMPOSING A FREE ESCAPE BOUNDARY CONDITION

$$\Phi_{esc}(E, x) = D(E) \left(\frac{\partial f(E, x)}{\partial x} \right)_{x=x_{fb}}$$



NON LINEAR THEORY OF DSA

WHY DO WE NEED A NON LINEAR THEORY?

TEST PARTICLE THEORY PREDICTS ENERGY DIVERGENT SPECTRA

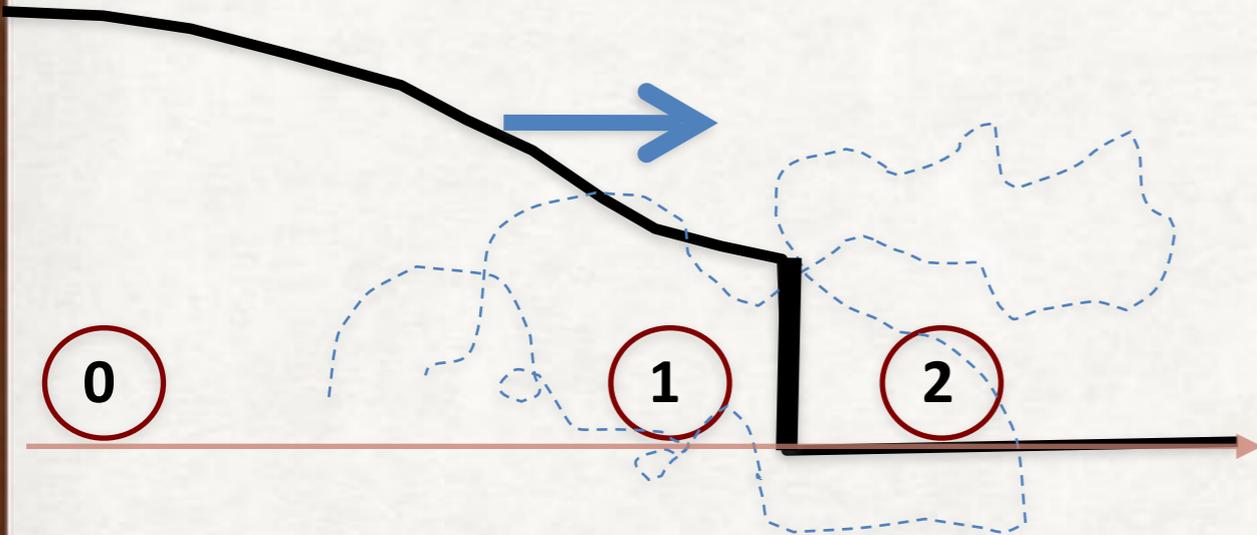
THE TYPICAL EFFICIENCY EXPECTED OF A SNR ($\sim 10\%$) IS SUCH THAT TEST PARTICLE THEORY IS A BAD APPROXIMATION

THE MAX MOMENTUM CAN ONLY BE INTRODUCED BY HAND IN TEST PARTICLE THEORY

SIMPLE ESTIMATES SHOW THAT E_{MAX} IS VERY LOW UNLESS CR TAKE PART IN THE ACCELERATION PROCESS, BY AFFECTING THEIR OWN SCATTERING

DYNAMICAL REACTION OF ACCELERATED PARTICLES

**VELOCITY
PROFILE**



Particle transport is described by using the usual transport equation including diffusion and advection

But now dynamics is important too:

$$\rho_0 u_0 = \rho_1 u_1$$

Conservation of Mass

$$\rho_0 u_0^2 + P_{g,0} = \rho_1 u_1^2 + P_{g,1} + P_{c,1}$$

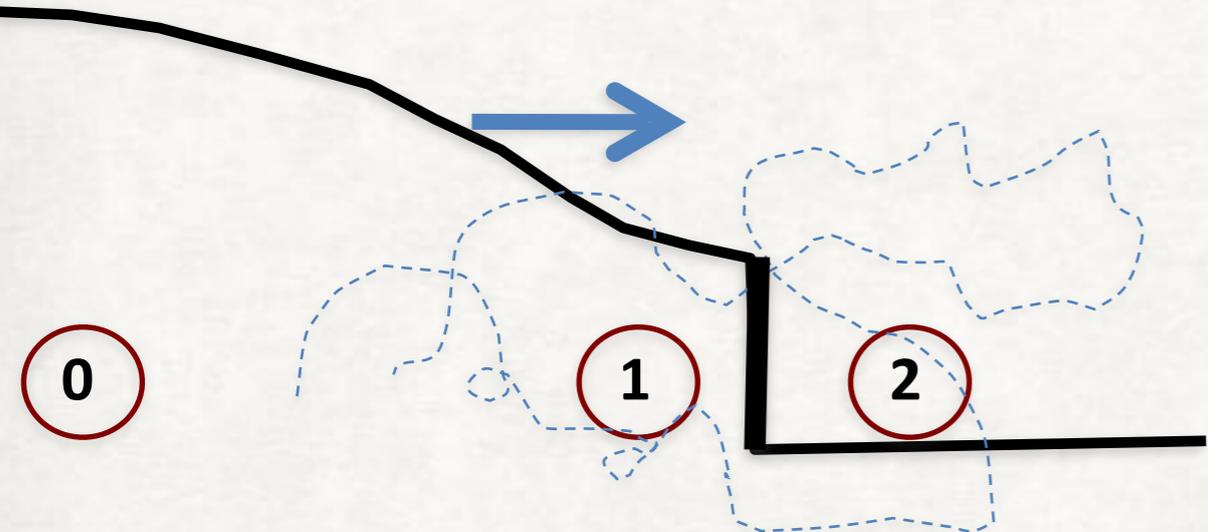
Conservation of Momentum

$$\frac{1}{2} \rho_0 u_0^3 + \frac{P_{g,0} u_0 \gamma_g}{\gamma_g - 1} - F_{esc} = \frac{1}{2} \rho_1 u_1^3 + \frac{P_{g,1} u_1 \gamma_g}{\gamma_g - 1} + \frac{P_{c,1} u_1 \gamma_c}{\gamma_c - 1}$$

Conservation of Energy

FORMATION OF A PRECURSOR - SIMPLIFIED

VELOCITY PROFILE



$$\frac{\partial}{\partial x} [\rho u] = 0 \rightarrow \rho(x)u(x) = \rho_0 u_0$$

$$\frac{\partial}{\partial x} [P_g + \rho u^2 + P_{CR}] = 0$$



$$P_g(x) + \rho u^2 + P_{CR} = P_{g,0} + \rho_0 u_0^2$$

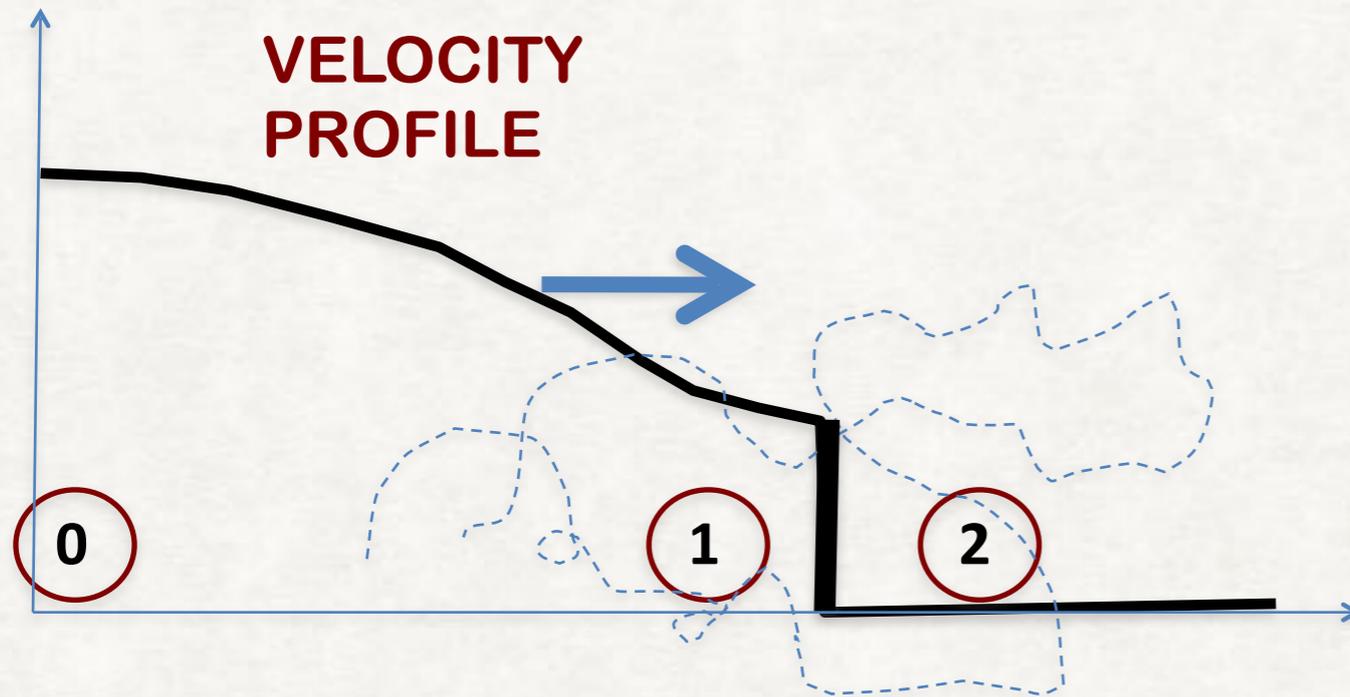
AND DIVIDING BY THE RAM PRESSURE AT UPSTREAM INFINITY:

$$\frac{P_g}{\rho_0 u_0^2} + \frac{u}{u_0} + \frac{P_{CR}}{\rho_0 u_0^2} = \frac{P_{g,0}}{\rho_0 u_0^2} + 1 \rightarrow \frac{u}{u_0} \approx 1 - \xi_{CR}(x)$$

WHERE WE NEGLECTED TERMS OF ORDER $1/M^2$

$$\xi_{CR}(x) = \frac{P_{CR}(x)}{\rho_0 u_0^2}$$

BASIC PREDICTIONS OF NON LINEAR THEORY



COMPRESSION FACTOR BECOMES
FUNCTION OF ENERGY

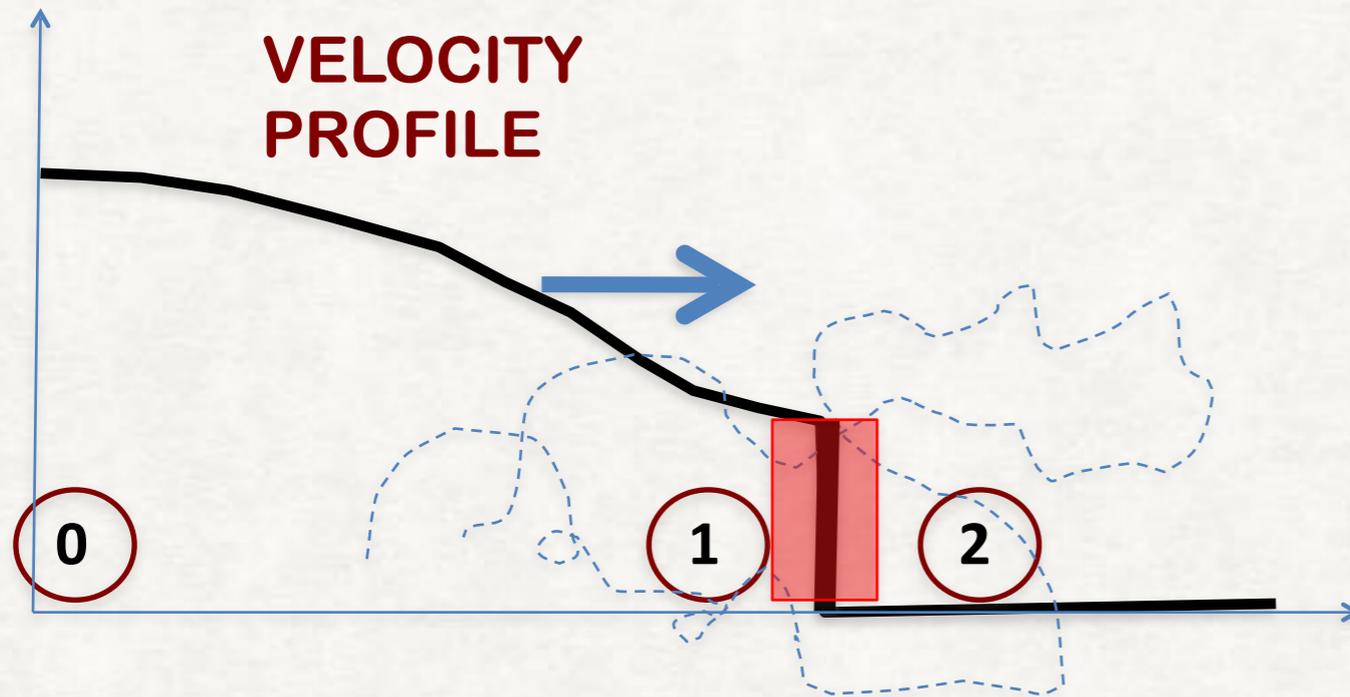
SPECTRA ARE NOT PERFECT
POWER LAWS (CONCAVE)

GAS BEHIND THE SHOCK IS
COOLER FOR EFFICIENT SHOCK
ACCELERATION

SYSTEM SELF REGULATED

EFFICIENT GROWTH OF B-FIELD IF
ACCELERATION EFFICIENT

BASIC PREDICTIONS OF NON LINEAR THEORY



COMPRESSION FACTOR BECOMES
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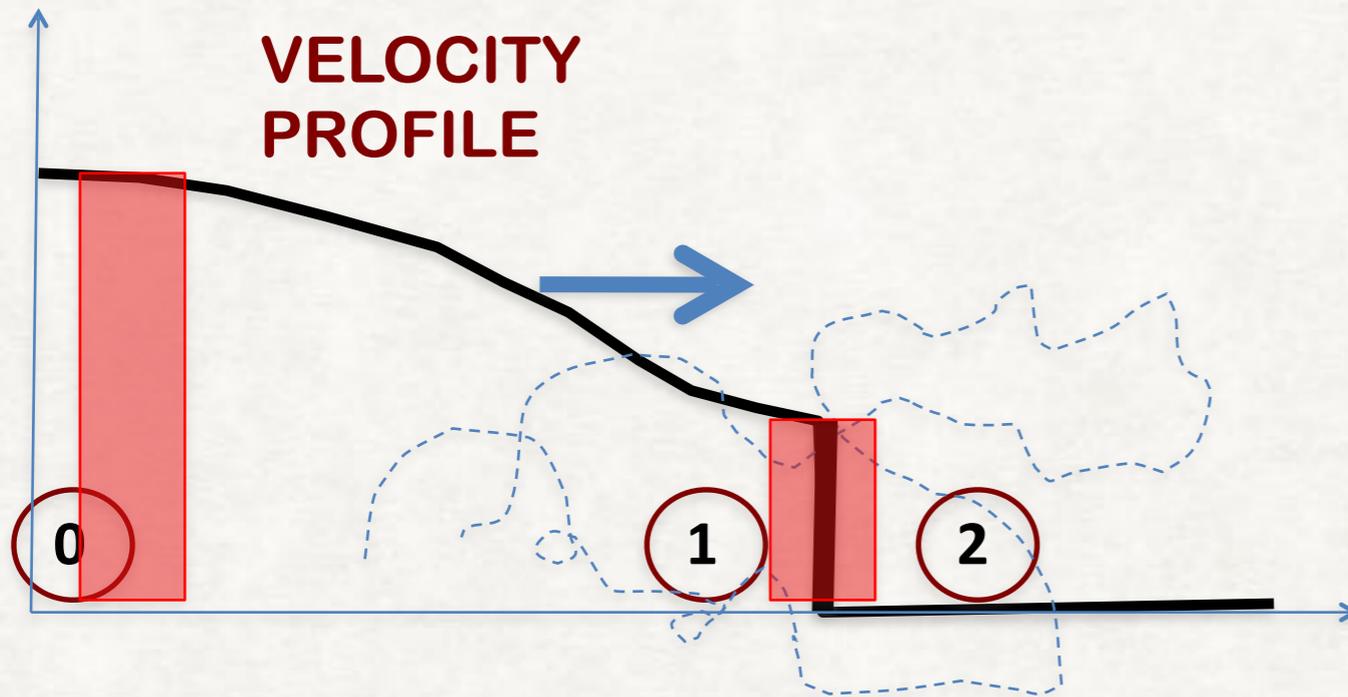
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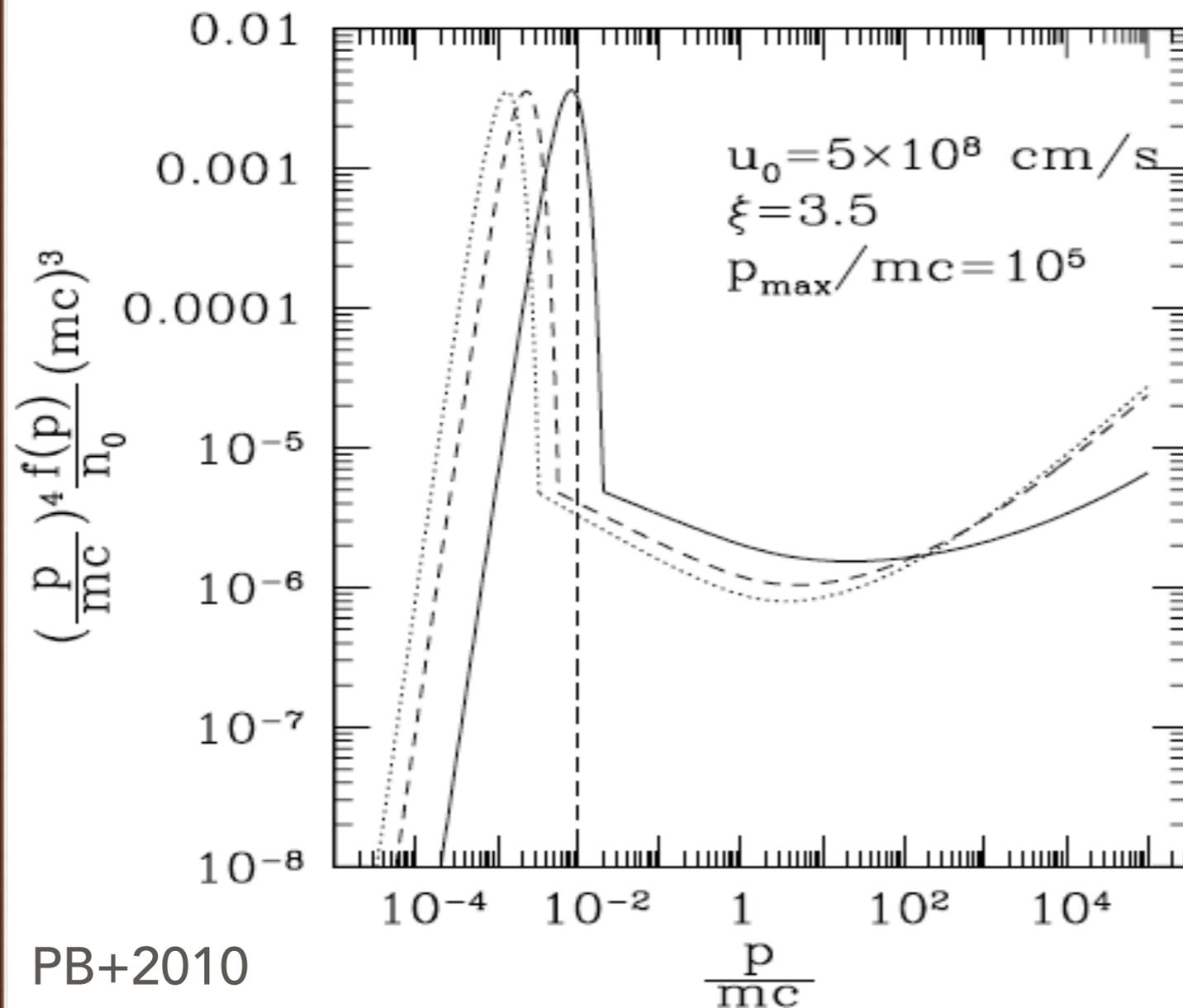
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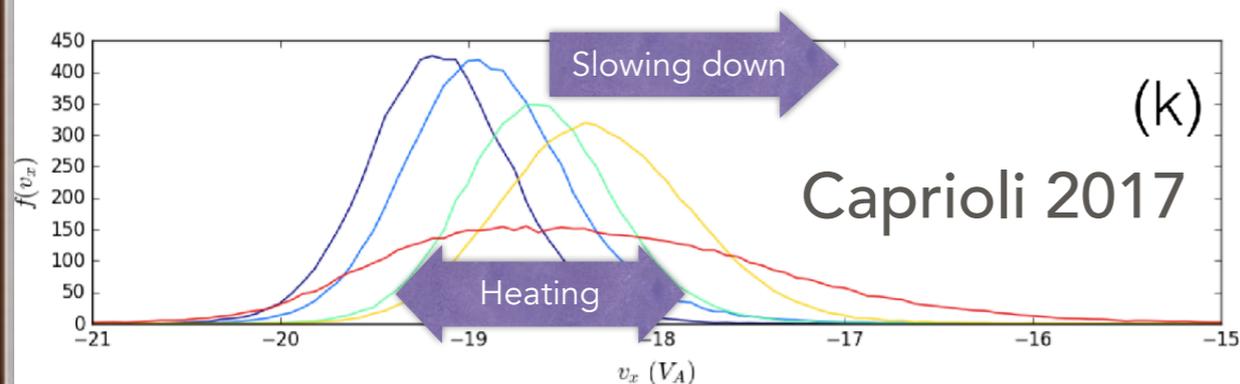
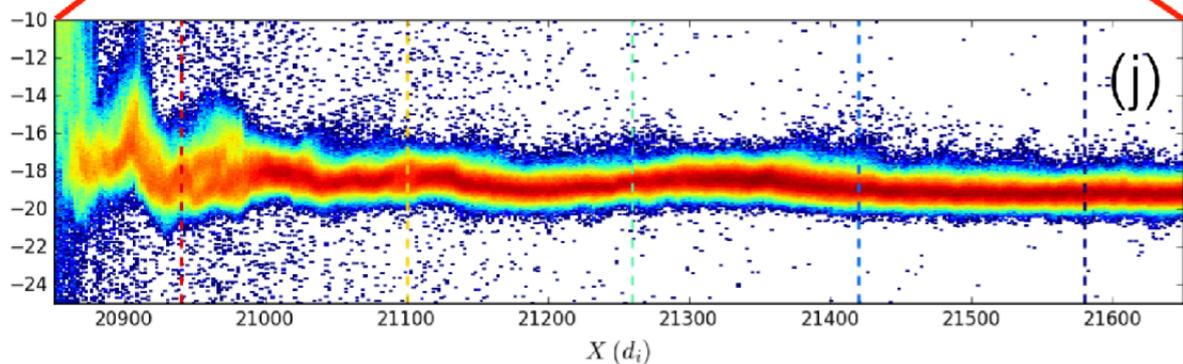
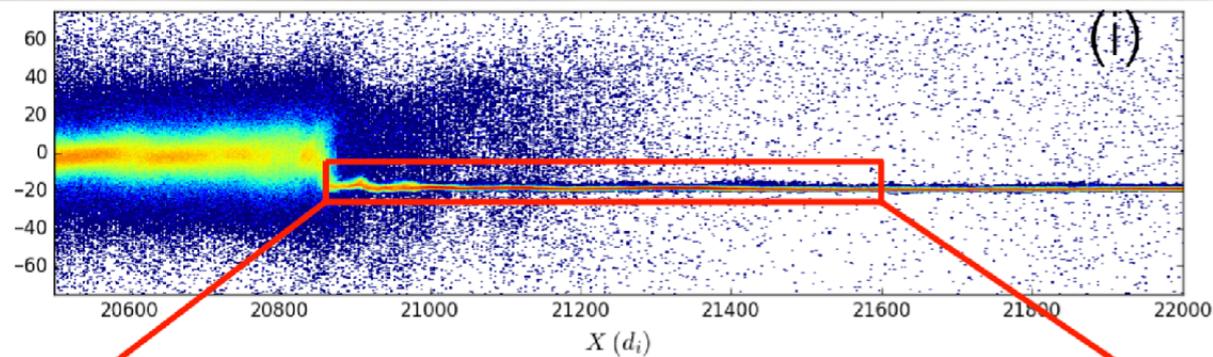
SYSTEM SELF REGULATED

EFFICIENT GROWTH OF B-FIELD IF ACCELERATION EFFICIENT

EFFECT OF TURBULENT DAMPING

AT LEAST A FRACTION OF THE ENERGY OF CR UPSTREAM IS TRANSFERRED TO THE THERMAL ENERGY OF THE BACKGROUND PLASMA

THIS PROCESS (TURBULENT HEATING) LEADS TO A REDUCTION OF THE MACH NUMBER IN THE PRECURSOR \rightarrow SMOOTHER PRECURSOR \rightarrow SPECTRA AGAIN CLOSE TO E^{-2}

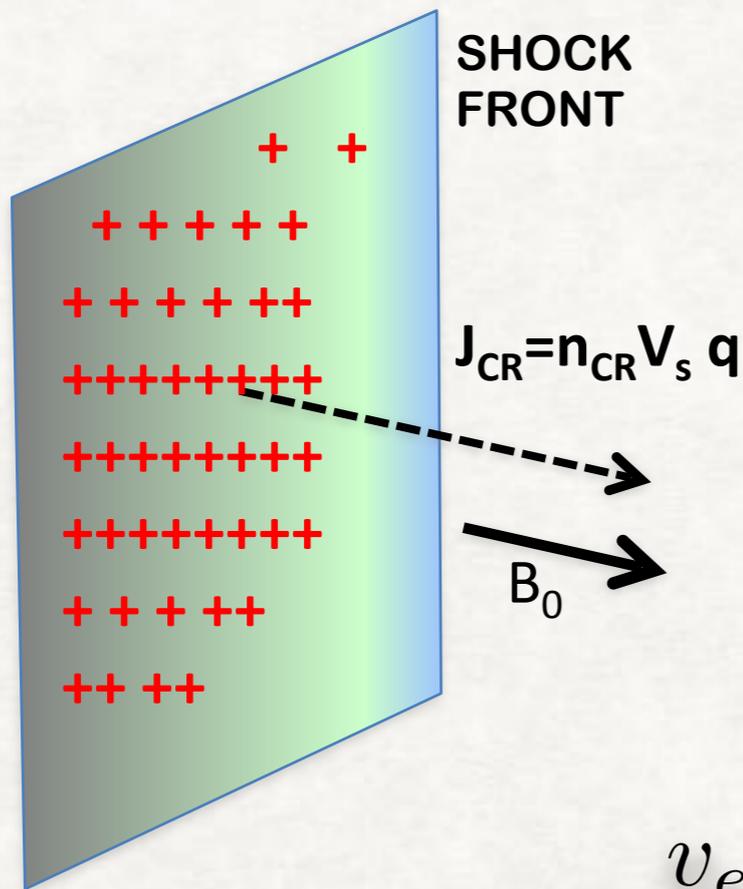


HYBRID SIMS SHOW THIS EFFECT IN THE FORM OF A SLOWING DOWN OF THE PLASMA AND HEATING

YET NO APPRECIABLE DEVIATION FROM E^{-2}

HOWEVER THESE SIMULATIONS ARE NON RELATIVISTIC

BASICS OF CR STREAMING INSTABILITY



THE UPSTREAM PLASMA REACTS TO THE UPCOMING CR CURRENT BY CREATING A RETURN CURRENT TO COMPENSATE THE POSITIVE CR CHARGE

THE SMALL INDUCED PERTURBATIONS MAY BE **UNSTABLE** (ACHTERBERG 1983, ZWEIBEL 1978, BELL 1978, BELL 2004, AMATO & PB 2009)

$$n_p + n_{CR} = n_e$$

$$n_{CR} v_{shock} = n_e v_e$$

$$v_e = \frac{n_{CR}}{n_{CR} + n_p} v_{shock} \approx v_{shock} \frac{n_{CR}}{n_p}$$

CR MOVE WITH THE SHOCK SPEED ($\gg v_A$). THIS UNSTABLE SITUATION LEADS THE PLASMA TO REACT IN ORDER TO SLOW DOWN CR TO $< v_A$ BY SCATTERING PARTICLES IN THE PERP DIRECTION (B-FIELD GROWTH)

STREAMING INSTABILITY - THE SIMPLE VIEW

CR streaming with the shock leads to growth of waves. The general idea is simple to explain:

$$n_{CR} m v_D \rightarrow n_{CR} m V_A \Rightarrow \frac{dP_{CR}}{dt} = \frac{n_{CR} m (v_D - V_A)}{\tau} \qquad \frac{dP_w}{dt} = \gamma_w \frac{\delta B^2}{8\pi} \frac{1}{V_A}$$

and assuming equilibrium:

$$\gamma_w = \sqrt{2} \frac{n_{CR}}{n_{gas}} \frac{v_D - V_A}{V_A} \Omega_{cyc}$$

And for parameters typical of SNR shocks:

$$\gamma_w \simeq \sqrt{2} \xi_{CR} \left(\frac{V_s}{c} \right)^2 \frac{V_s}{V_A} \Omega_{cyc} \sim \mathcal{O}(10^{-4} \text{ seconds}^{-1})$$

BRANCHES OF THE CR INDUCED STREAMING INSTABILITY

A CAREFUL ANALYSIS OF THE INSTABILITY REVEALS THAT THERE ARE TWO BRANCHES

RESONANT

MAX GROWTH AT
 $k=1/\text{LARMOR}$

NON RESONANT

MAX GROWTH AT
 $k \gg 1/\text{LARMOR}$

THE MAX GROWTH CAN ALWAYS BE WRITTEN IN THE FORM

$$\gamma_{max} = k_{max} v_A$$

WHERE THE WAVENUMBER IS DETERMINED BY THE TENSION CONDITION:

$$k_{max} B_0 \approx \frac{4\pi}{c} J_{CR} \rightarrow k_{max} \approx \frac{4\pi}{c B_0} J_{CR}$$

THE SEPARATION BETWEEN THE TWO REGIMES IS AT $k_{\text{MAX}} r_L = 1$

IF WE WRITE THE CR CURRENT AS $J_{CR} = n_{CR}(> E) e v_D$

WHERE E IS THE ENERGY OF THE PARTICLES DOMINATING THE CR CURRENT, WE CAN WRITE THE CONDITION ABOVE AS

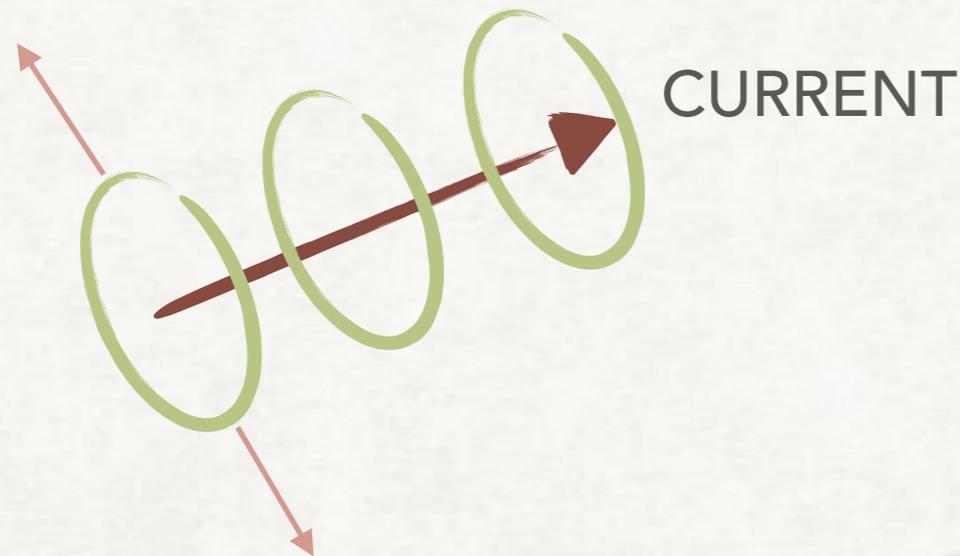
$$\frac{U_{CR}}{U_B} = \frac{c}{v_D}$$

$$U_{CR} = n_{CR}(> E) E \quad U_B = \frac{B^2}{4\pi}$$

IN CASE OF SHOCKS $v_D = \text{SHOCK VELOCITY}$ AND THE CONDITION SAYS THAT THE NON-RESONANT MODES DOMINATED WHEN THE SHOCK IS VERY FAST AND ACCELERATION IS EFFICIENT — FOR TYPICAL CASES THIS IS ALWAYS THE CASE

BUT RECALL! THE WAVES THAT GROW HAVE k MUCH LARGER THAN THE LARMOR RADIUS OF THE PARTICLES IN THE CURRENT —> NO SCATTERING BECAUSE EFFICIENT SCATTERING REQUIRES RESONANCE!!!

THE EASY WAY TO SATURATION OF GROWTH



The current exerts a force on the background plasma

$$\rho \frac{dv}{dt} \sim \frac{1}{c} J_{CR} \delta B$$

which translates into a plasma displacement:

$$\Delta x \sim \frac{J_{CR}}{c\rho} \frac{\delta B(0)}{\gamma_{max}^2} \exp(\gamma_{max} t)$$

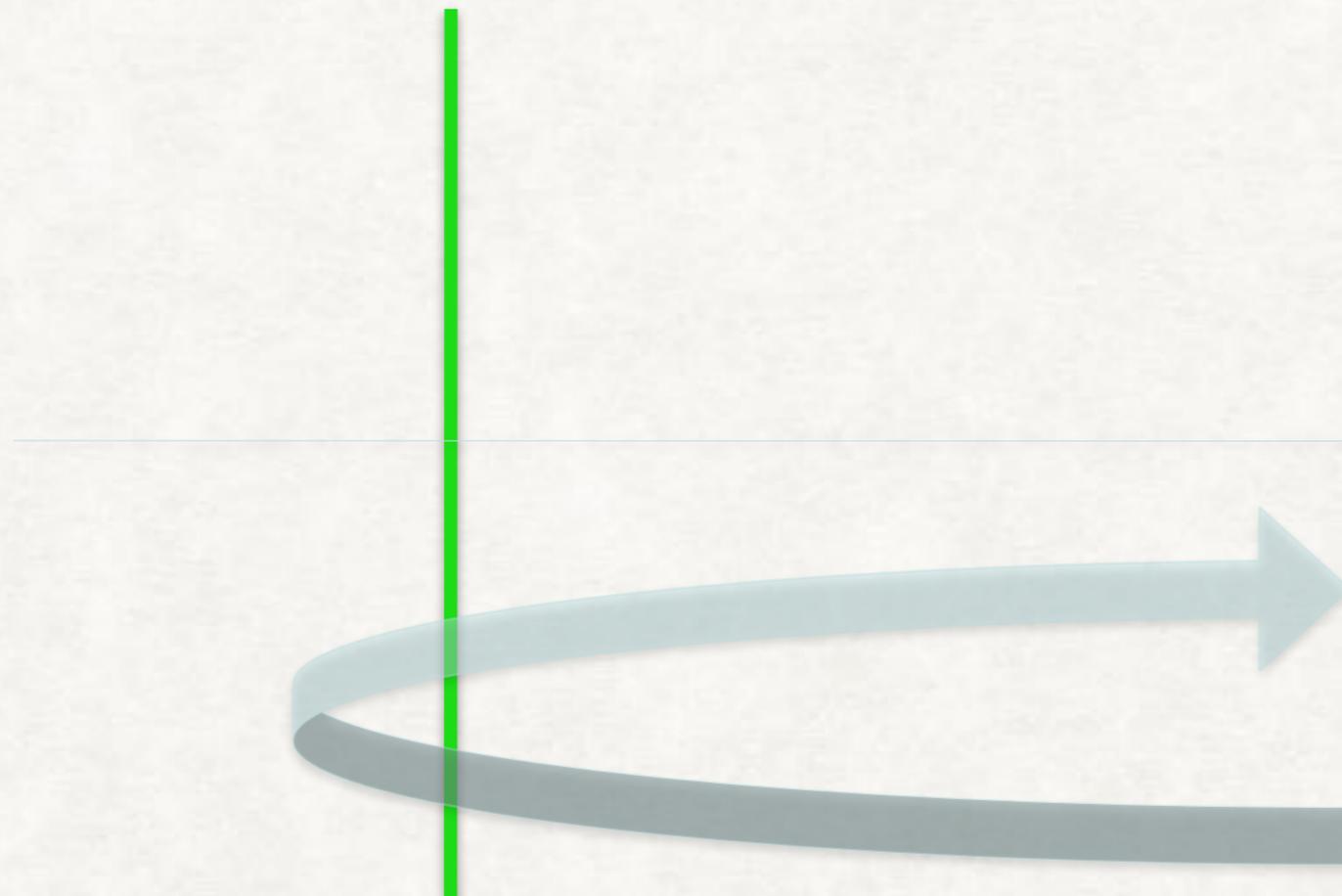
which stretches the magnetic field line by the same amount...

The saturation takes place when the displacement equals the Larmor radius of the particles in the field δB ... imposing this condition leads to:

$$\frac{\delta B^2}{4\pi} = \frac{\xi_{CR}}{\Lambda} \rho v_s^2 \frac{v_s}{c} \quad \Lambda = \ln(E_{max}/E_{min})$$

specialized to a strong shock and a spectrum E^{-2}

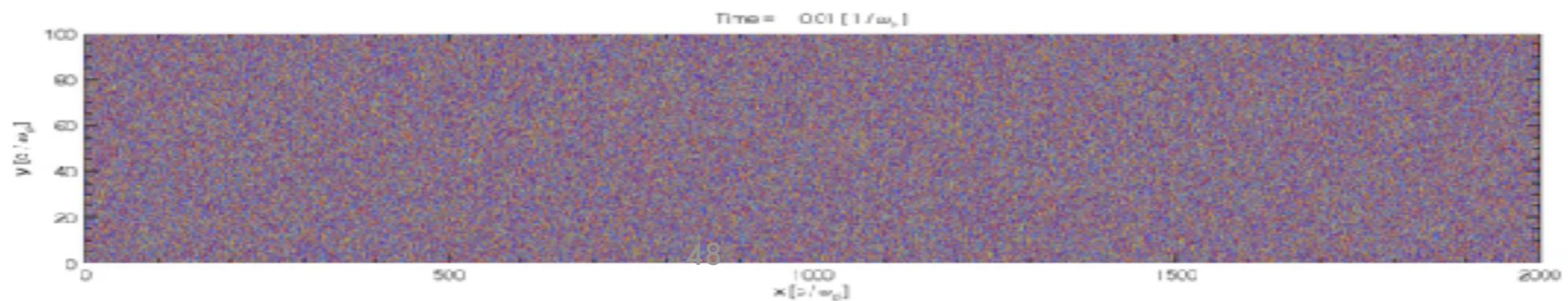
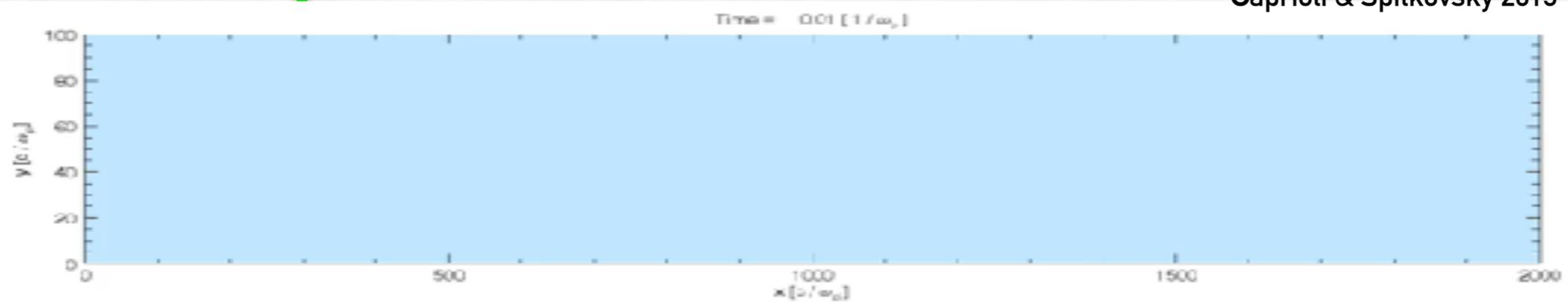
A QUALITATIVE PICTURE OF ACCELERATION



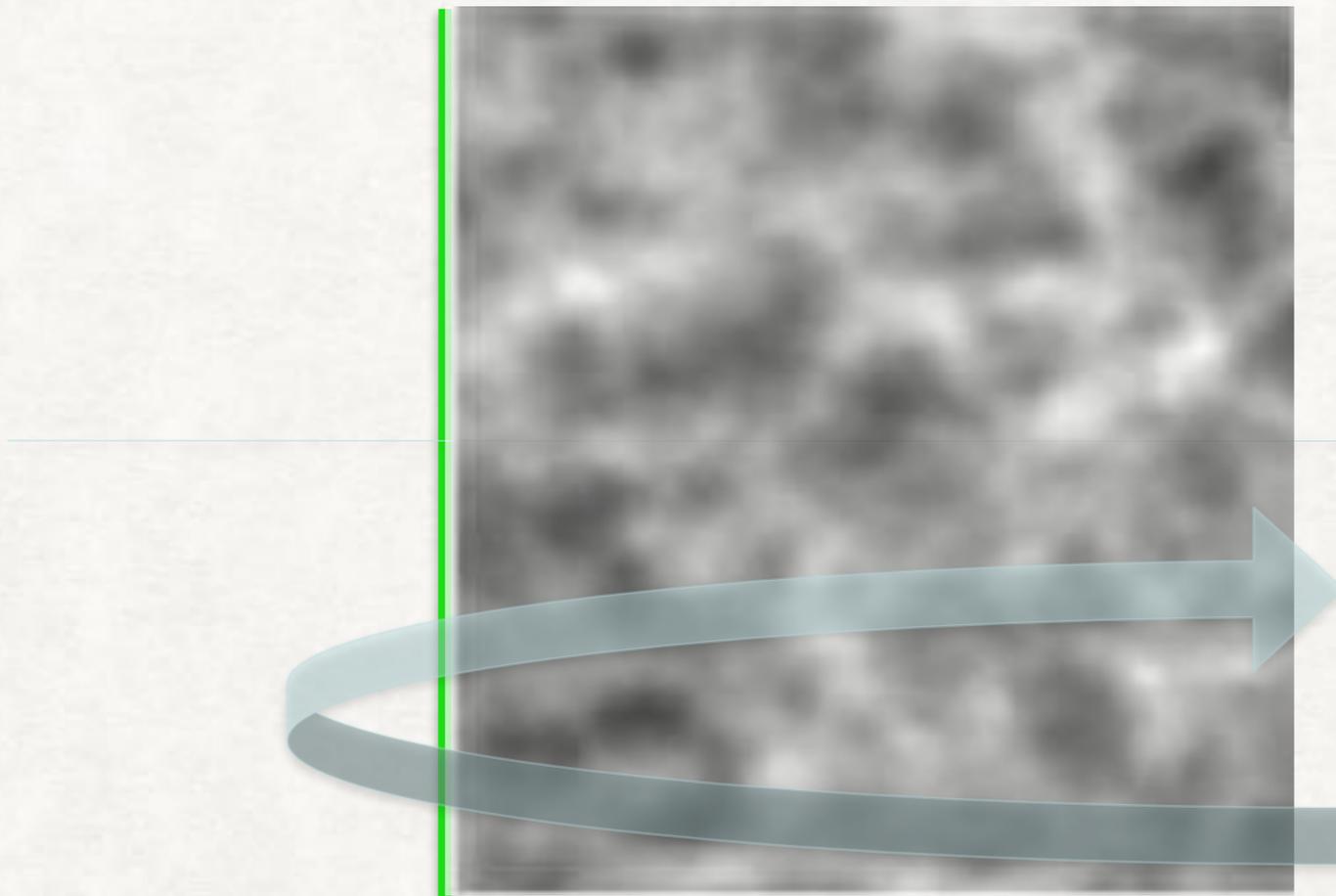
Bell & Schure 2013

Cardillo, Amato & PB 2015

Caprioli & Spitkovsky 2013

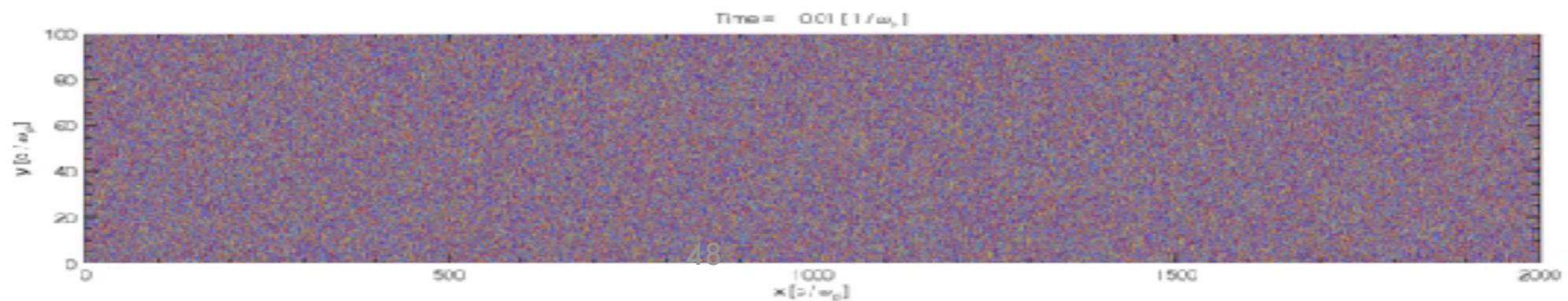
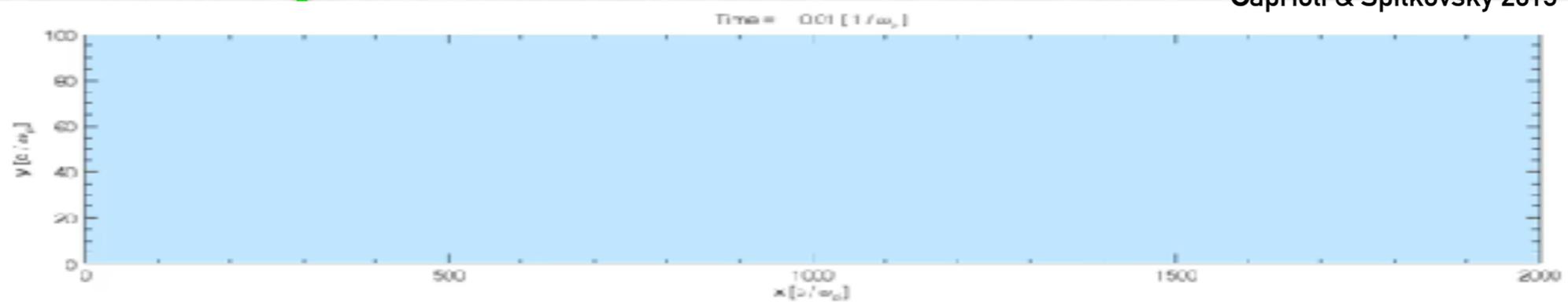


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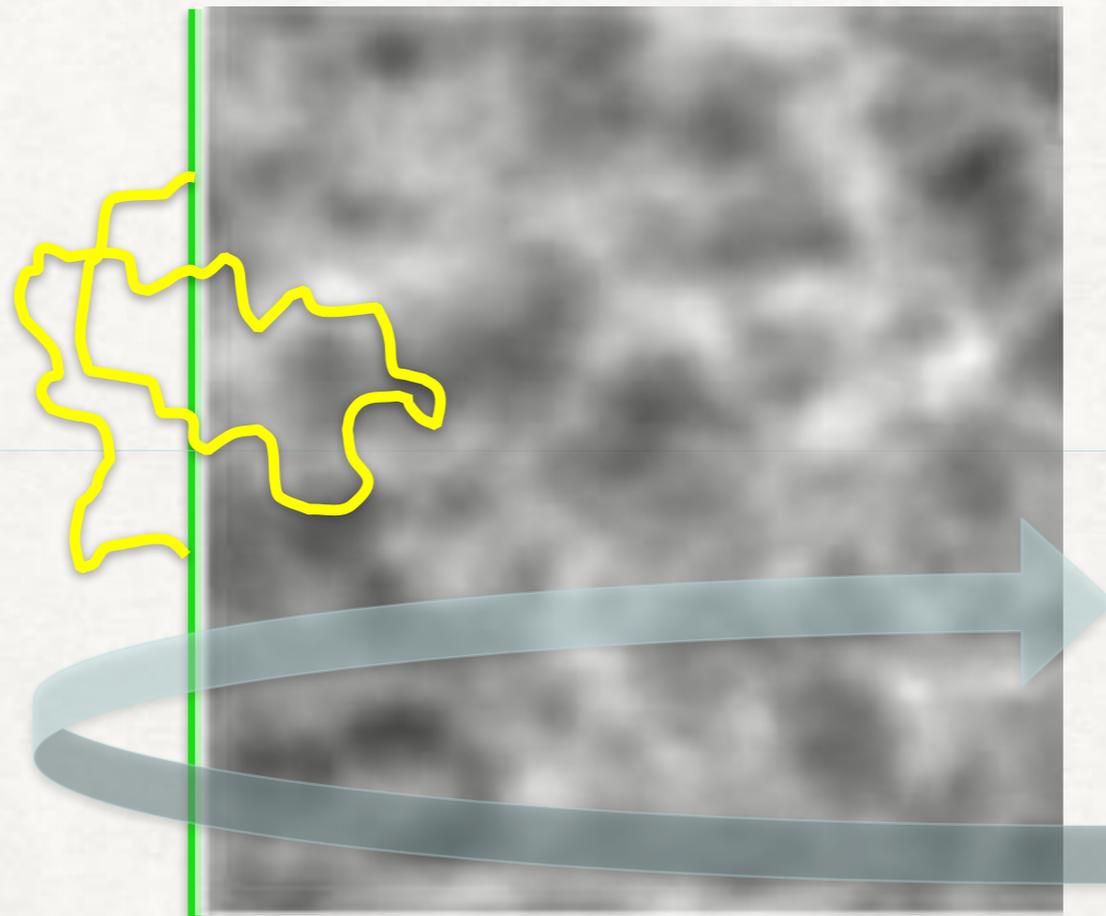


Bell & Schure 2013
Cardillo, Amato & PB 2015

Caprioli & Spitkovsky 2013

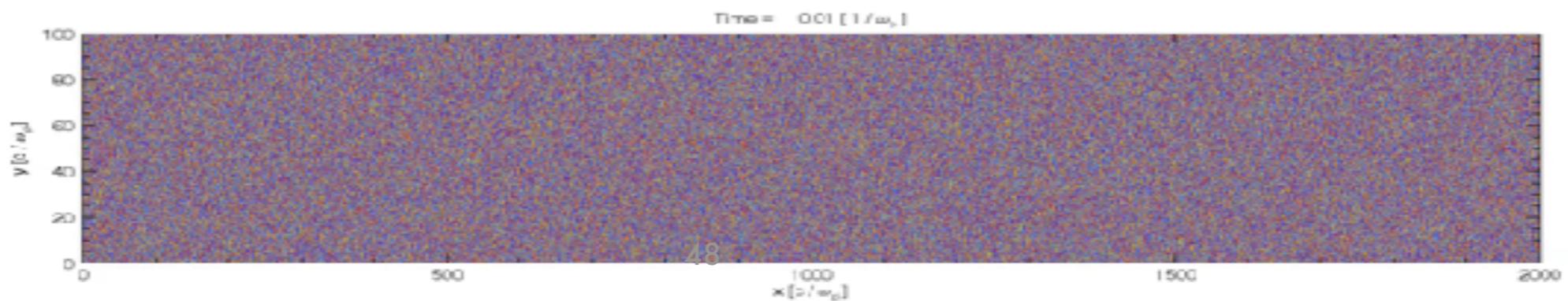
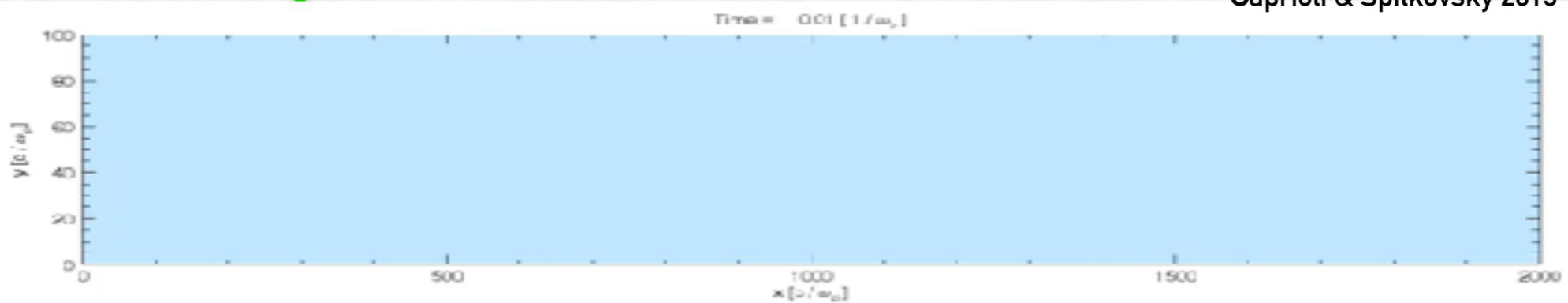


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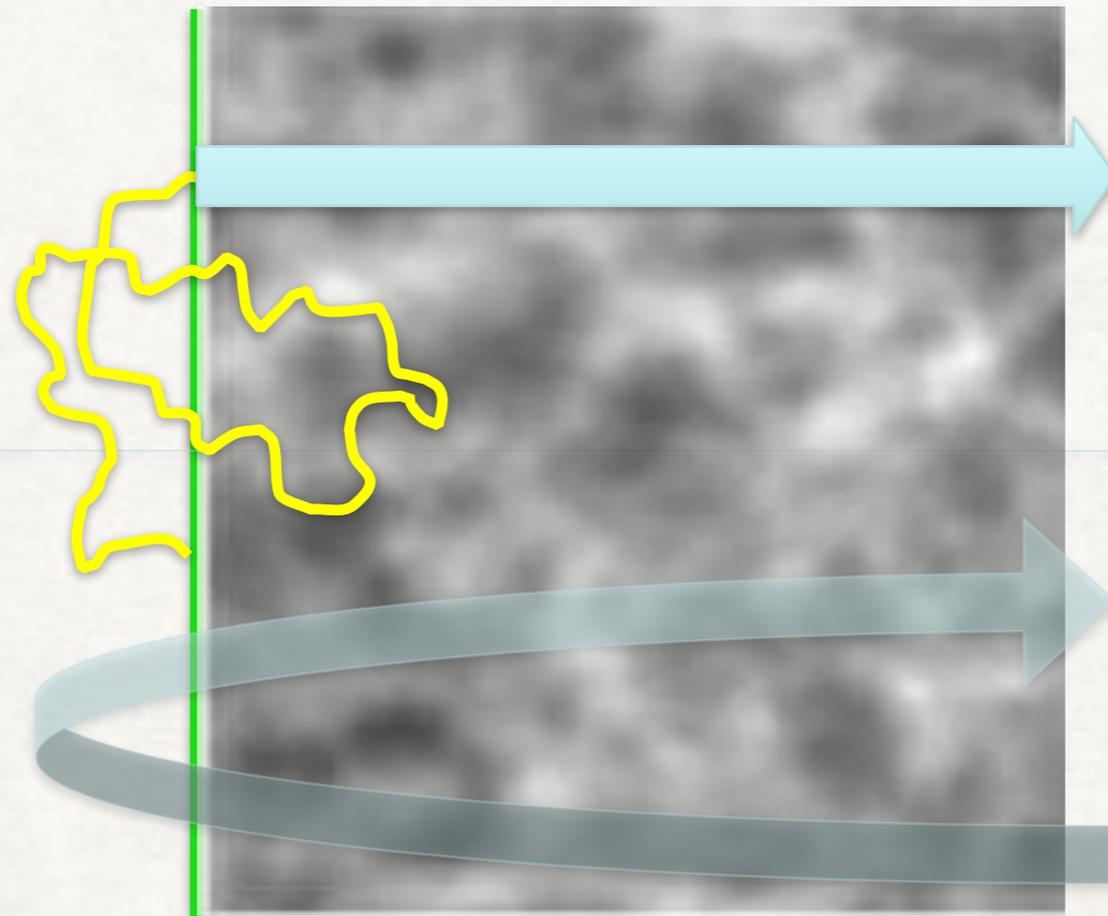


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Cardillo, Amato & PB 2015

Caprioli & Spitkovsky 2013

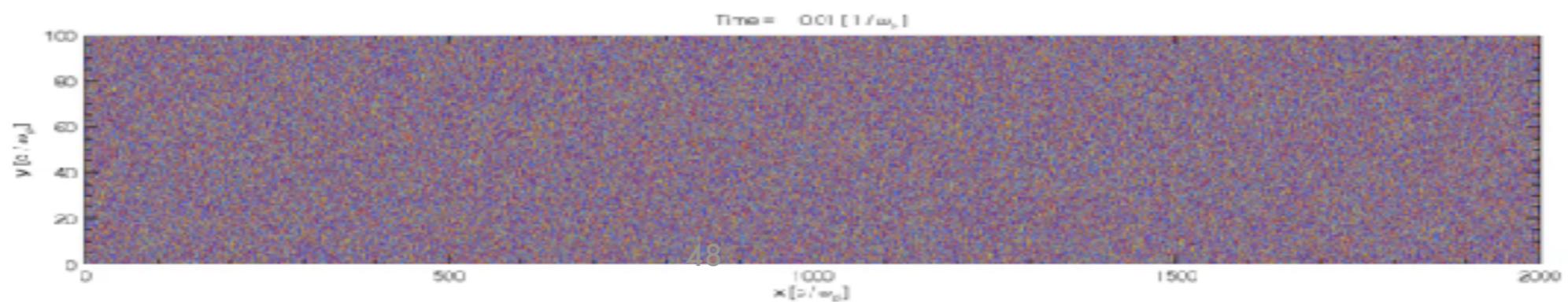
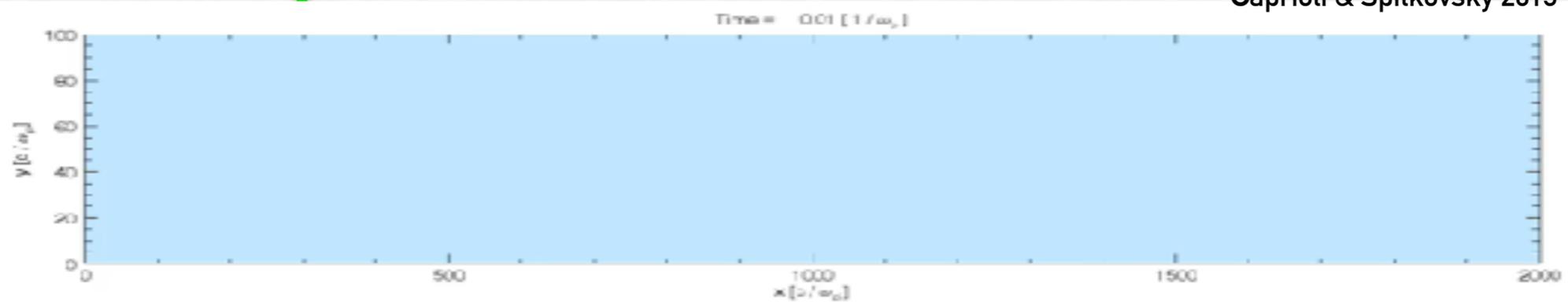


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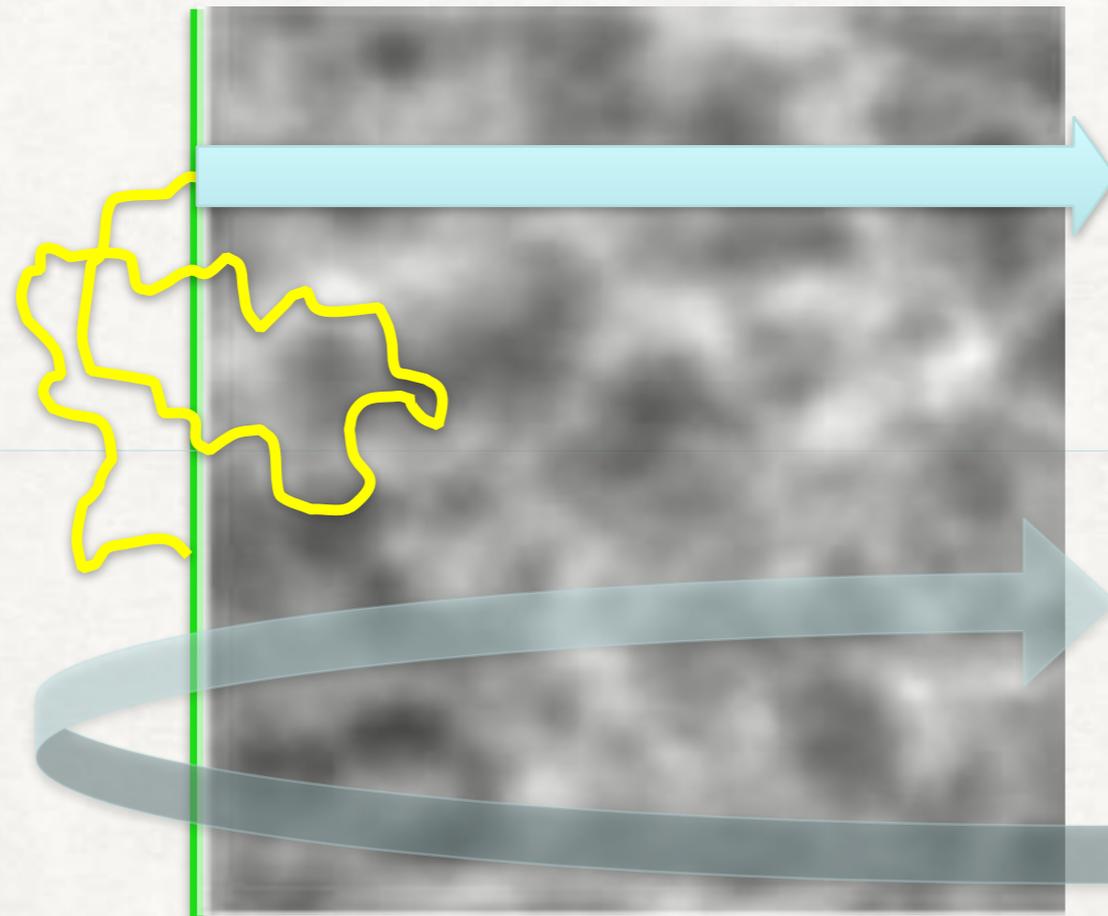


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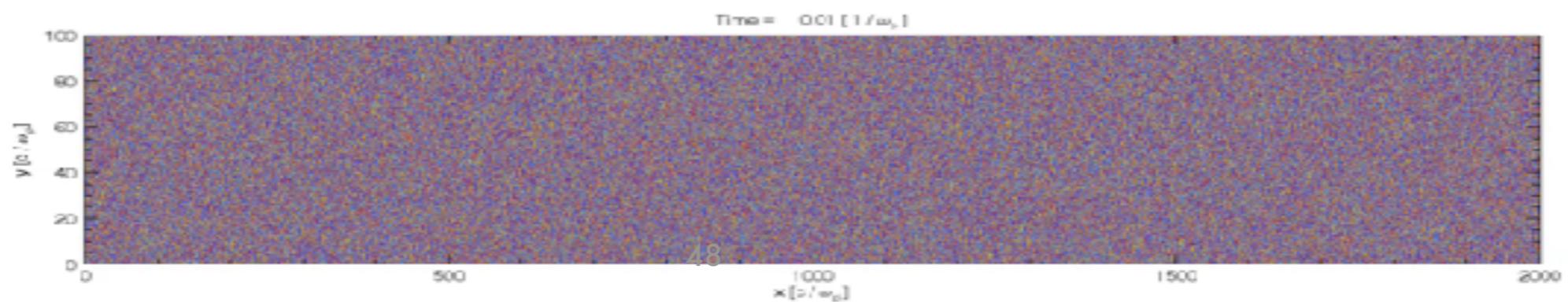
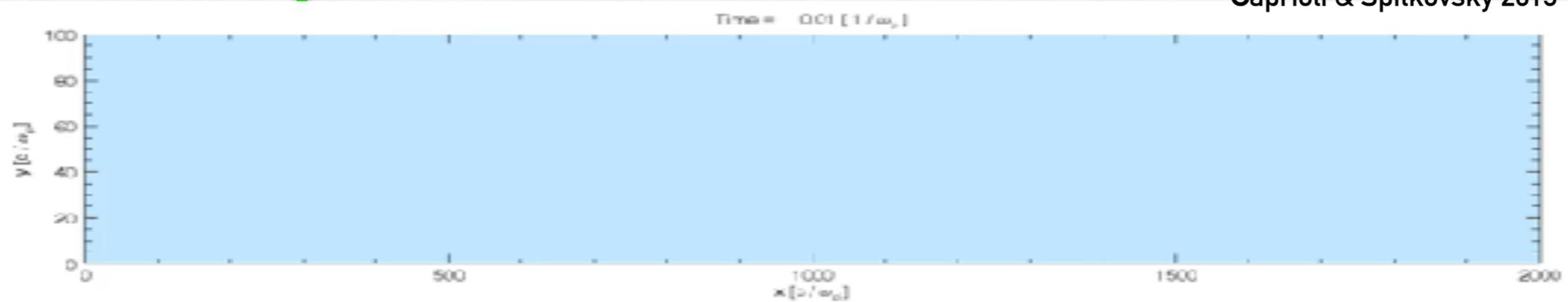


A QUALITATIVE PICTURE OF ACCELERATION



Bell & Schure 2013
Cardillo, Amato & PB 2015

Caprioli & Spitkovsky 2013

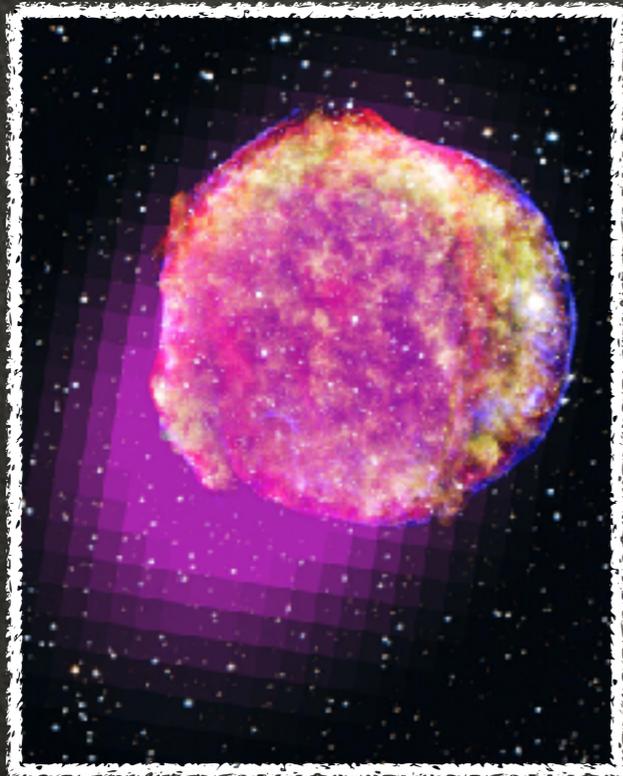


IMPLICATIONS FOR MAXIMUM ENERGY

Supernovae of type Ia

Explosion takes place in the ISM with spatially constant density

$$E_{max} \approx 130 \text{ TeV} \left(\frac{\xi_{CR}}{0.1} \right) \left(\frac{M_{ej}}{M_{\odot}} \right)^{-2/3} \left(\frac{E_{SN}}{10^{51} \text{ erg}} \right) \left(\frac{n_{ISM}}{\text{cm}^{-3}} \right)^{1/6}$$



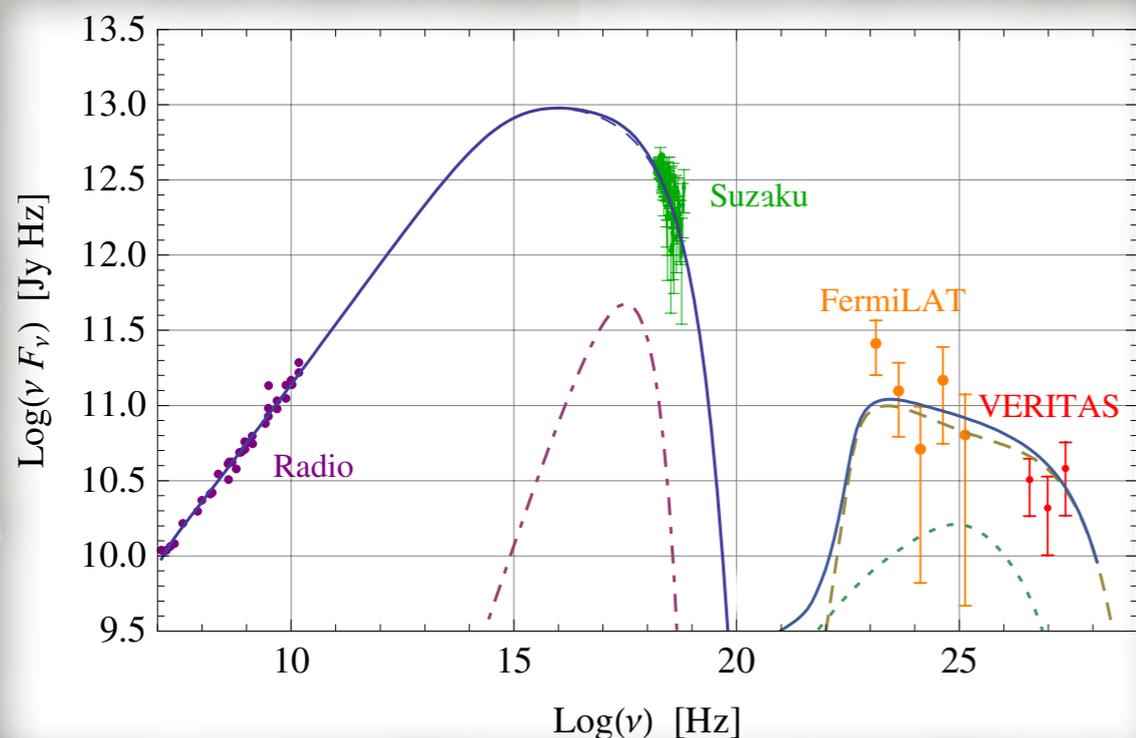
Supernovae of type II

IMPLICATIONS FOR MAXIMUM ENERGY

Supernovae of type Ia

Explosion takes place in the ISM with spatially constant density

$$E_{max} \approx 130 \text{ TeV} \left(\frac{\xi_{CR}}{0.1} \right) \left(\frac{M_{ej}}{M_{\odot}} \right)^{-2/3} \left(\frac{E_{SN}}{10^{51} \text{ erg}} \right) \left(\frac{n_{ISM}}{\text{cm}^{-3}} \right)^{1/6}$$



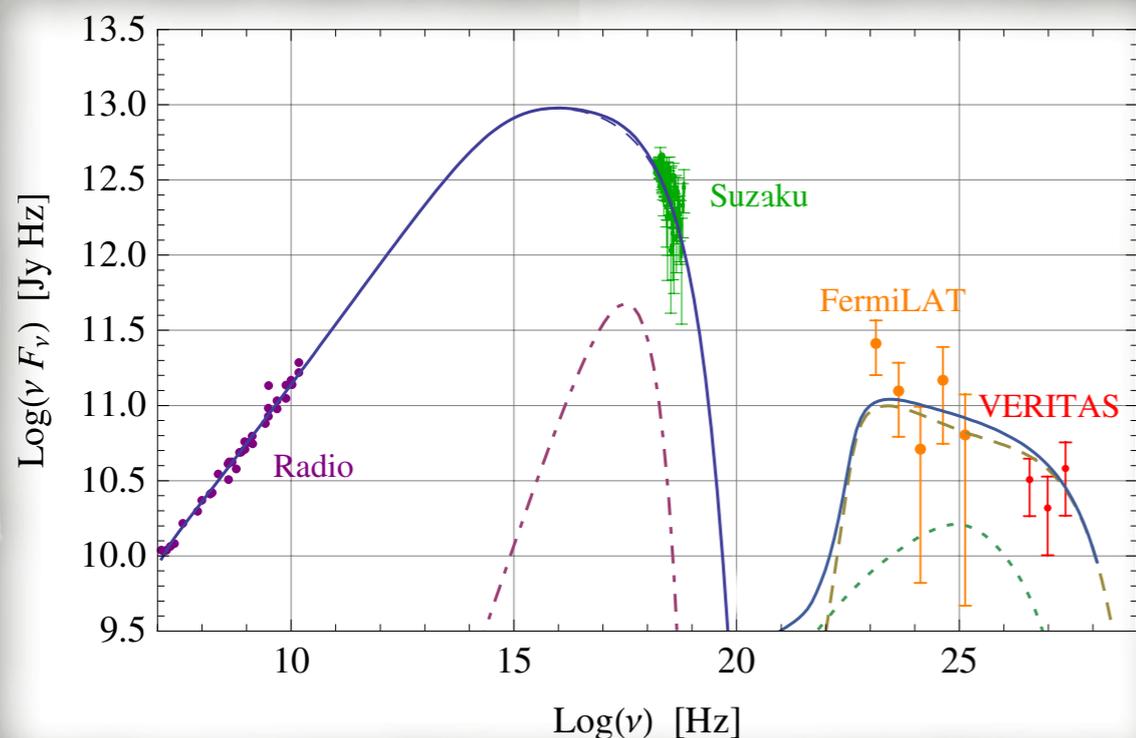
Supernovae of type II

IMPLICATIONS FOR MAXIMUM ENERGY

Supernovae of type Ia

Explosion takes place in the ISM with spatially constant density

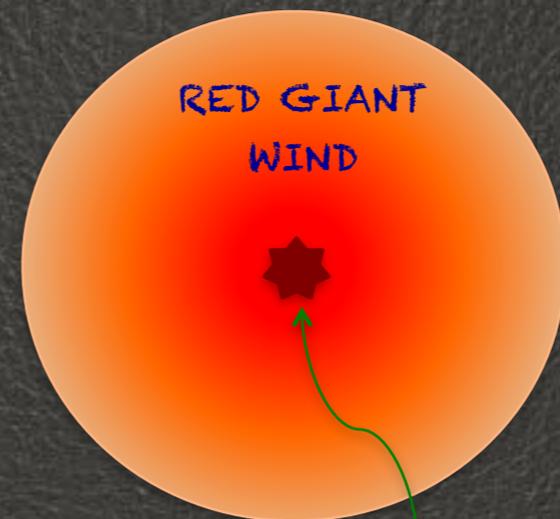
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Supernovae of type II

In most cases the explosion takes place in the dense wind of the red super-giant progenitor

$$\rho(r) = \frac{\dot{M}}{4\pi r^2 v_W}$$



The Sedov phase reached while the shock expands inside the wind

$$R = M_{ej} v_W / \dot{M}$$

This corresponds to typical times of few tens of years after the SN explosion !!!

$$E_{max} \approx 1 \text{ PeV} \left(\frac{\xi_{CR}}{0.1} \right) \left(\frac{M_{ej}}{M_{\odot}} \right)^{-1} \left(\frac{E_{SN}}{10^{51} \text{ erg}} \right) \times \left(\frac{\dot{M}}{10^{-5} M_{\odot} \text{ yr}^{-1}} \right)^{1/2} \left(\frac{v_{wind}}{10 \text{ km/s}} \right)^{-1/2}$$

X-ray rims and B-field amplification

TYPICAL THICKNESS OF FILAMENTS: $\sim 10^{-2}$ pc

The synchrotron limited thickness is:

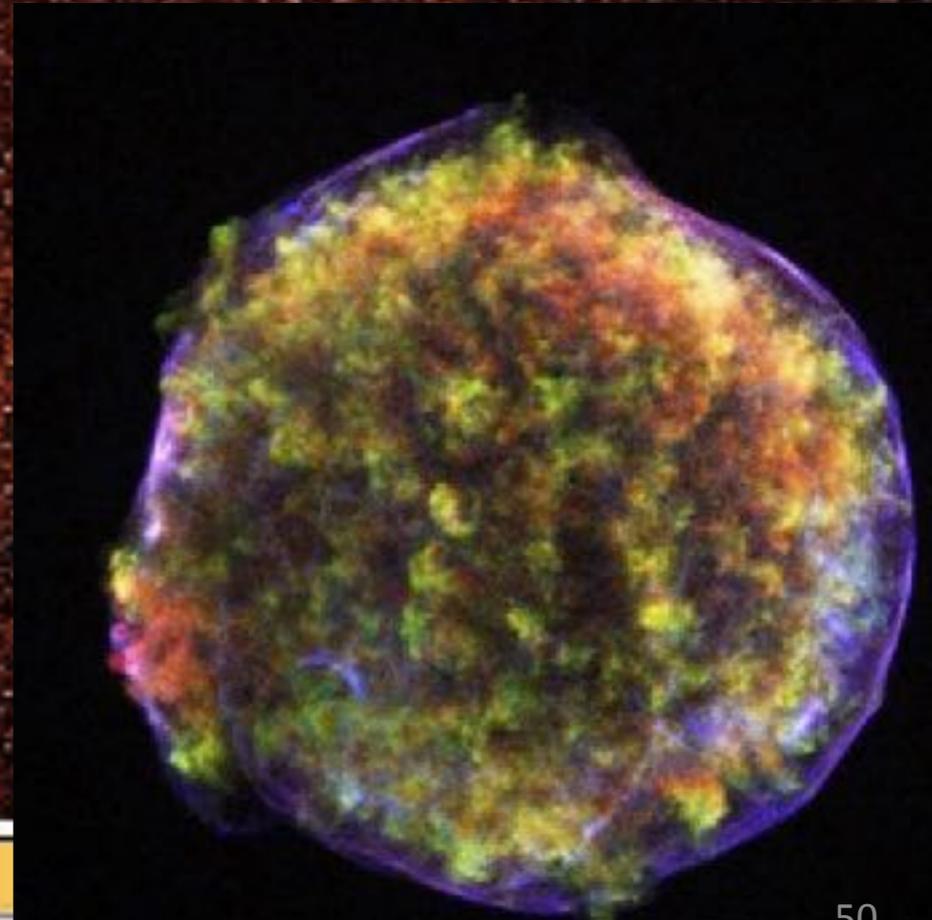
$$\Delta x \approx \sqrt{D(E_{max})\tau_{loss}(E_{max})} \approx 0.04 B_{100}^{-3/2} \text{ pc}$$

$B \approx 100 \mu\text{Gauss}$

$$E_{max} \approx 10 B_{100}^{-1/2} u_8 \text{ TeV}$$

$$\nu_{max} \approx 0.2 u_8^2 \text{ keV}$$

In some cases the strong fields are confirmed by time variability of X-rays
Uchiyama & Aharonian, 2007



SUCCESS AND PROBLEMS

○ Effective max energy at the beginning of Sedov phase (~30 years...) - not easy to catch Pevatrons with gamma rays...

○ No exponential cutoff at E_{\max} (broken power law)

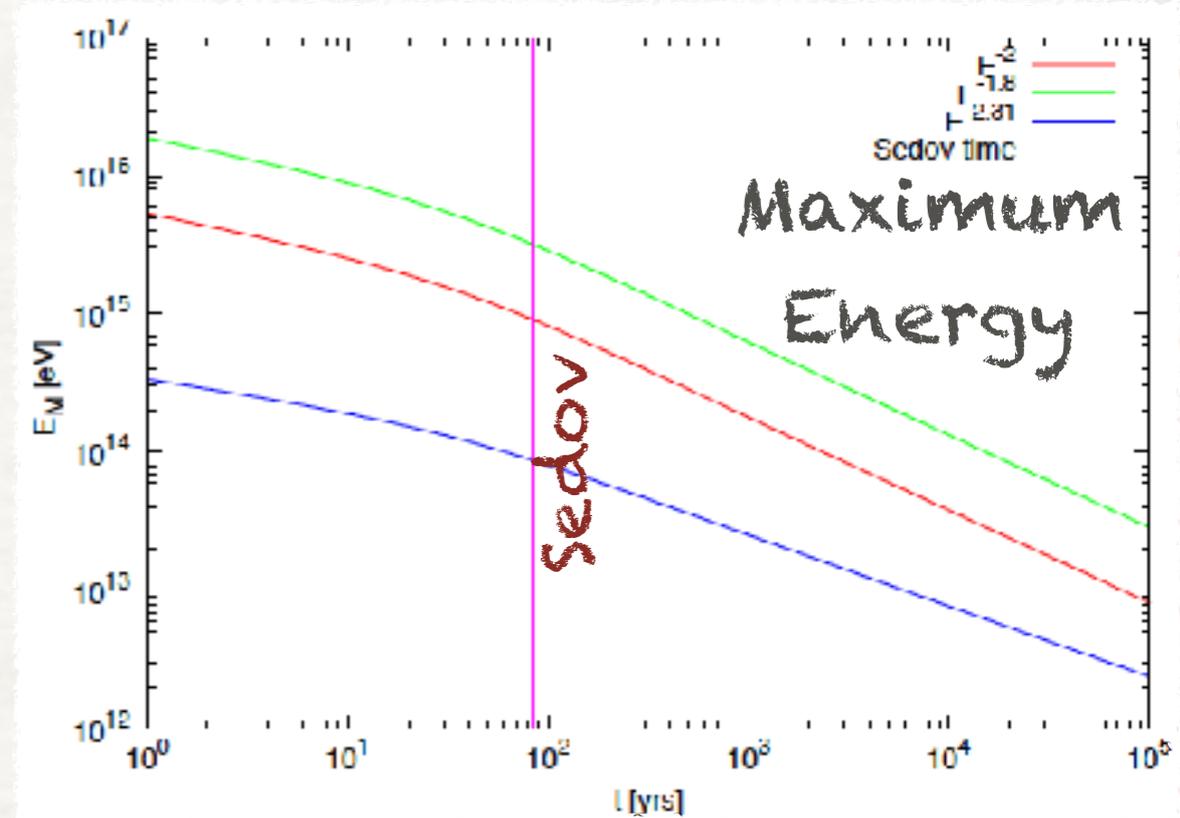
○ SPECTRUM OF ACCELERATED PARTICLES IS VERY CLOSE TO E^{-2}

○ SUCH HARD SPECTRUM NEEDED FOR GROWTH OF MODES

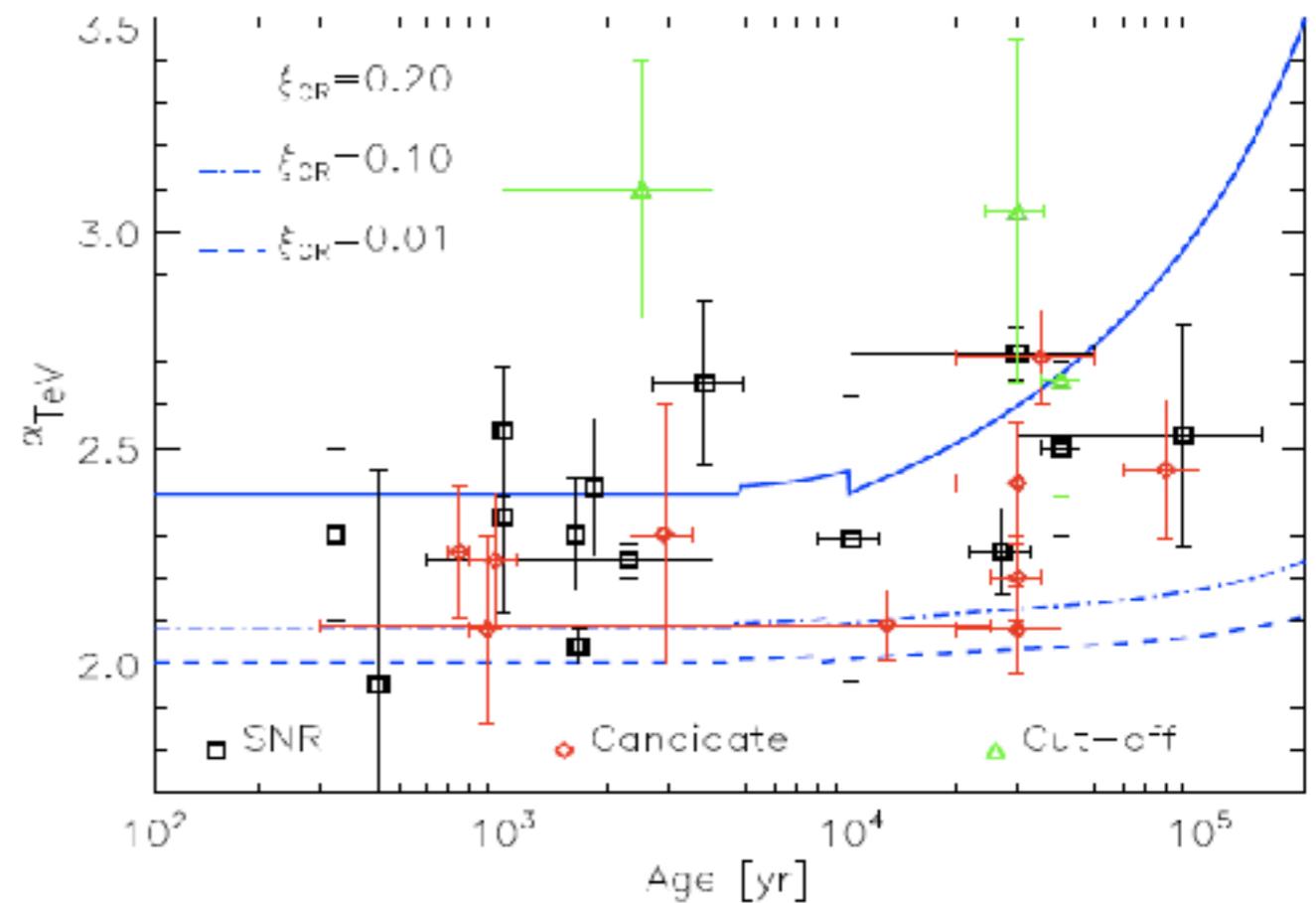
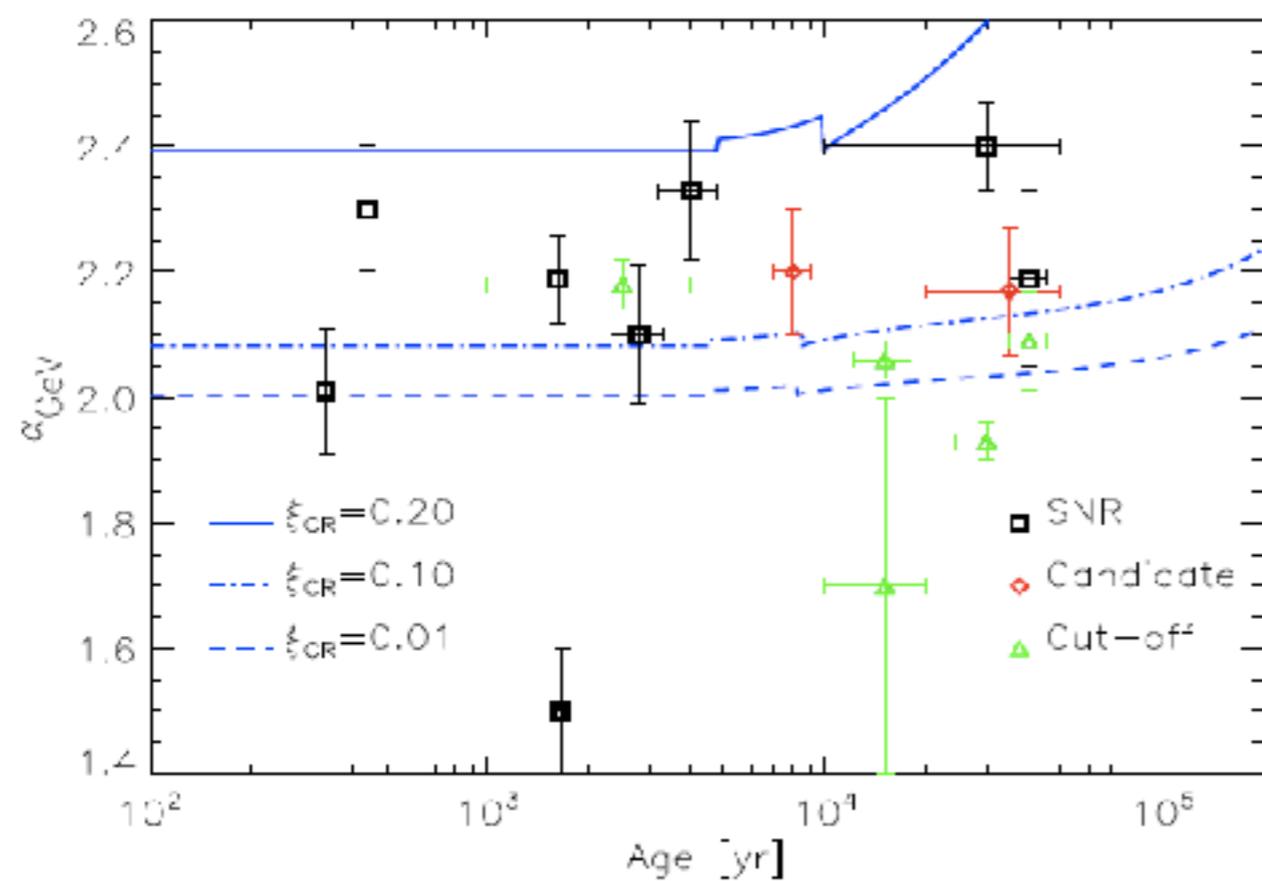
○ BUT NOT OBSERVED IN ANY SNR SO FAR!

○ AND CERTAINLY NOT THE ONE REQUIRED BY TRANSPORT THEORY

Cardillo, Amato & PB 2015



ISSUES WITH SPECTRA INSIDE SNR



Caprioli 2011

DSA IN PARTIALLY IONIZED MEDIA

MOTIVATION

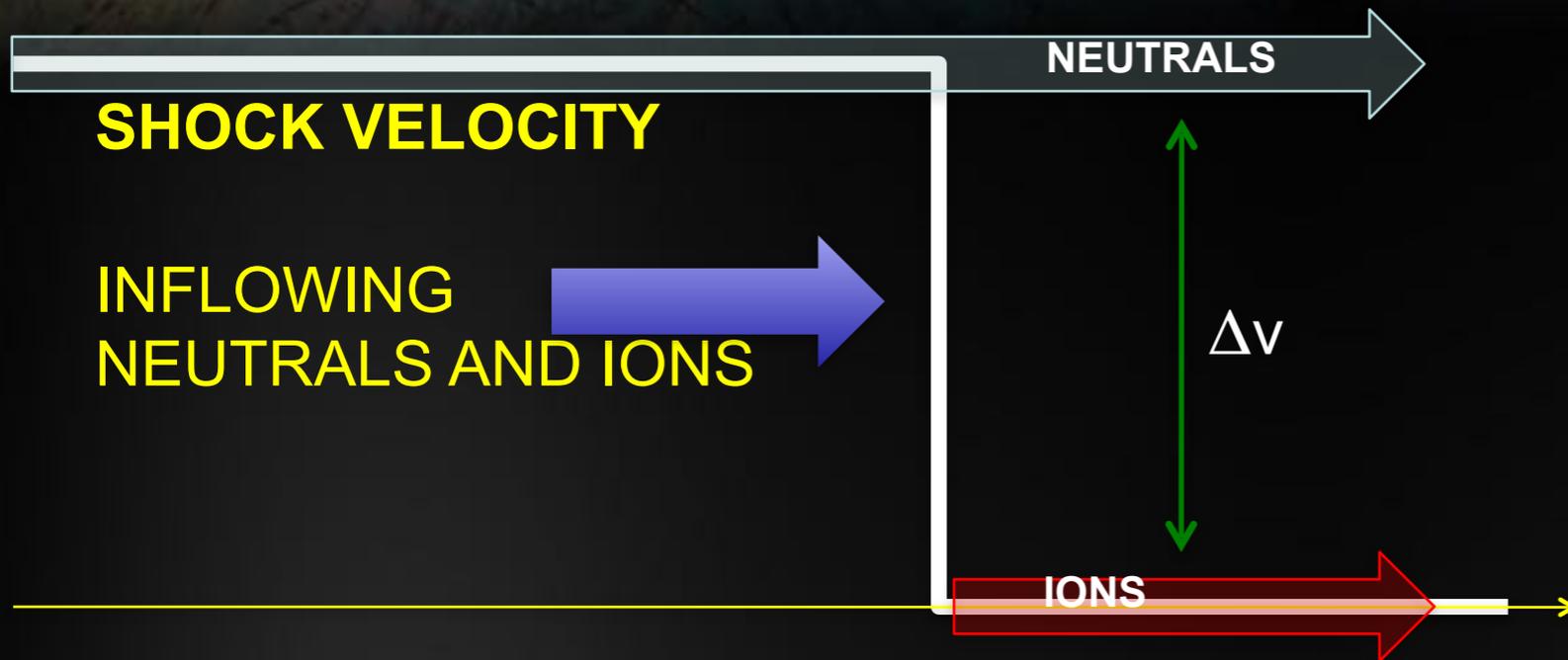
THE COLLISIONLESS NATURE OF MOST ASTROPHYSICAL SHOCKS LEADS TO THE RELEVANT QUESTION 'WHAT DO NEUTRAL ATOMS DO AT THE SHOCK?' (see case of pick up ions at the solar wind termination shock)

PARTIALLY IONIZED PLASMAS ARE THE NORM, AT LEAST IN THE ORDINARY ISM WHERE SN TYPE Ia EXPLODE BUT ALSO IN THE SURROUNDINGS OF SOME TYPE II SN

- 1) SHOCK MODIFICATION INDUCED BY NEUTRALS IN THE ABSENCE OF ACCELERATED PARTICLES
 - a) Neutral return flux
 - b) Spectra of test particles accelerated at neutrals-mediated collisionless shocks

- 2) NON LINEAR THEORY OF DSA IN THE PRESENCE OF NEUTRALS
 - a) Shock modification induced by neutrals vs CR modification
 - b) Narrow and broad Balmer lines in the presence of efficient CR acceleration
 - c) Application to some SNR where Balmer emission is observed

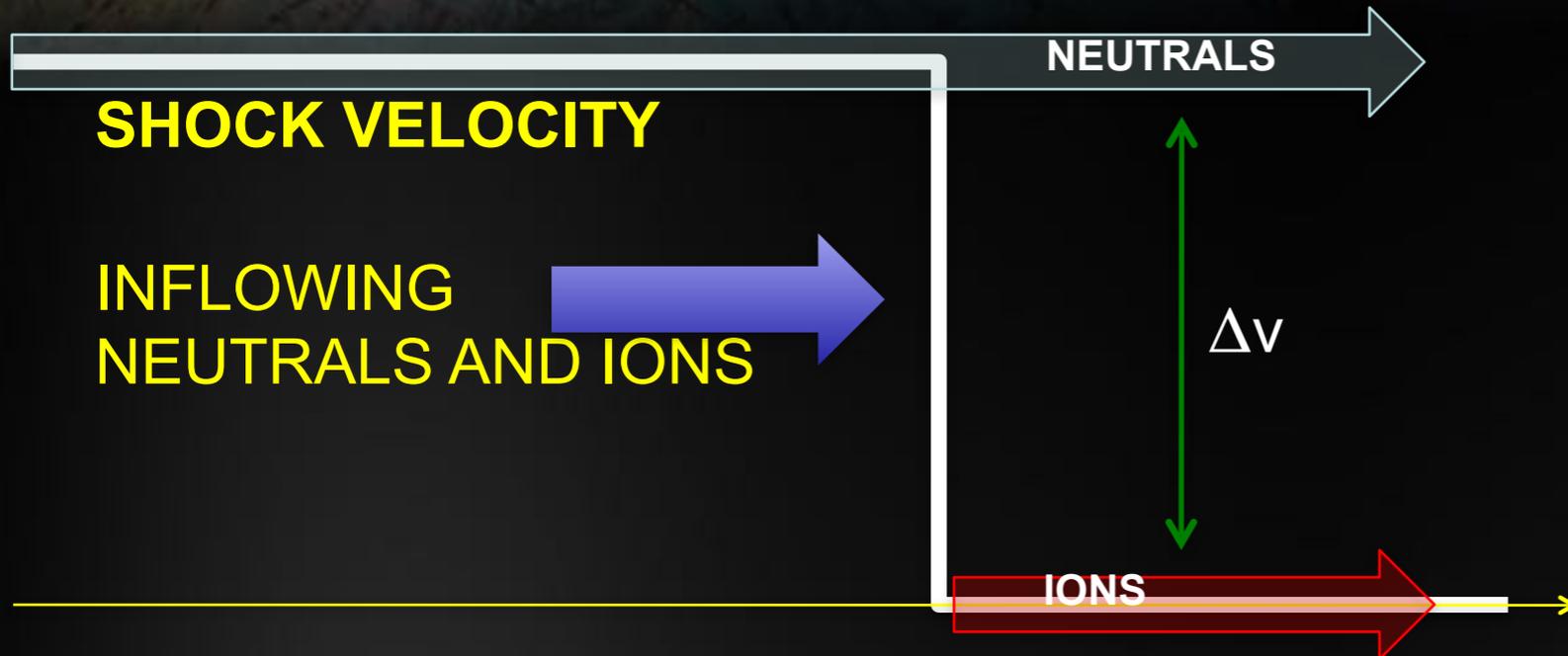
SHOCKS IN PARTIALLY IONIZED PLASMAS



AT ZERO ORDER NOTHING HAPPENS TO NEUTRALS

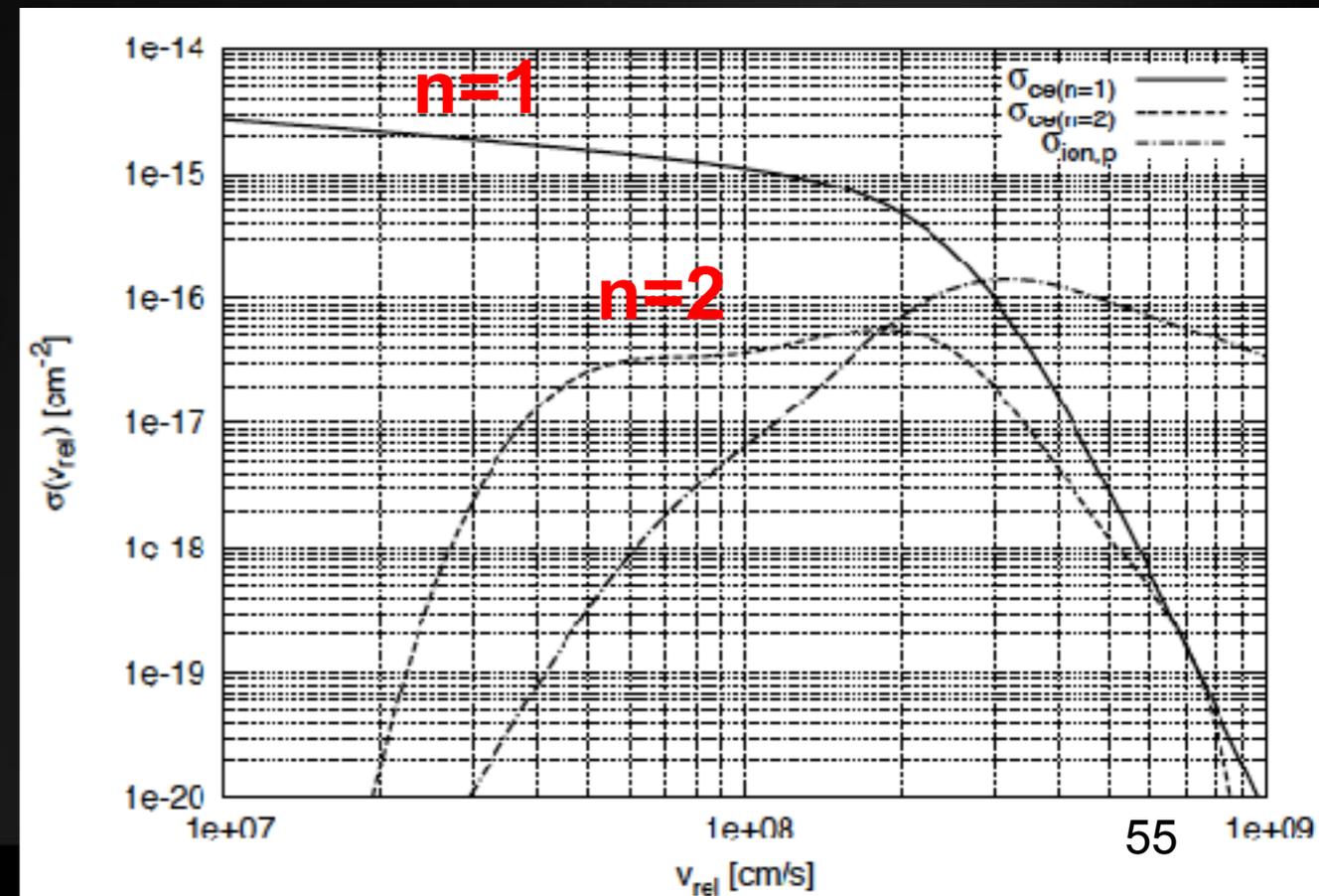
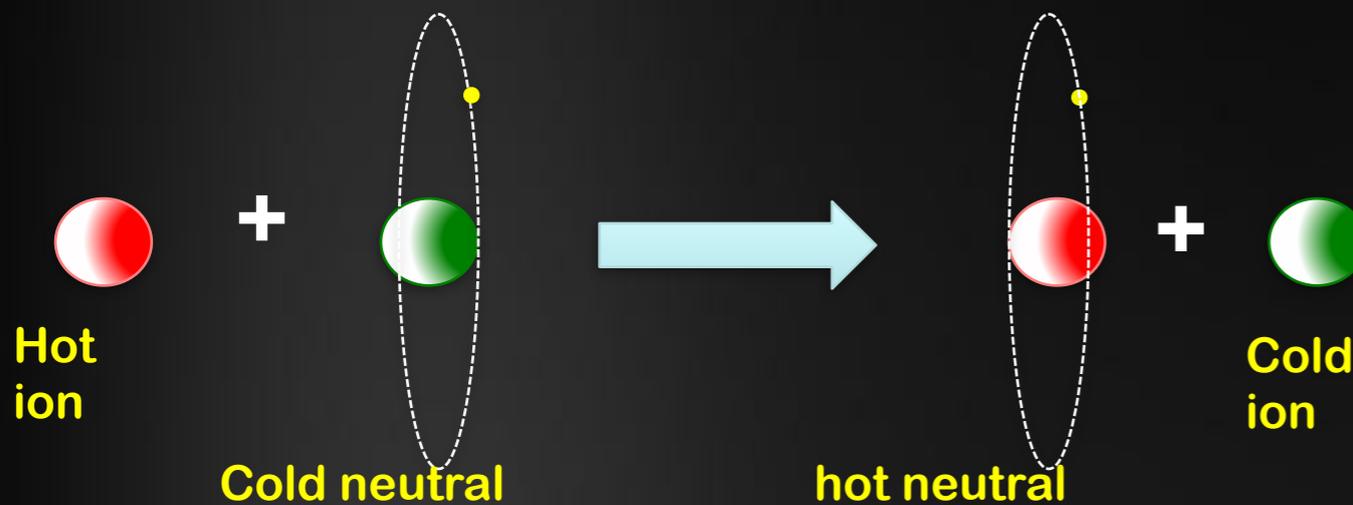
IONS ARE HEATED UP AND SLOWED DOWN

SHOCKS IN PARTIALLY IONIZED PLASMAS



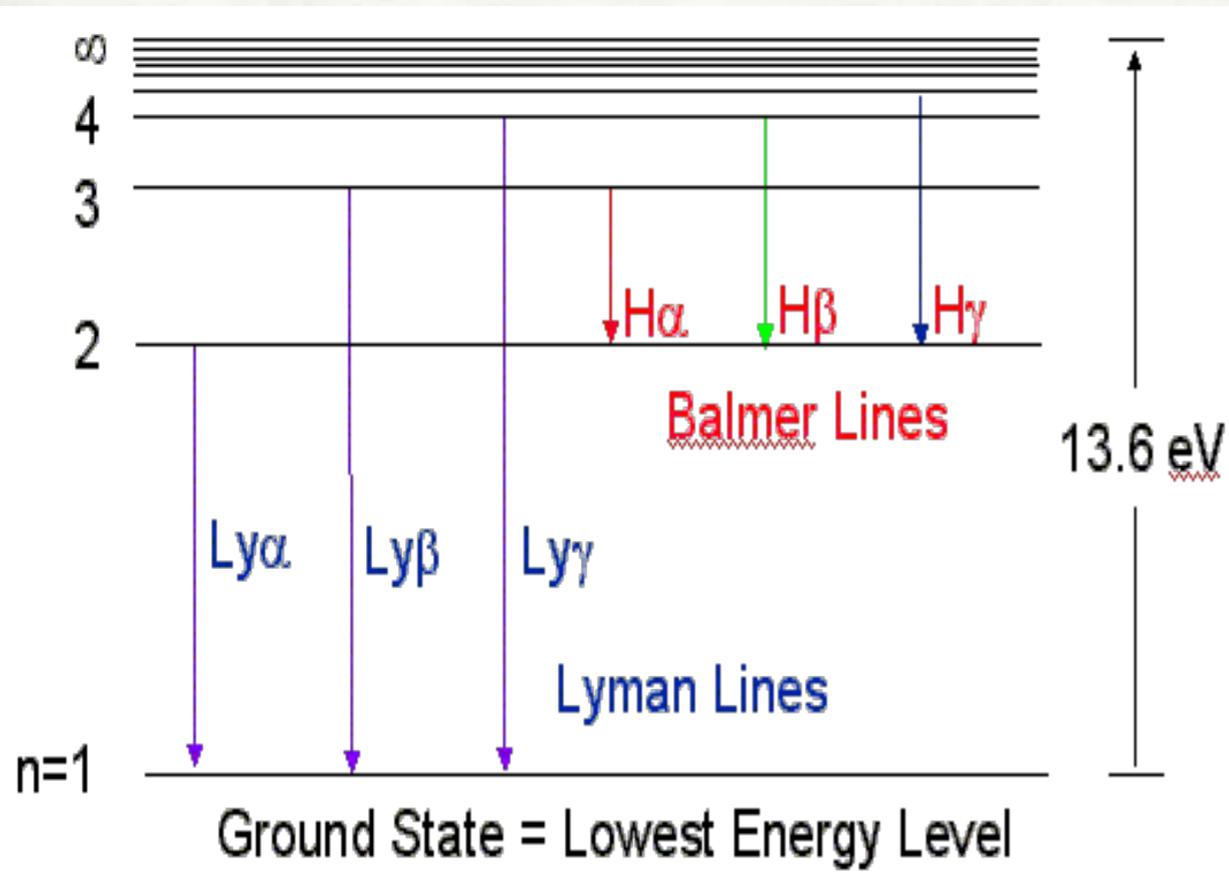
AT ZERO ORDER NOTHING HAPPENS TO NEUTRALS

IONS ARE HEATED UP AND SLOWED DOWN



BASIC PHYSICS OF BALMER SHOCKS

[Chevalier & Raymond (1978); Chevalier et al. (1980)]



H α LINES ARE PRODUCED AFTER EXCITATION OF H ATOMS TO THE n=3 AND DE-EXCITATION TO n=2

IF EXCITATION OCCURS BEFORE THE ATOM SUFFERS A CHARGE EXCHANGE \rightarrow NARROW BALMER LINE (ION T UPSTREAM)

IF H IS EXCITED AFTER CHARGE EXCHANGE DOWNSTREAM \rightarrow BROAD BALMER LINE (ION T DOWNSTREAM)

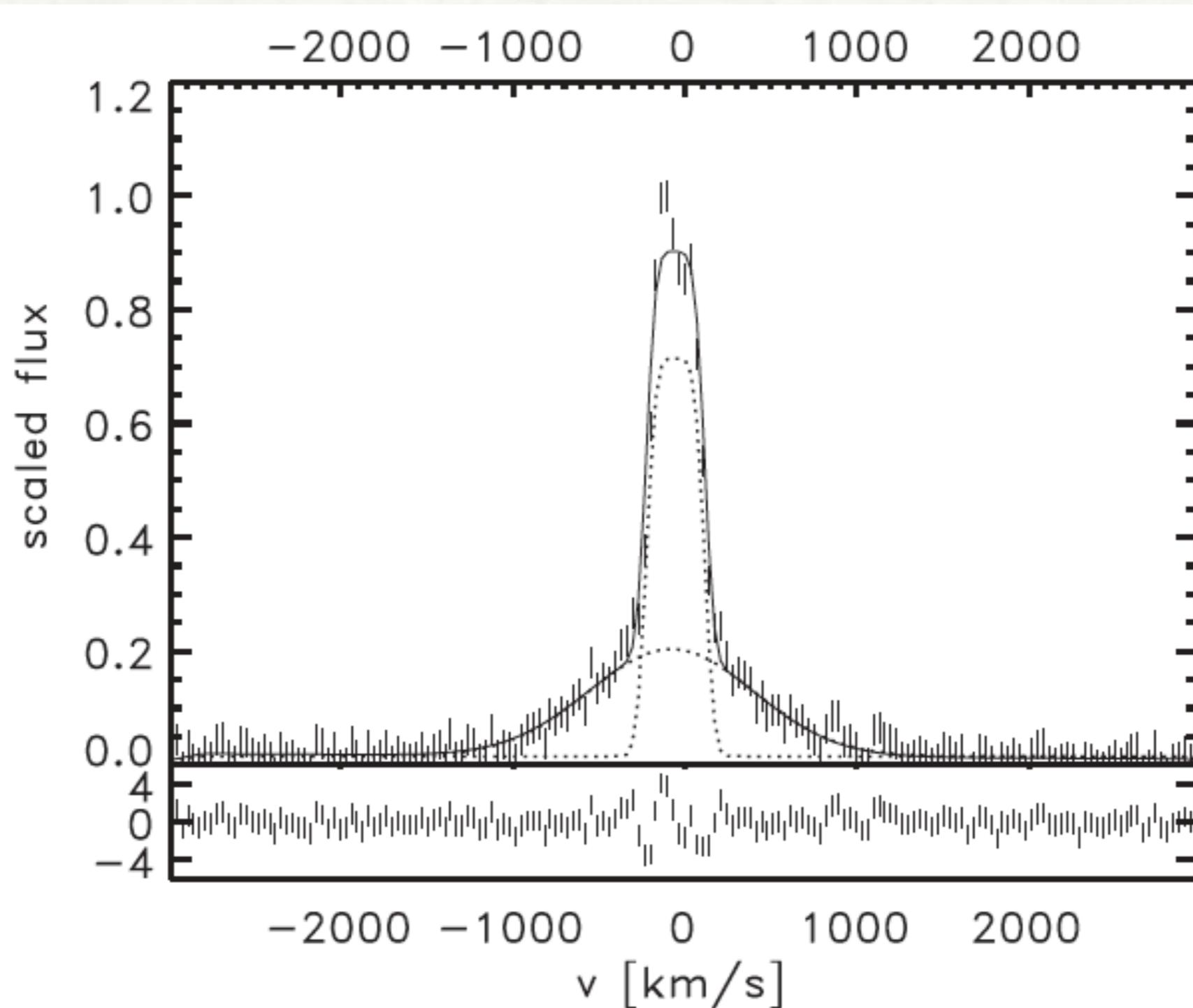
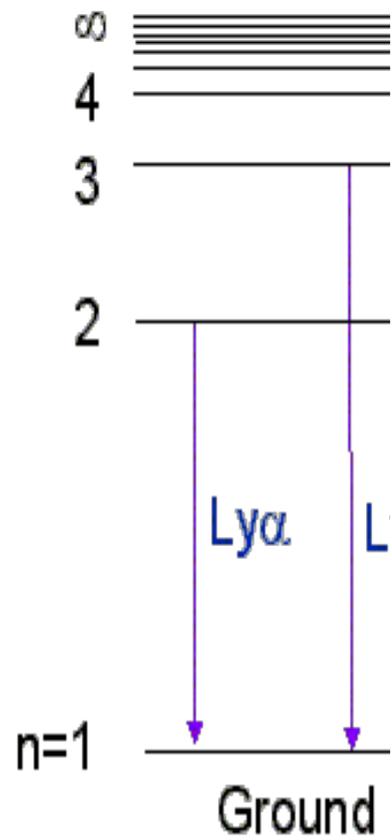
THE WIDTH OF THE BROAD H α LINES TELLS US ABOUT THE ION TEMPERATURE DOWNSTREAM OF THE SHOCK

$$W_{\text{narrow}} \propto \sqrt{T_0}$$

$$W_{\text{broad}} \propto \sqrt{T_2} \sim V_{sh}$$

BASIC PHYSICS OF BALMER SHOCKS

[Chevalier & Raymond (1978); Chevalier et al. (1980)]



THE WIDTH
DOWNSTREAM

narrow $v \approx 0$

broad $v \approx 2000$ sh

PRODUCED AFTER
S TO THE $n=3$
 $n=2$

BEFORE THE
E EXCHANGE
LINE (ION T

ER CHARGE
M \rightarrow BROAD
STREAM)

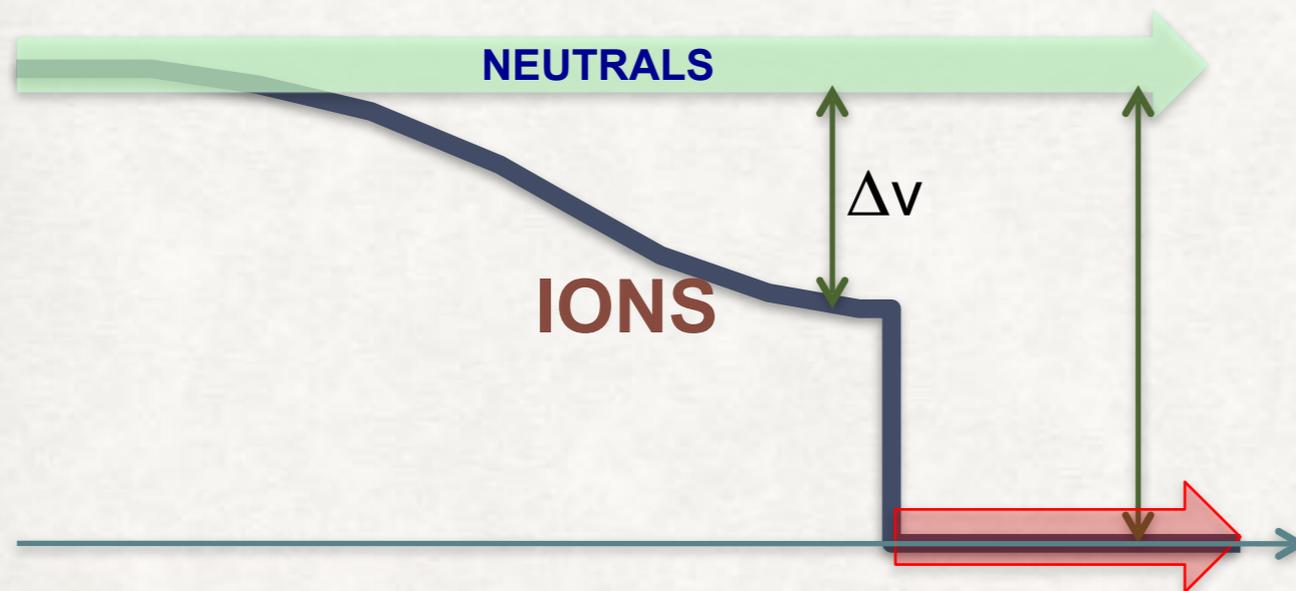
TEMPERATURE

BALMER LINE WIDTHS IN CR MODIFIED SHOCKS

IN THE PRESENCE OF PARTICLE ACCELERATION TWO THINGS HAPPEN:

LOWER TEMPERATURE DOWNSTREAM

A PRECURSOR APPEARS UPSTREAM



**BROAD BALMER LINE GETS
NARROWER**

**NARROW BALMER LINE
GETS BROADER**

BALMER SHOCKS WITH NO CR

PB, Morlino, Bandiera, Amato & Caprioli, 2012

IONS ARE TREATED AS A PLASMA WITH GIVEN DENSITY AND A THERMAL DISTRIBUTION

NEUTRAL ATOMS ARE DESCRIBED USING A BOLTZMAN EQUATION WITH SCATTERING TERMS DESCRIBING CHARGE EXCHANGE AND IONIZATION

$$v_z \frac{\partial f_N(z, \mathbf{v})}{\partial z} = f_i(z, \mathbf{v}) \beta_N(z, \mathbf{v}) - f_N(z, \mathbf{v}) \beta_i(z, \mathbf{v})$$

$$\beta_i(z, \mathbf{v}) = \int d^3 w \, v_{rel} \left[\sigma_{ce}(v_{rel}) + \sigma_{ion}(v_{rel}) \right] f_i(z, \mathbf{w})$$

$$\beta_N(z, \mathbf{v}) = \int d^3 w \, v_{rel} \sigma_{ce}(v_{rel}) f_N(z, \mathbf{w})$$

Partial Scattering Functions

PB+ 2012

WE INTRODUCE THE FUNCTIONS: $f_N^{(k)}(z, v_{\parallel}, v_{\perp})$

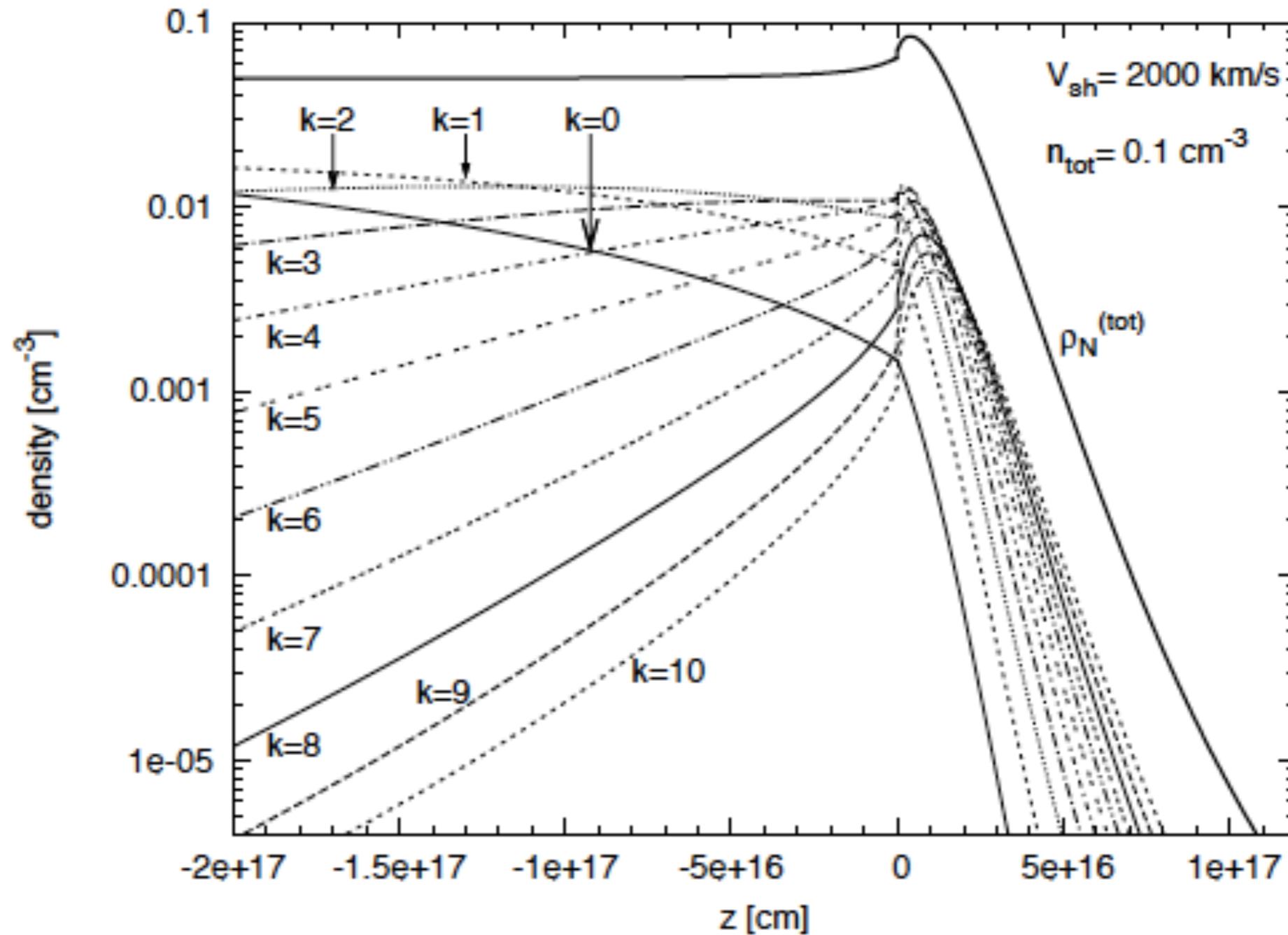
THEY REPRESENT THE DISTRIBUTION FUNCTIONS OF NEUTRALS THAT SUFFERED 0, 1, 2, ..., k CHARGE EXCHANGE REACTIONS AT GIVEN LOCATION. THEY SATISFY:

$$v_{\parallel} \frac{\partial f_N^{(0)}}{\partial z} = -\beta_i f_N^{(0)} \quad v_{\parallel} \frac{\partial f_N^{(k)}}{\partial z} = \beta_N^{(k-1)} f_i - \beta_i f_N^{(k)} \quad k=1,2,\dots$$

WE SOLVE THESE EQUATIONS ANALYTICALLY AND THE TOTAL SOLUTION CAN BE WRITTEN AS:

$$f_N(z, v_{\parallel}, v_{\perp}) = \sum_{k=0}^{\infty} f_N^{(k)}(z, v_{\parallel}, v_{\perp})$$

Spatial dependence of the partial scattering functions



PB+2012

SHOCKS IN PARTIALLY IONIZED MEDIA WITH NO CR

PB, Morlino, Bandiera, Amato & Caprioli, 2012

IONS AND NEUTRALS ARE CROSS-REGULATED THROUGH MASS, MOMENTUM AND ENERGY CONSERVATION:

Flux conservation:

$$\frac{\partial}{\partial z} [\rho_i u_i + F_{mass}] = 0$$

MASS FLUX

$$\frac{\partial}{\partial z} [\rho_i u_i^2 + P_i + F_{mom}] = 0$$

MOMENTUM FLUX

$$\frac{\partial}{\partial z} \left[\frac{1}{2} \rho_i u_i^3 + \frac{\gamma_g}{\gamma_g - 1} P_i u_i + F_{en} \right] = 0$$

ENERGY FLUX

$$F_{mass} = m_p \int d^3 v v_z f_N$$

$$F_{mom} = m_p \int d^3 v v_z^2 f_N$$

$$F_{en} = \frac{m_p}{2} \int d^3 v v_z (v_z^2 + v_{\perp}^2) f_N$$

NEUTRAL RETURN FLUX

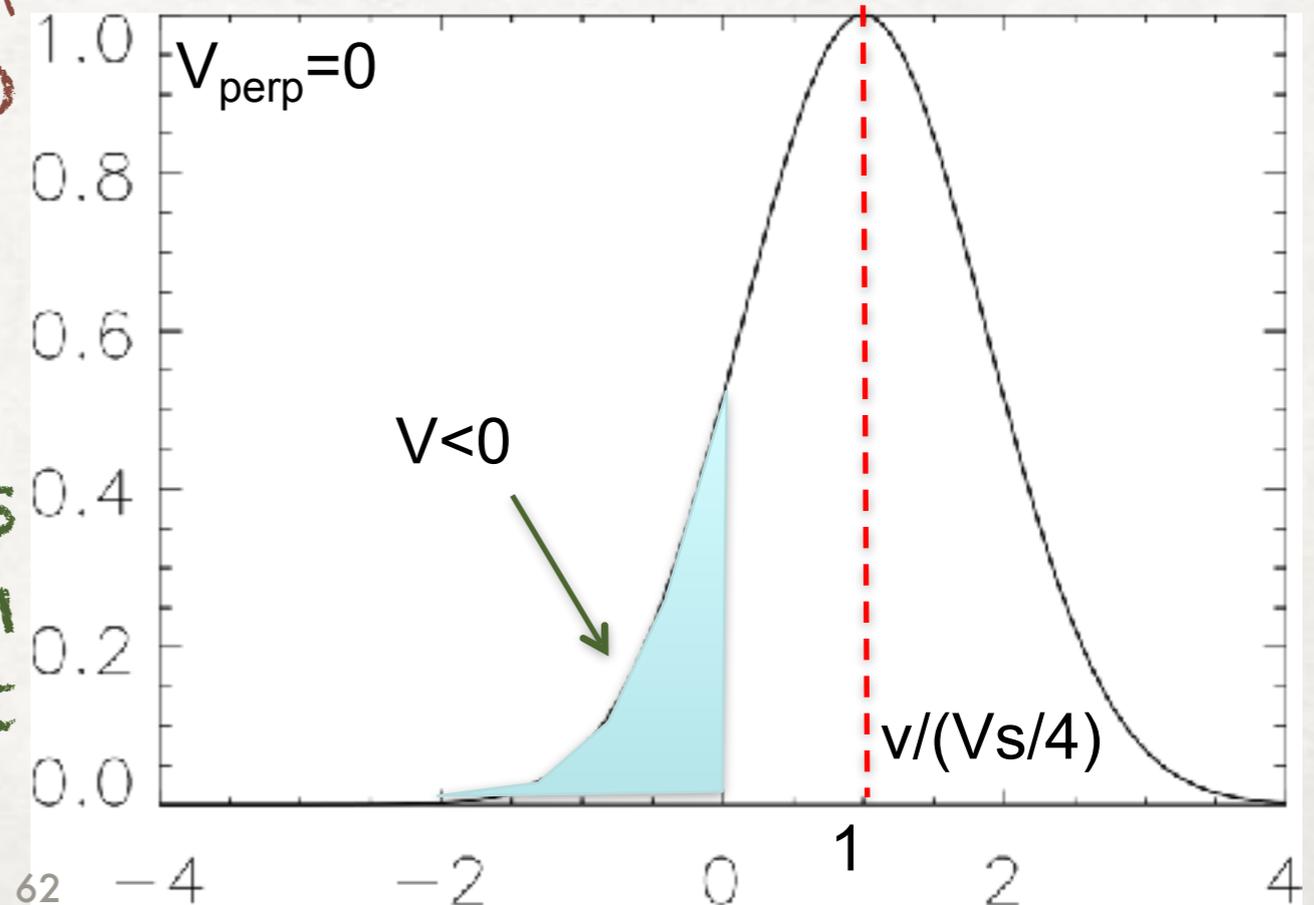
PB et al. 2012

NEUTRALS
AND IONS

SHOCK VELOCITY

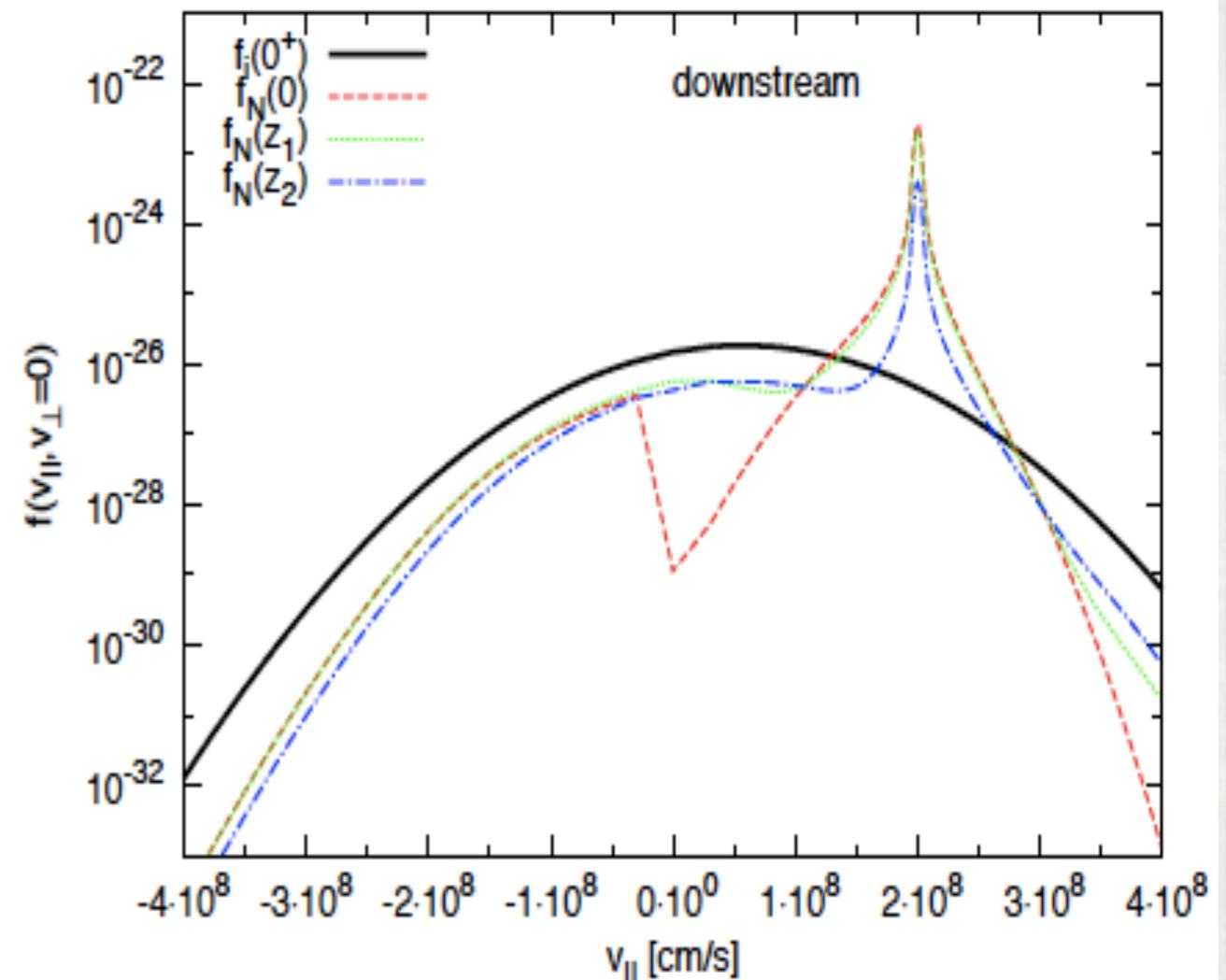
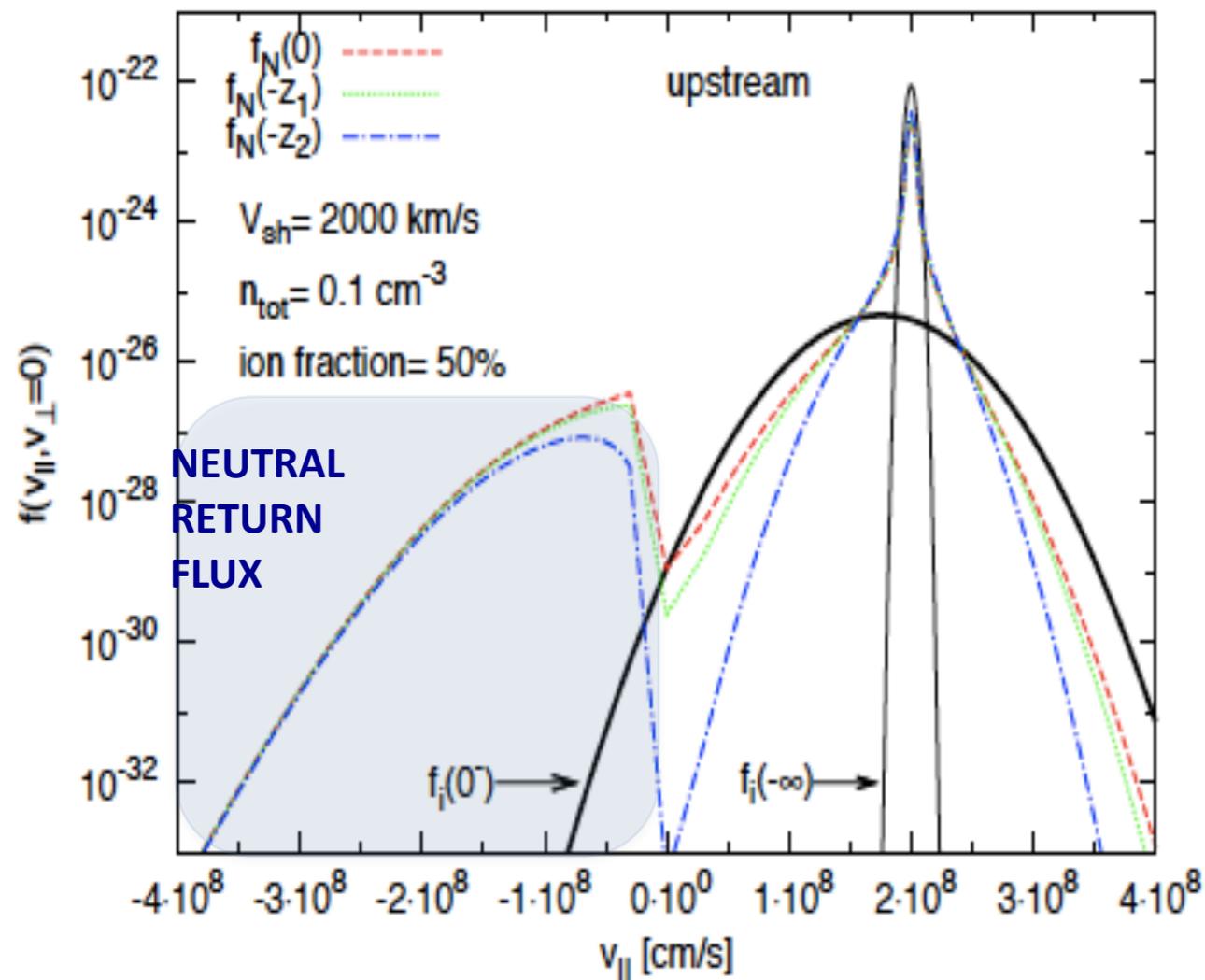
A NEUTRAL ATOM CAN CHARGE EXCHANGE WITH AN ION WITH $v < 0$, THEREBY GIVING RISE TO A NEUTRAL WHICH IS NOW FREE TO RETURN UPSTREAM

THIS NEUTRAL RETURN FLUX LEADS TO ENERGY AND MOMENTUM DEPOSITION UPSTREAM OF THE SHOCK!



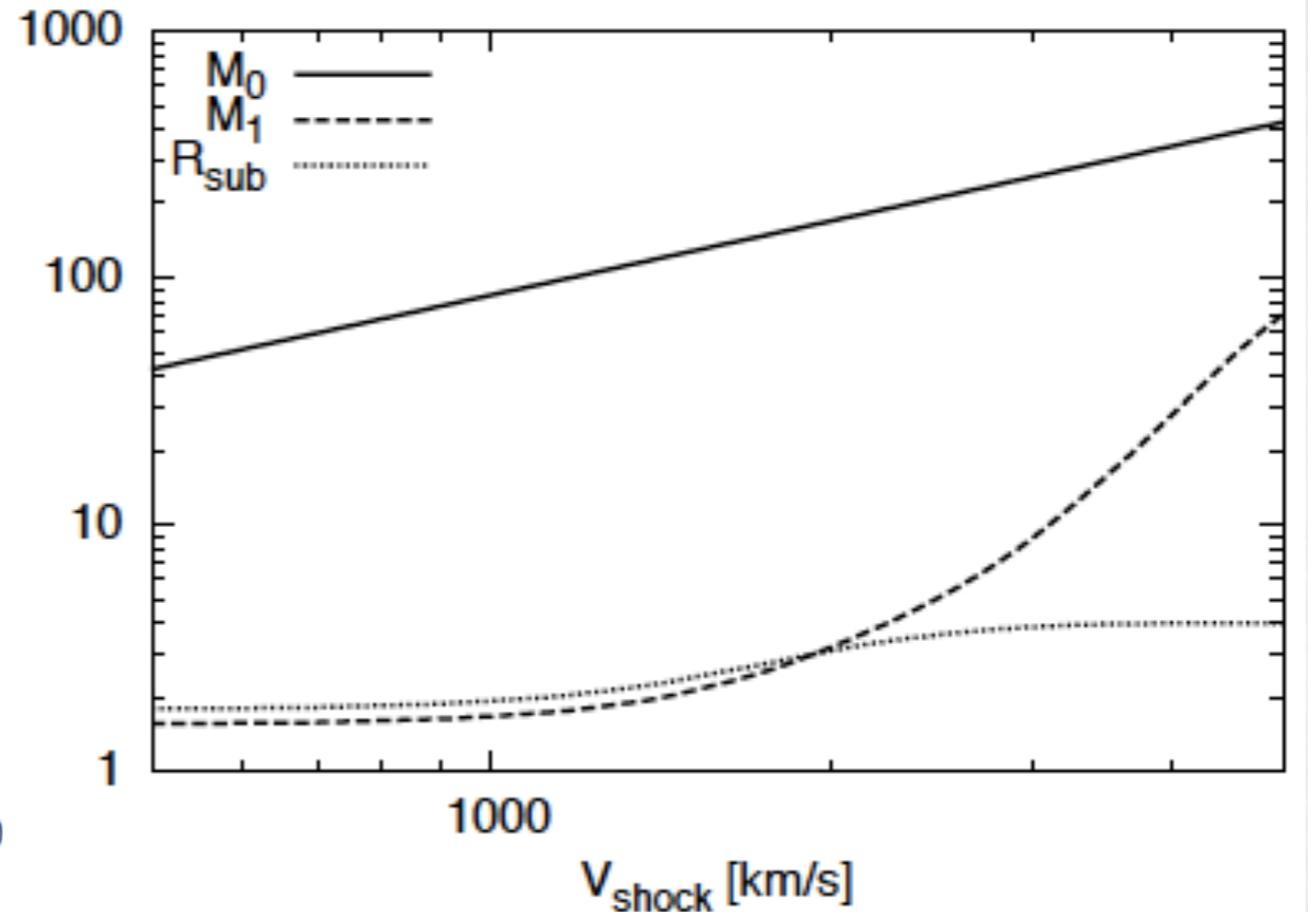
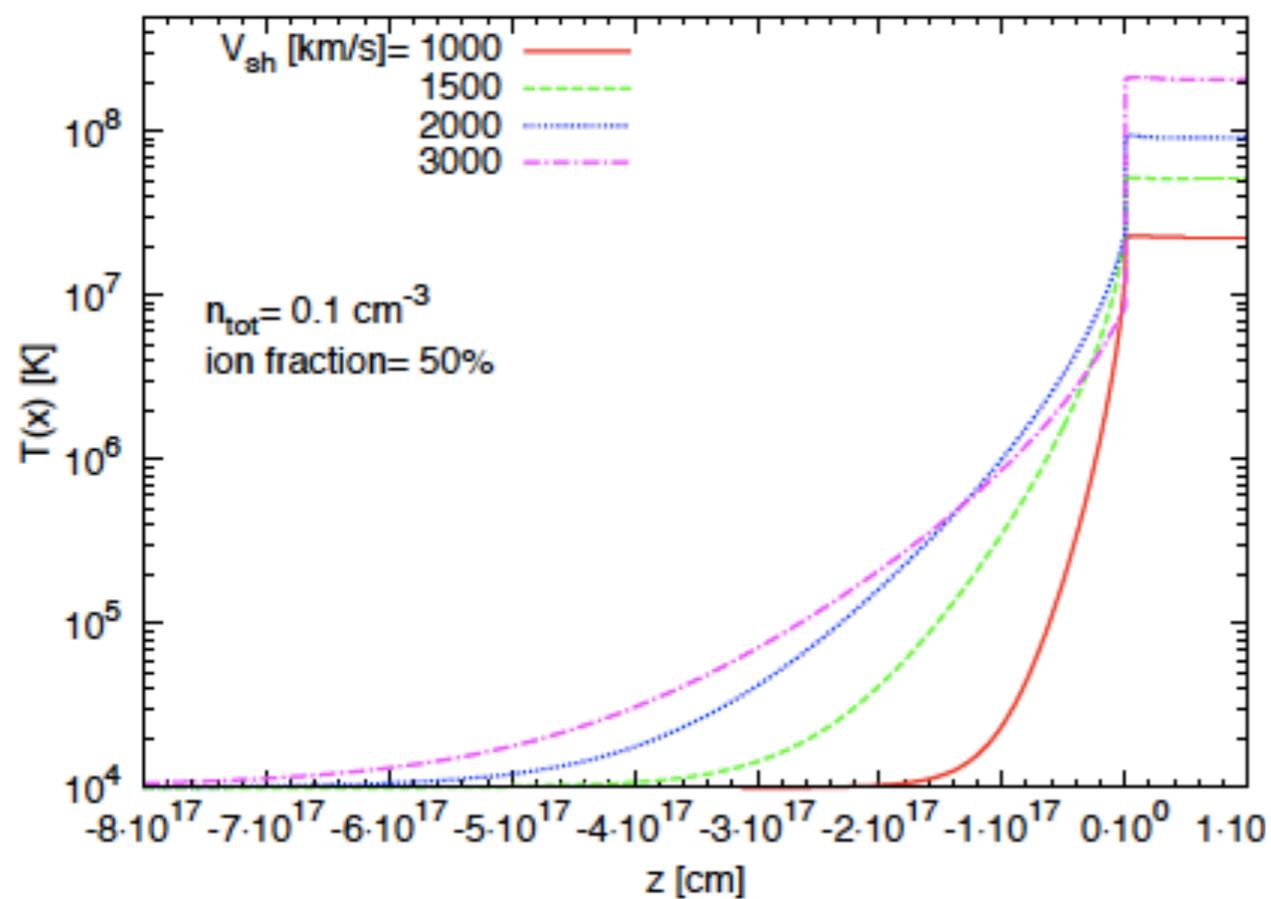
DISTRIBUTION FUNCTIONS IN PHASE SPACE

PB+ 2012



THE DISTRIBUTION FUNCTIONS OF NEUTRALS ARE NOT MAXWELLIAN IN SHAPE THOUGH THEY APPROACH A MAXWELLIAN AT DOWNSTREAM INFINITY

NEUTRAL INDUCED PRECURSOR

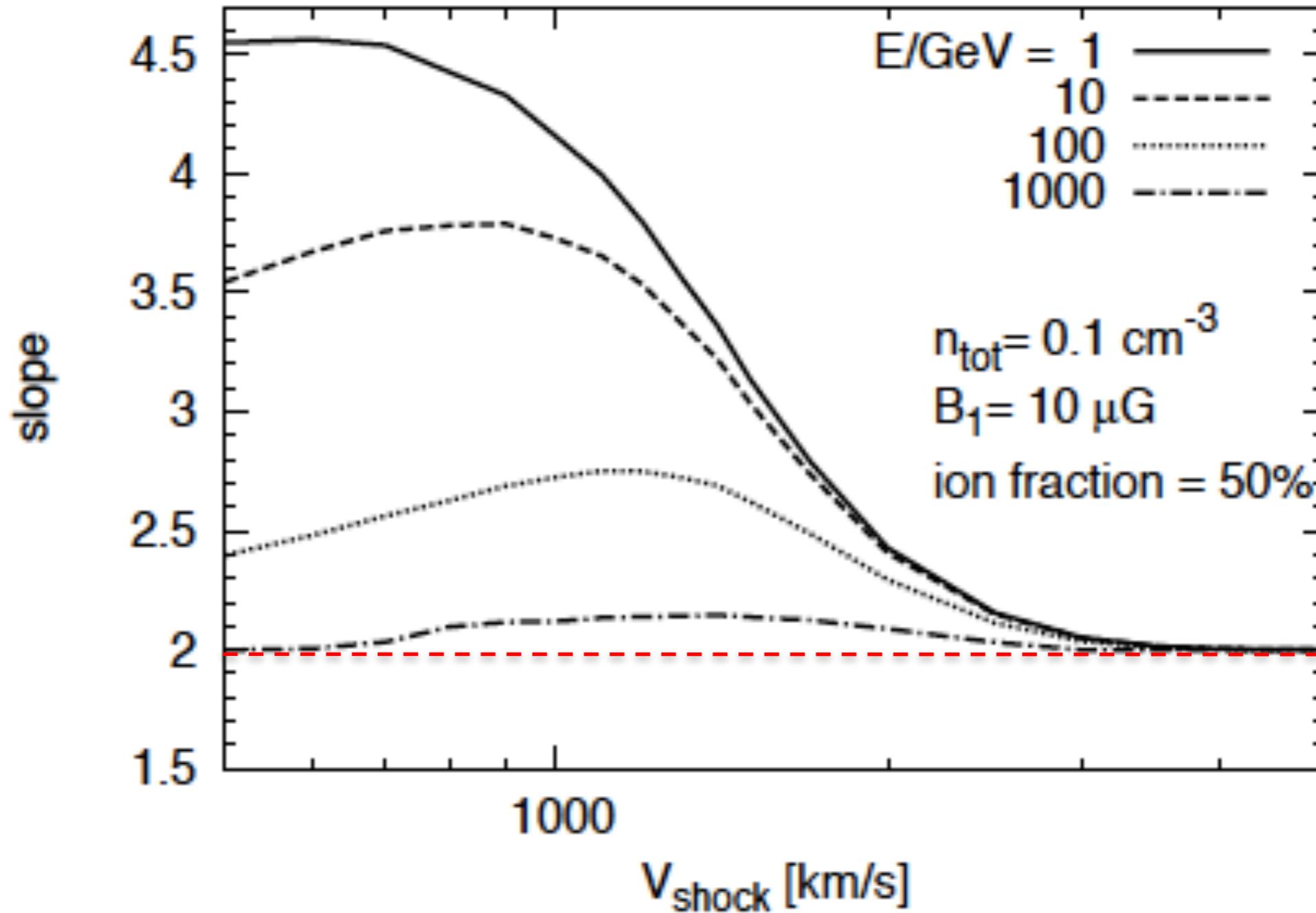


PB+ 2012

EVEN FOR A STRONG SHOCK ($M \gg 1$) THE EFFECTIVE MACH NUMBER OF THE PLASMA IS DRAMATICALLY REDUCED DUE TO THE ACTION OF THE NEUTRAL RETURN FLUX

ACCELERATION OF TEST PARTICLES

PB+ 2012



NON LINEAR CR ACCELERATION IN PARTIALLY IONIZED PLASMAS

$$v_z \frac{\partial f_N}{\partial z} = f_i \beta_N - f_N \beta_i$$

BOLTZMANN EQUATION FOR NEUTRALS

$$\frac{\partial}{\partial z} \left[D(z, p) \frac{\partial f_{CR}}{\partial z} \right] - u \frac{\partial f_{CR}}{\partial z} + \frac{1}{3} \frac{du}{dz} p \frac{\partial f_{CR}}{\partial p} = 0$$

NON LINEAR CR TRANSPORT EQ.

$$\frac{\partial}{\partial z} \left[\rho_i u_i + F_{mass} \right] = 0$$

$$\frac{\partial}{\partial z} \left[\rho_i u_i^2 + P_i + P_{CR} + F_{mom} \right] = 0$$

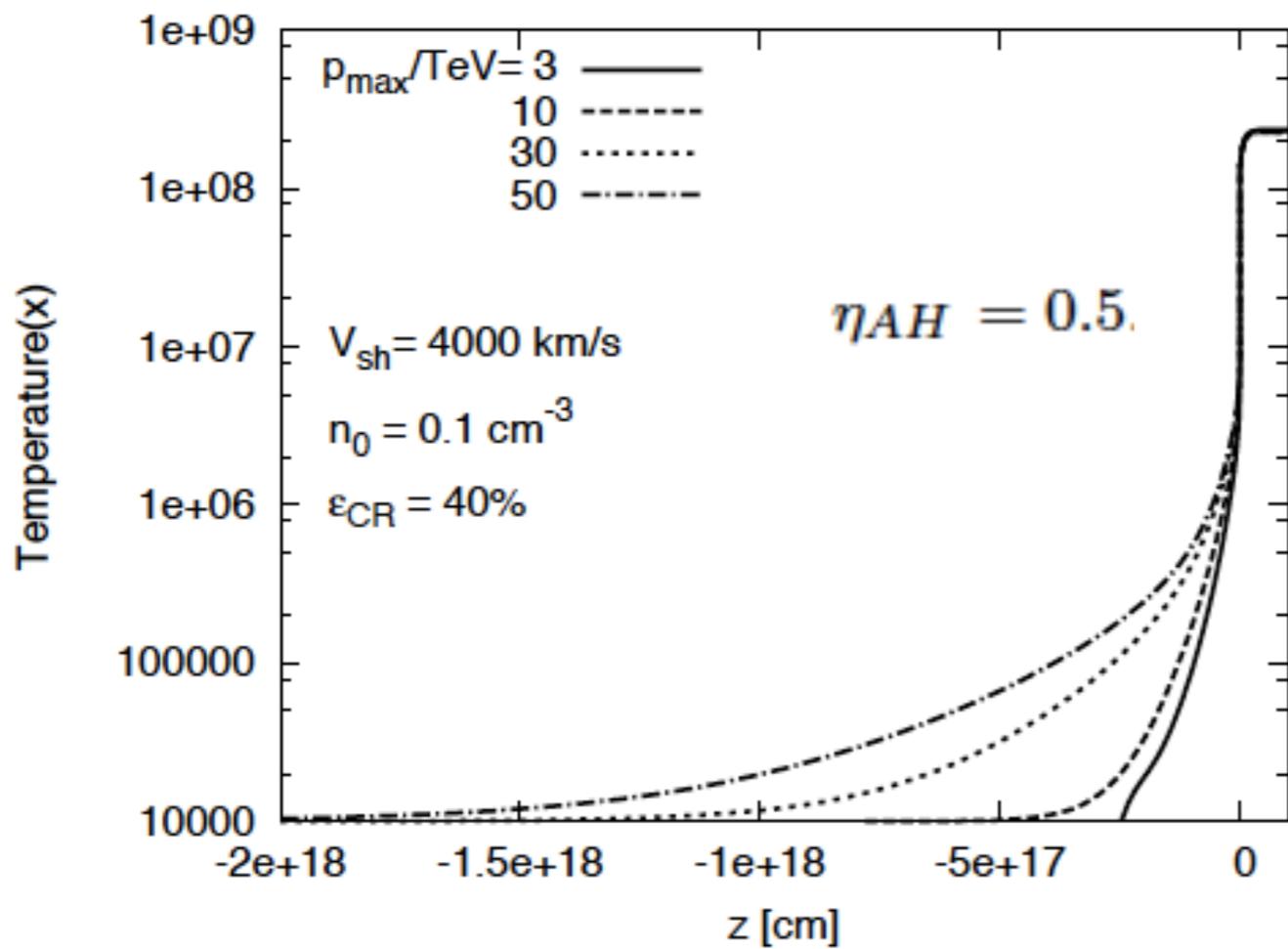
$$\frac{\partial}{\partial z} \left[\frac{1}{2} \rho_i u_i^3 + \frac{\gamma}{\gamma-1} P_i u_i + F_{en} \right] = -u \frac{\partial P_{CR}}{\partial z}$$

$$\frac{\partial F_w}{\partial z} = u \frac{\partial P_w}{\partial z} + P_w \left[\sigma_{CR}(k, z) - \Gamma(k, z) \right]$$

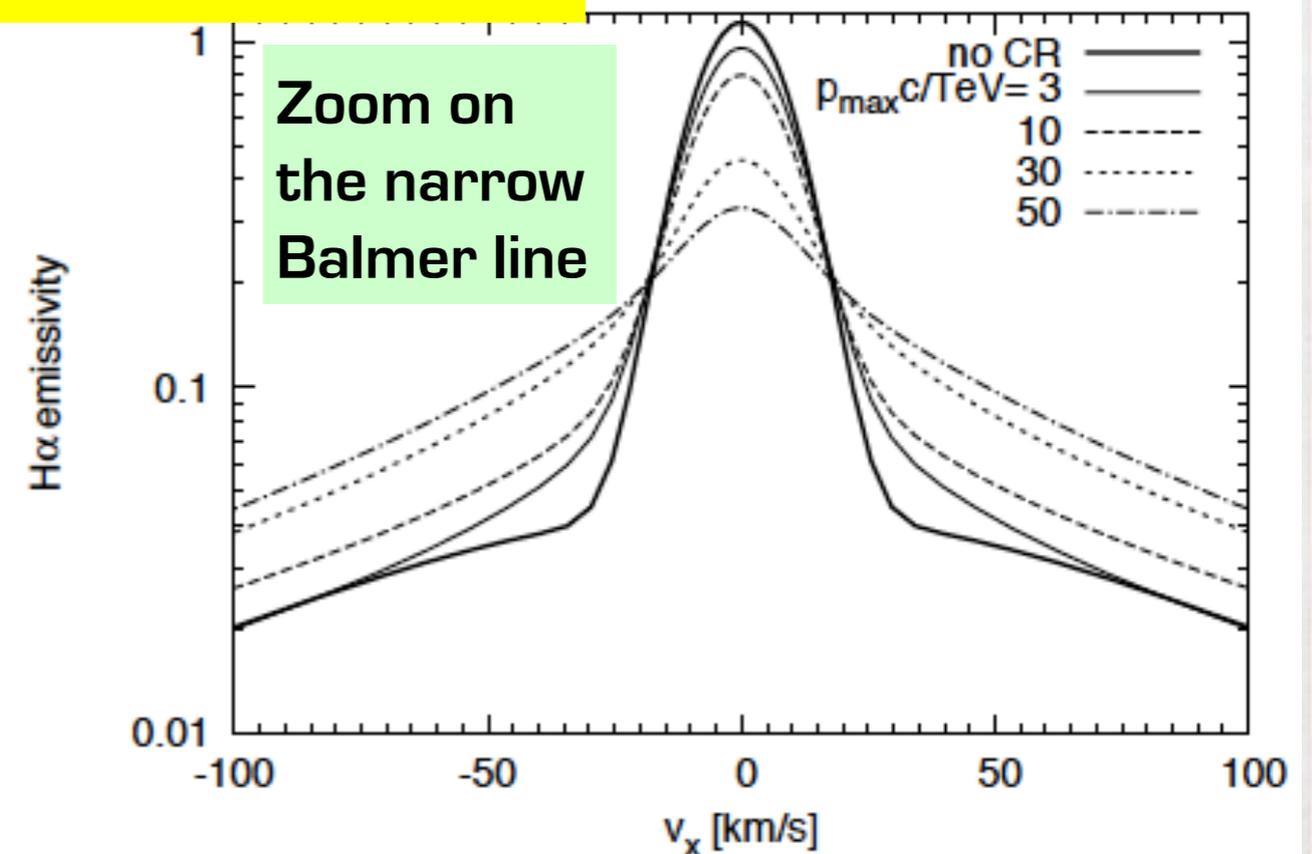
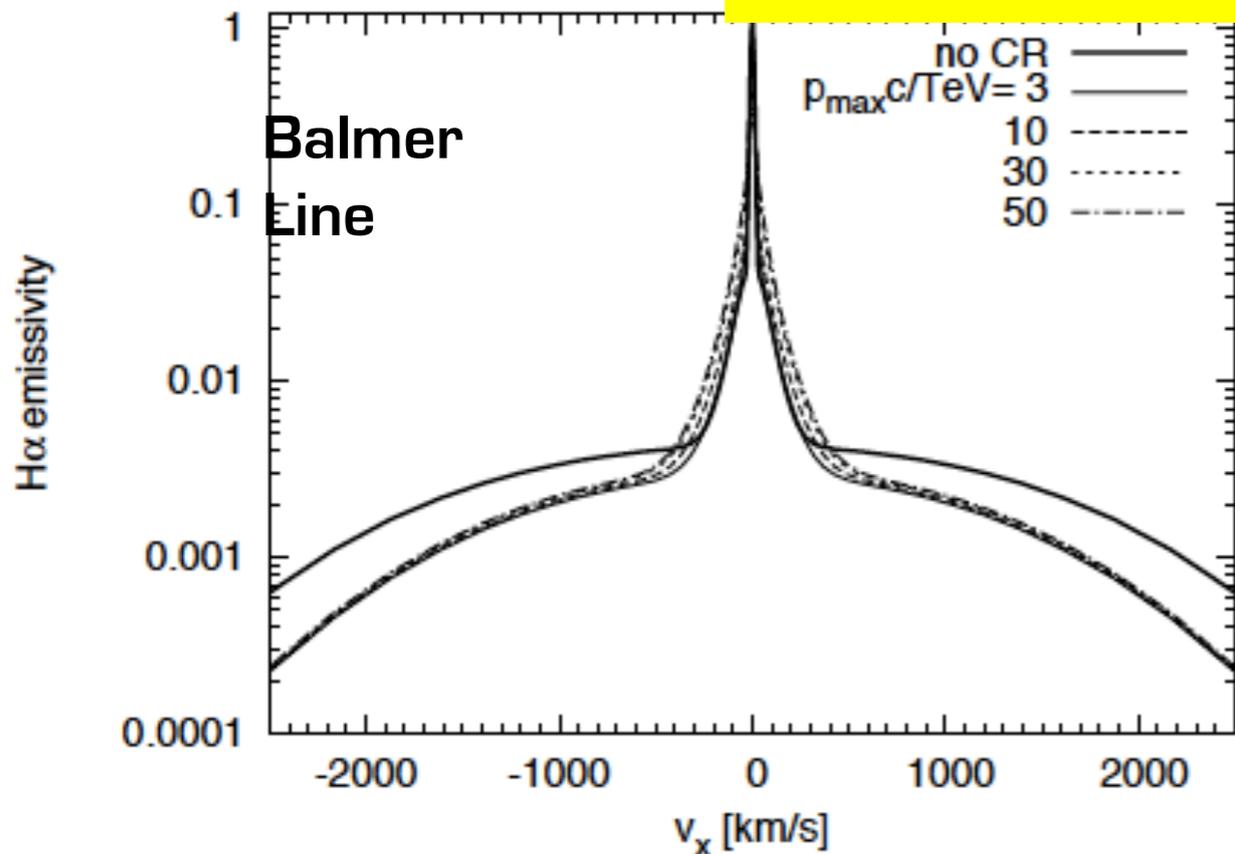
TRANSPORT OF WAVES

GENERALIZED CONSERVATION EQUATIONS

HEATING IN THE PRECURSOR



SHAPE OF THE BALMER LINE

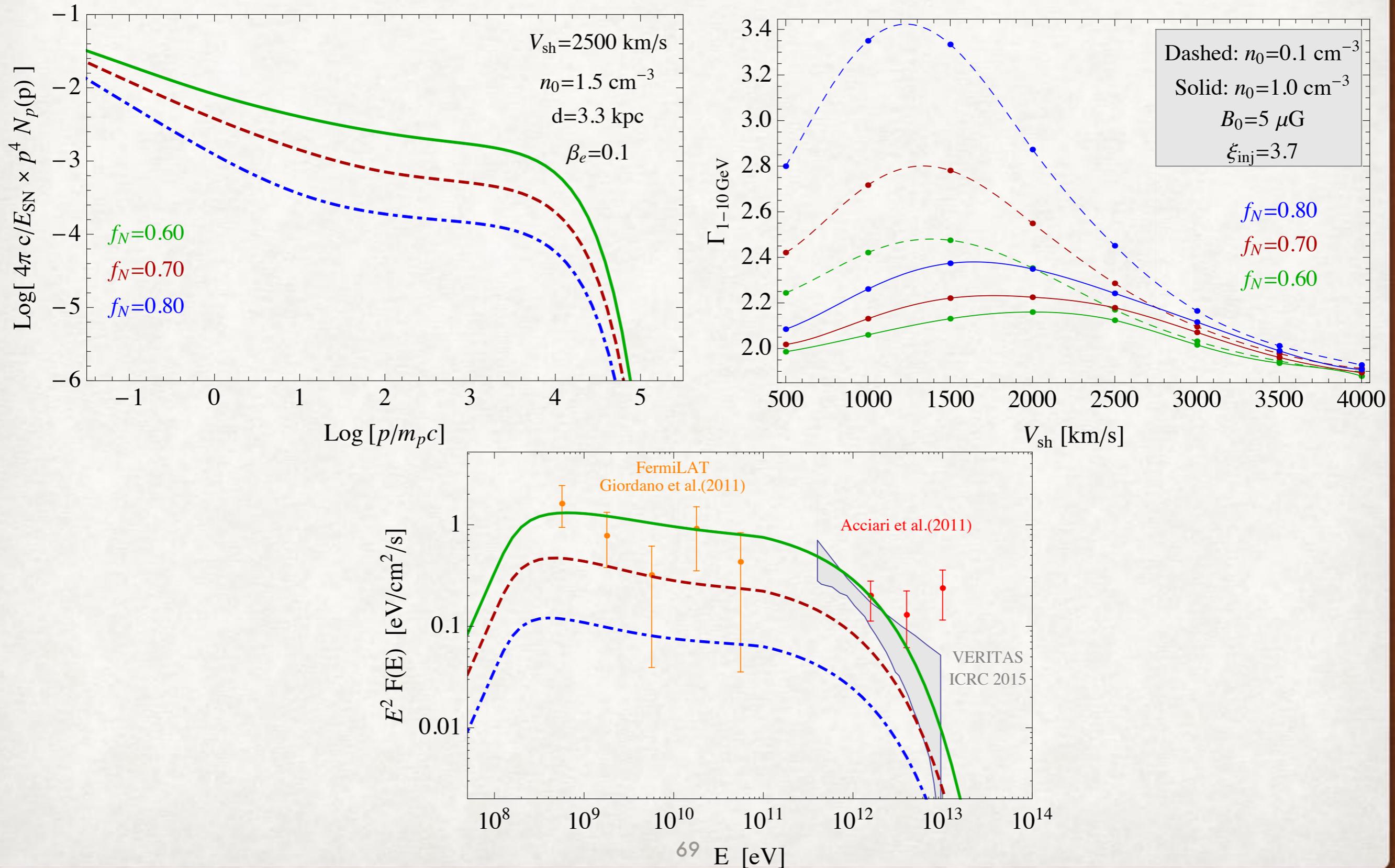


MAIN IMPLICATIONS OF CR + NEUTRALS

- ☑ THE UPSTREAM PLASMA IS HEATED BY BOTH THE NEUTRAL RETURN FLUX AND TURBULENT HEATING INDUCED BY CR
- ☑ TURBULENT HEATING OCCURS ON THE SCALE OF THE PRECURSOR WHICH IS IN GENERAL LARGER THAN THE NEUTRAL PRECURSOR
- ☑ THE NARROW BALMER LINE IS AFFECTED BY TURBULENT HEATING AND BROADENS
- ☑ AN INTERMEDIATE COMPONENT OF THE BALMER LINE IS CREATED AS A RESULT OF CHARGE EXCHANGE IN THE NEUTRAL INDUCED PRECURSOR
- ☑ THE BROAD BALMER LINE GETS NARROWER AS A RESULT OF THE NON LINEAR CR FEEDBACK

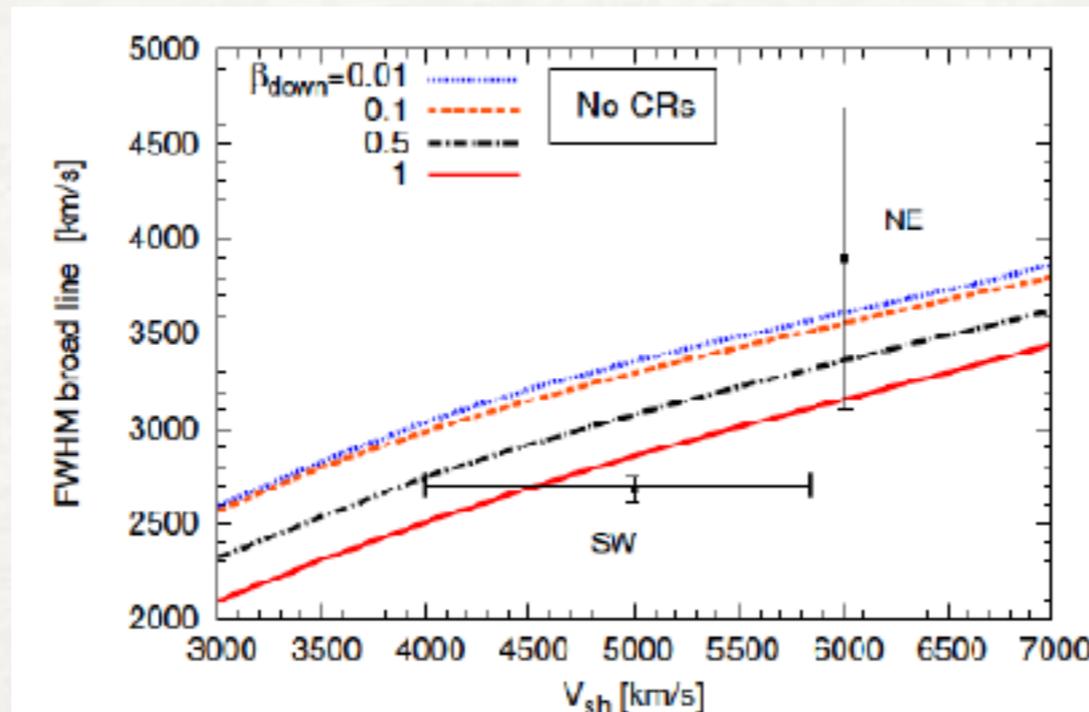
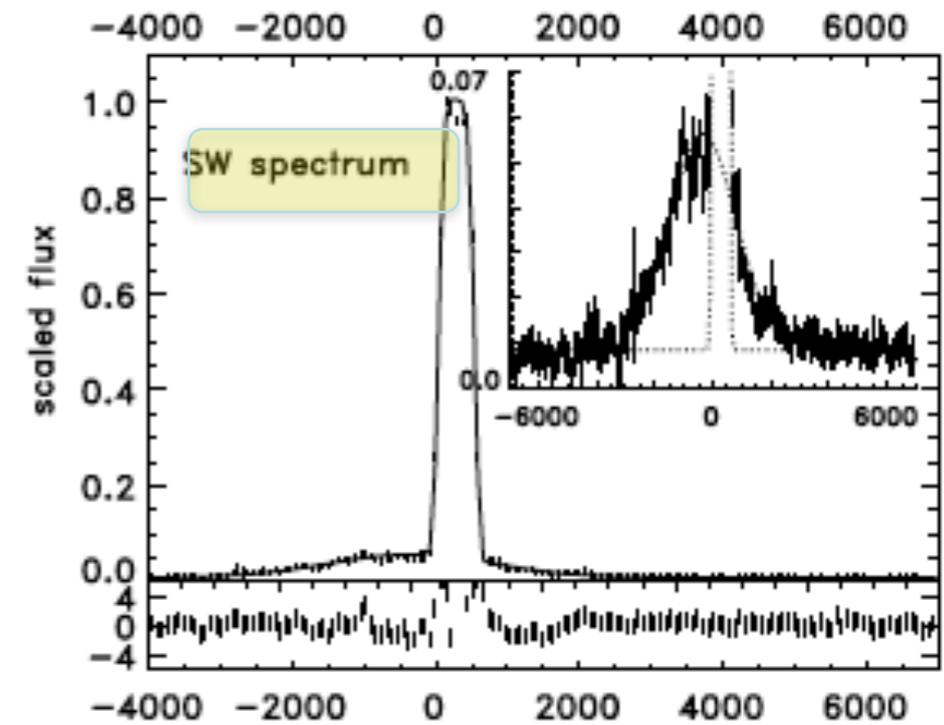
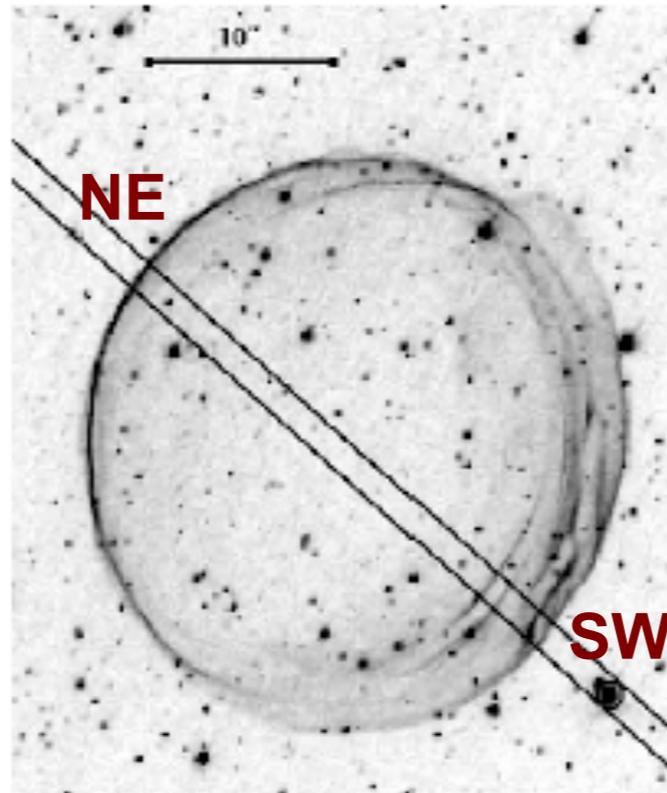
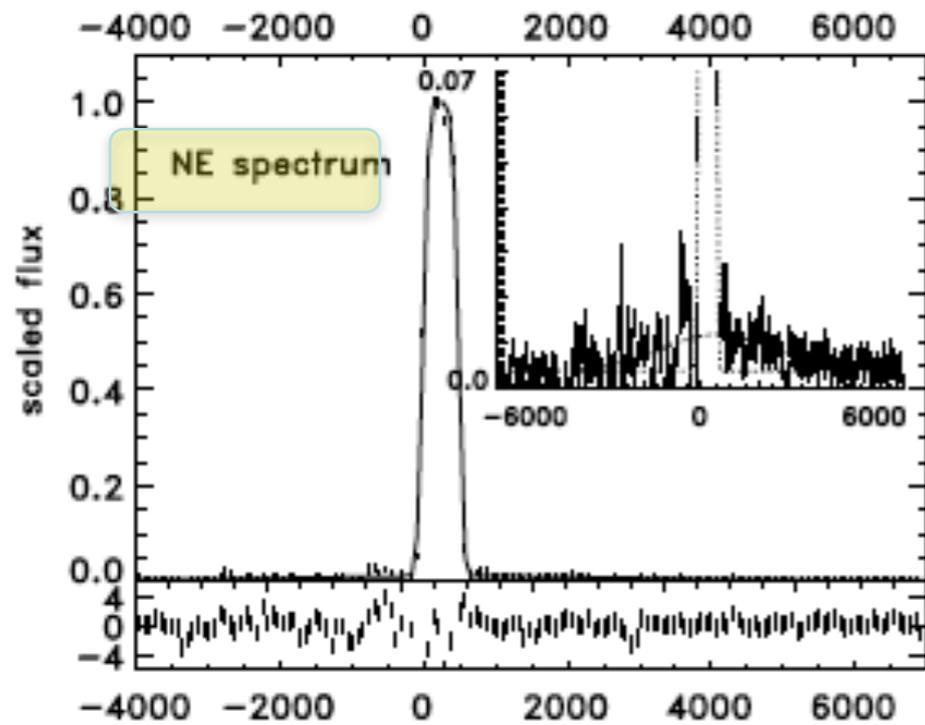
TYCHO: AN INSTANCE OF DSA WITH NEUTRALS

MORLINO & PB 2016



SNR 0509-67.5

Helder et al. 2009

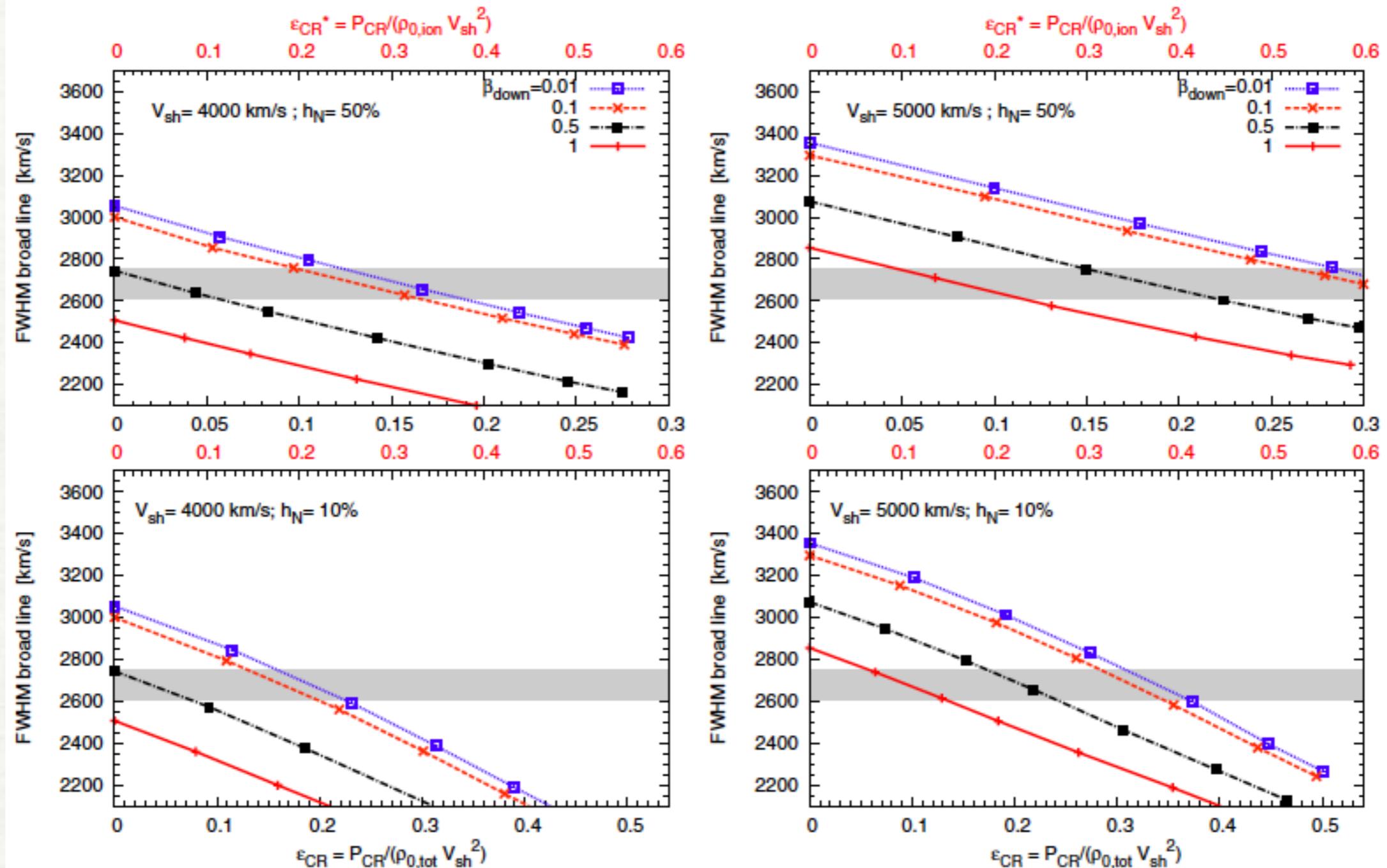


Morlino et al. 2013

SHOCK VELOCITY RATHER
UNCERTAIN

DISTANCE WELL KNOWN
(LMC): 50 ± 1 kpc

SNR 0509-67.5

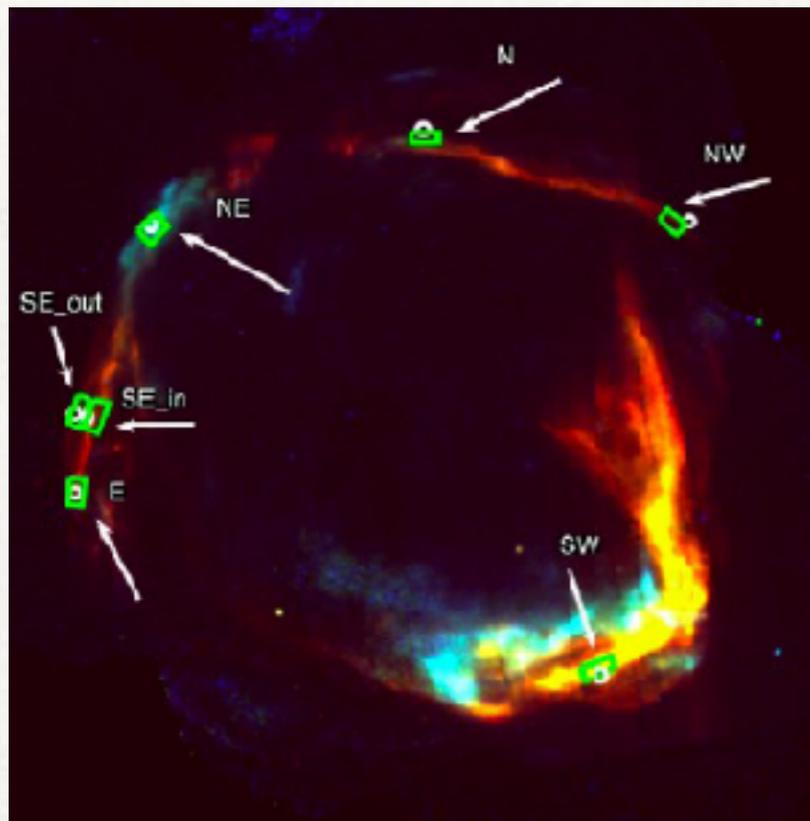


Morlino et al. 2013

FOR SHOCK VELOCITY ~ 5000 km/s A LOWER LIMIT OF 5-10% TO THE CR ACCELERATION EFFICIENCY CAN BE IMPOSED

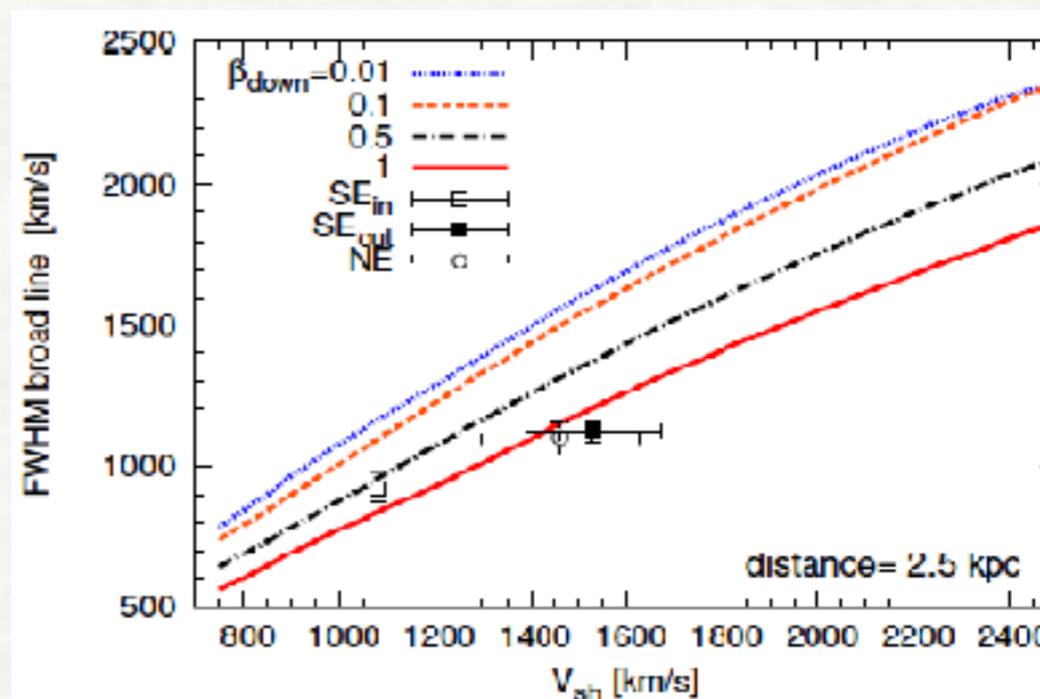
RCW 86

Helder, Vink and Bassa 2011



- Balmer line + proper motion
- Thermal X-ray spectrum

DISTANCE TO THIS SNR RATHER UNCERTAIN WITH VALUES RANGING FROM 2 TO 3 kpc, WITH MOST LIKELY VALUE OF 2.5 kpc

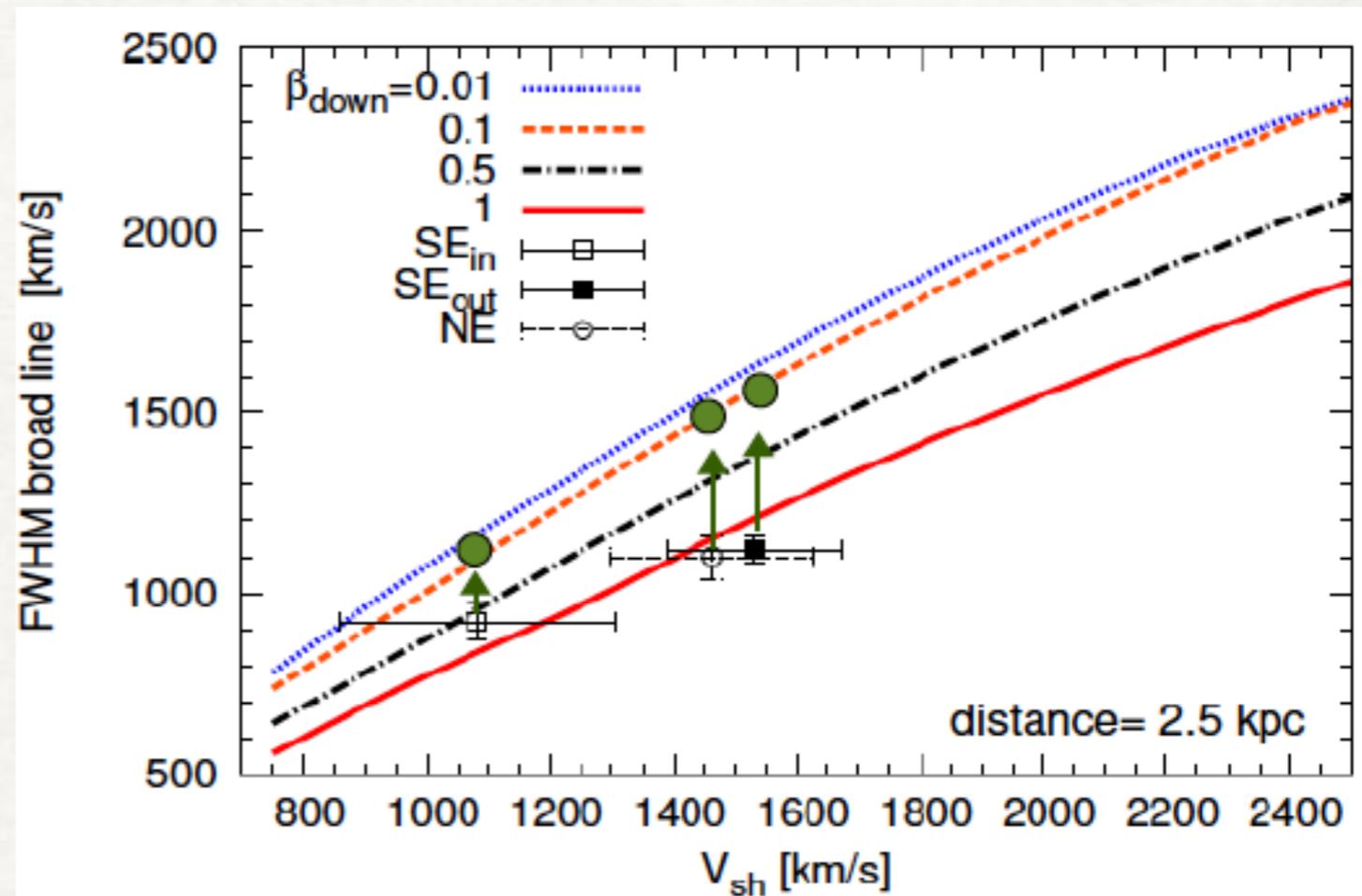
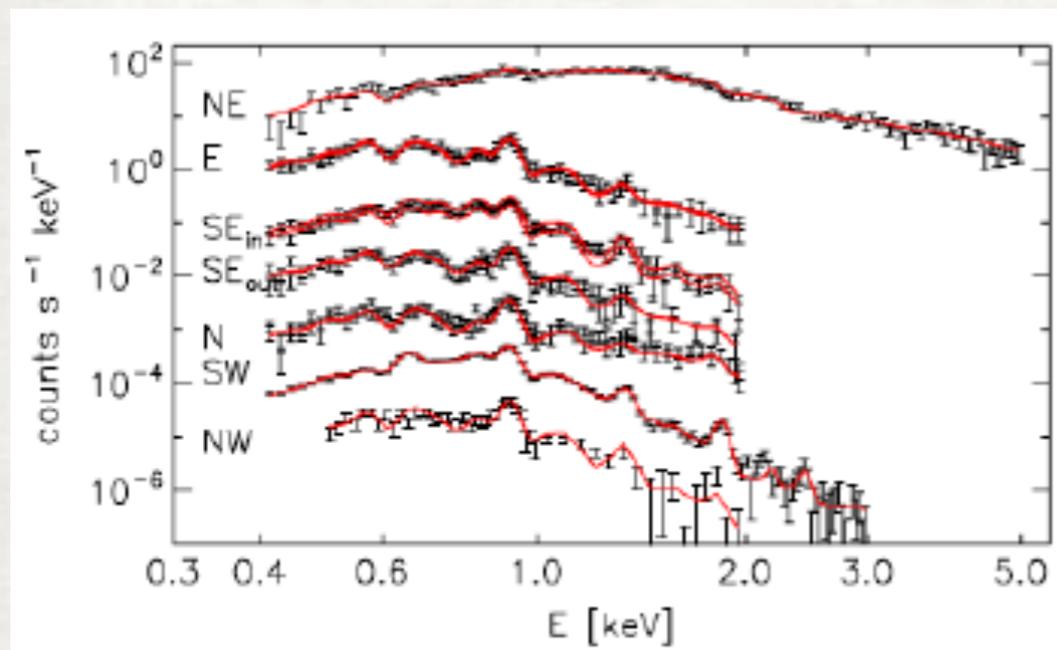


IN THE ABSENCE OF INDEPENDENT INFORMATION ON THE ELECTRON-ION EQUILIBRATION, THE BALMER LINE WIDTH IS COMPATIBLE WITH NO CR ACCELERATION

IN SOME REGIONS HOWEVER THERE ARE X-RAY MEASUREMENTS OF THE ELECTRON TEMPERATURE

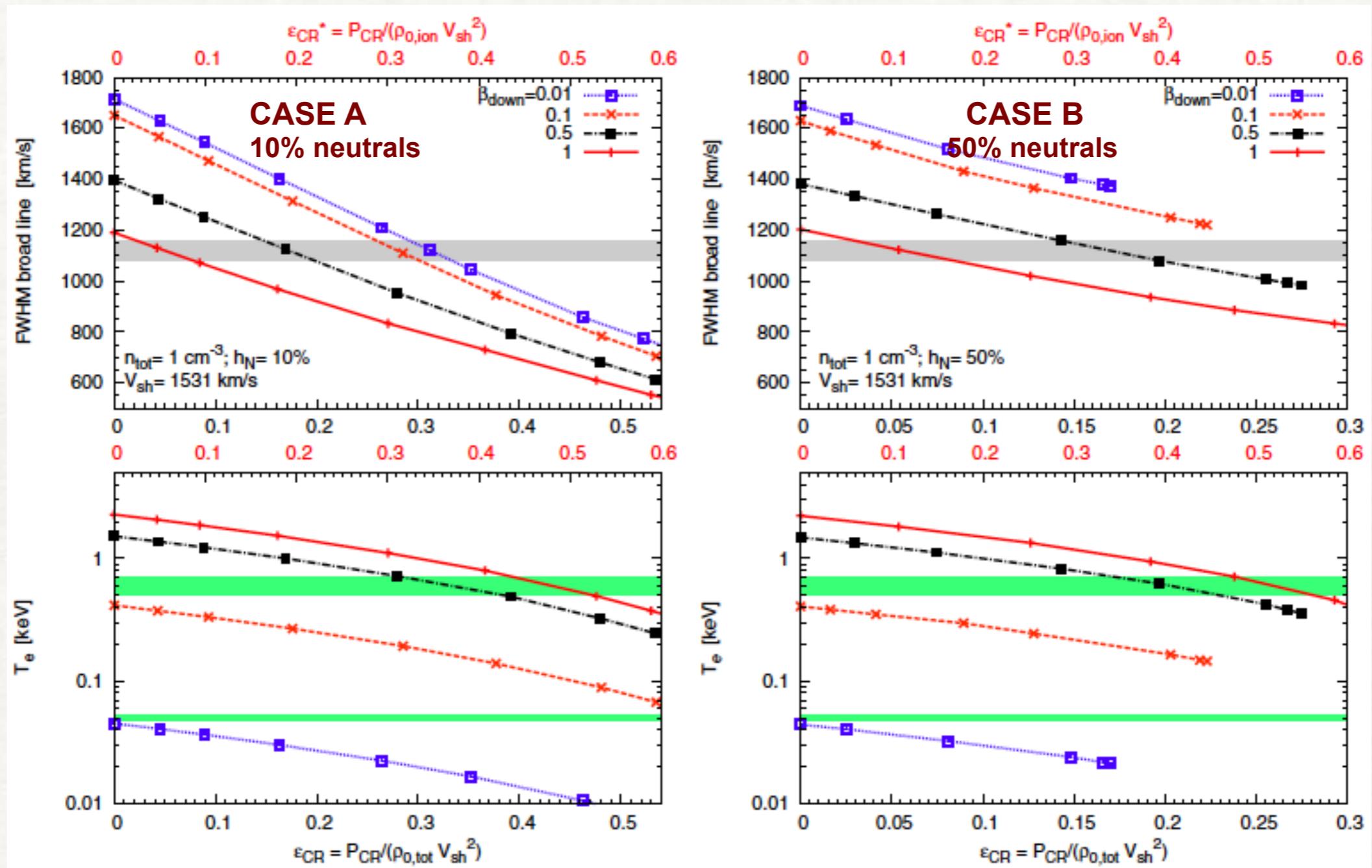
RCW 86

	NE	SE _{in}	SE _{out}
T_e (keV)	37^{+29}_{-19}	0.9 ± 0.1	0.6 ± 0.1



IF THE MEASURED ELECTRON TEMPERATURE IS THE ACTUAL T_e DOWNSTREAM, THEN ALL MEASURED FWHM OF THE BROAD BALMER LINE SUGGEST EFFICIENT CR ACCELERATION

RCW 86 – FILAMENT SE_{OUT}



A NON THERMAL PRESSURE OF ABOUT 20-30% IS REQUIRED TO EXPLAIN AT THE SAME TIME THE FWHM OF THE BALMER LINE AND THE VALUE OF T_e