# The physics and astrophysics of merging neutron-star binaries

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#### Outline

• the irresistible "attraction" of gravity

beauty and challenges of general relativity

• neutron stars: Einstein's richest laboratory

binary mergers:

gravitational waves, gamma-ray bursts, nucleosynthesis,...

\* Instinctive notion



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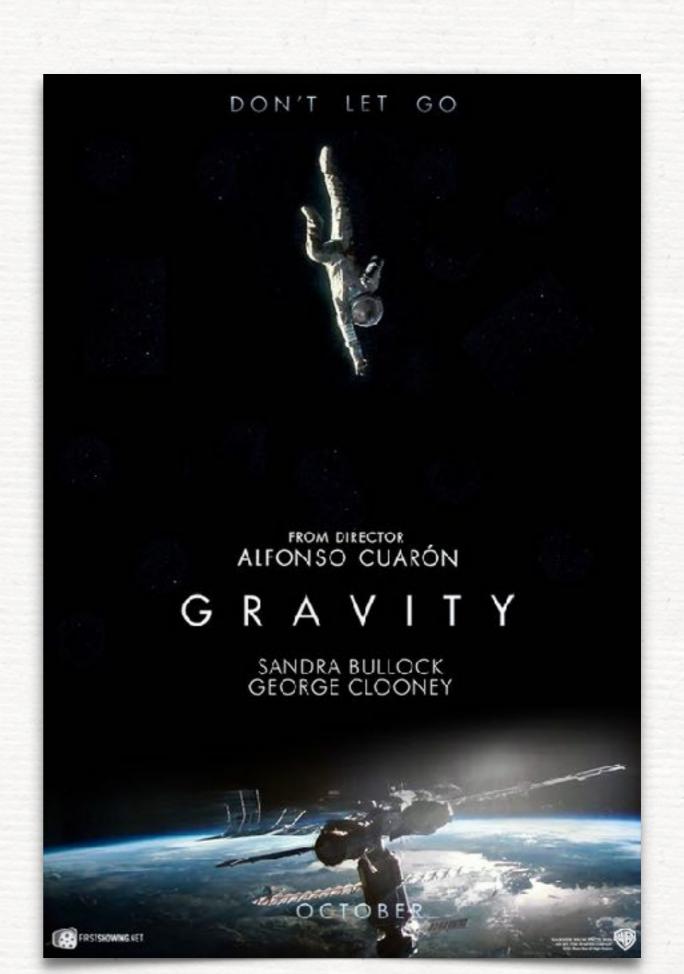
\* Intuitive notion



\* Instinctive notion

\* Intuitive notion

\* Imaginative notion

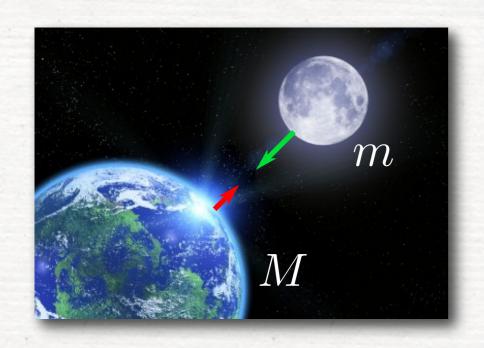


#### The fathers of gravity

In 1679 Newton publishes his theory of gravity.

Gravity is an instantaneous **force** between two masses proportional to the masses and inversely proportional to to the square of the distance.





$$ec{m{F}} = -rac{G}{c^2}rac{Mm}{r^2}ec{m{e_r}}$$

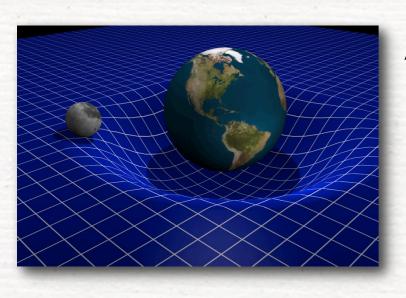
With this theory he could explain essentially all astronomical observations of his time.

#### The fathers of gravity

In 1915 Einstein publishes his theory of gravity (Allgemeine Relativitätstheorie) changing our understanding of gravity.

According to Einstein, gravity is the manifestation of spacetime curvature.

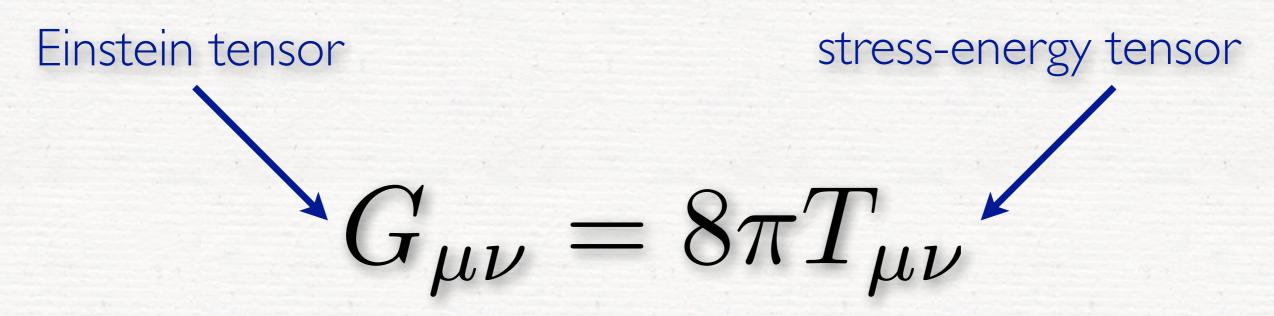


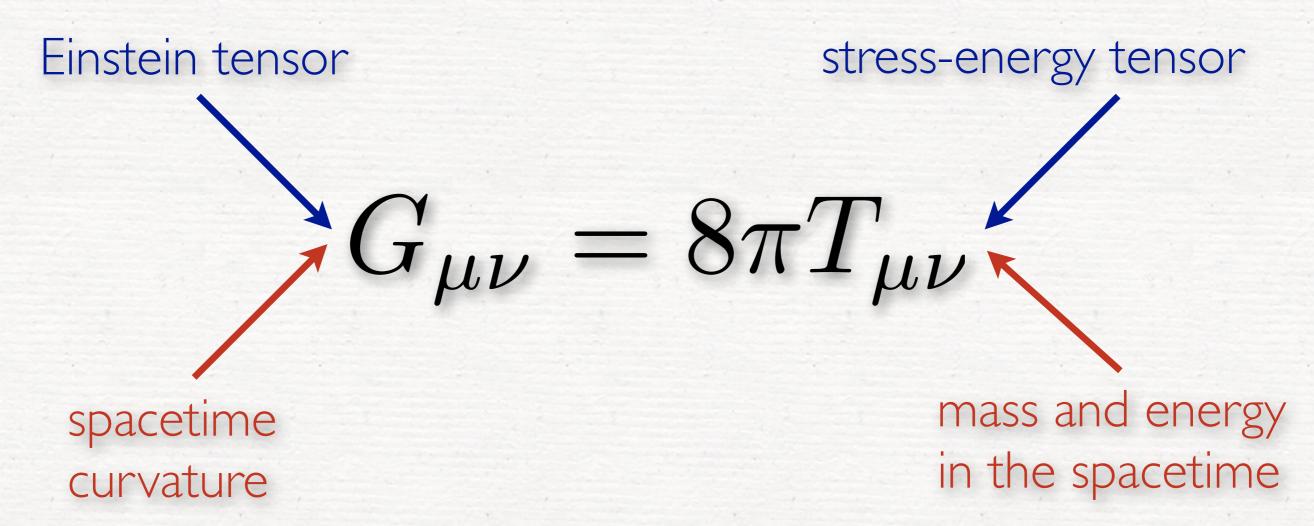


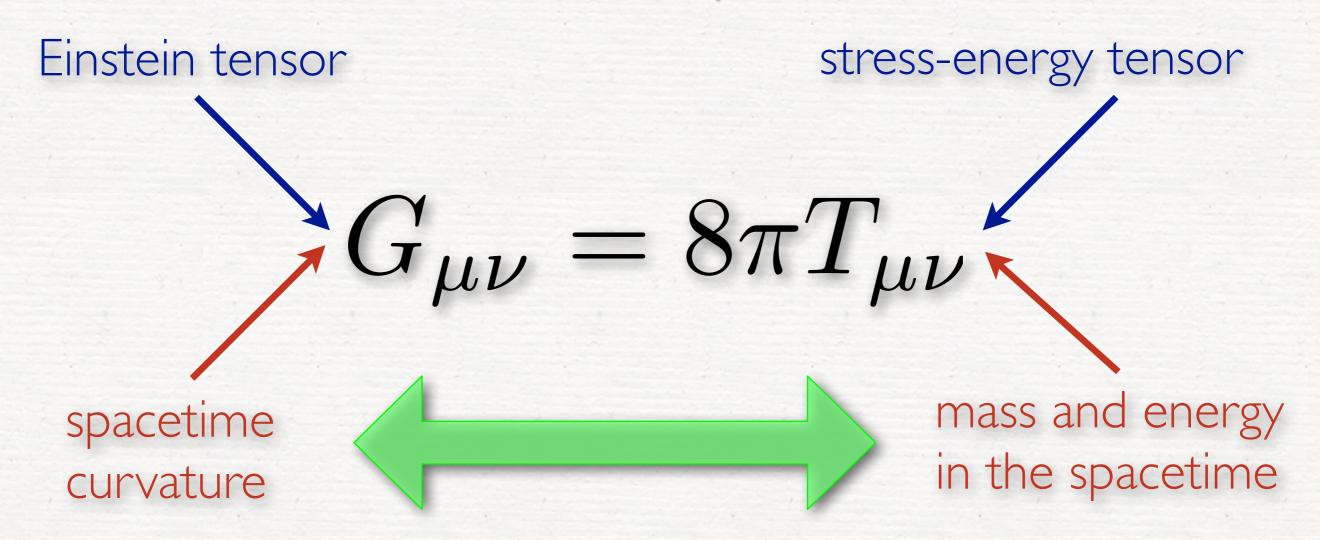
Any form of mass/energy curves the spacetime.

Implications of this view are: black holes, neutron stars, gravitational waves.

$$G_{\mu\nu} = 8\pi T_{\mu\nu}$$



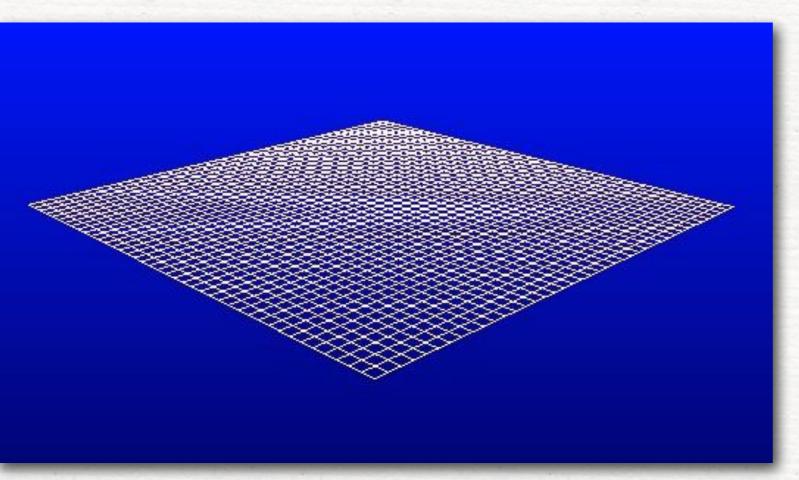




There is a relation between the curvature and mass/energy.
gravity is the manifestation of spacetime curvature

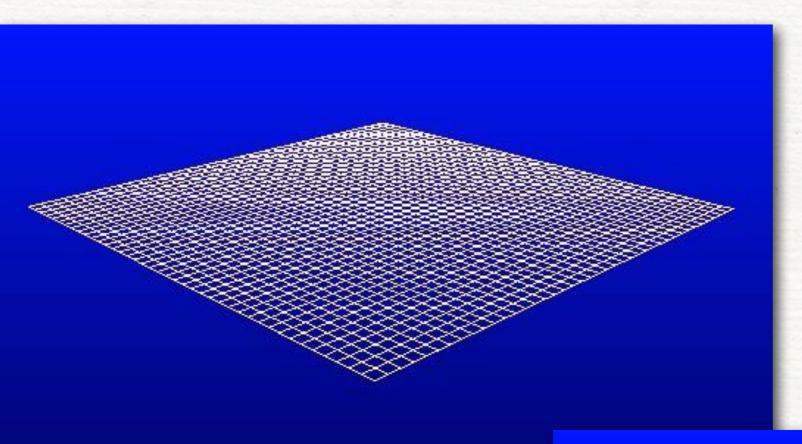
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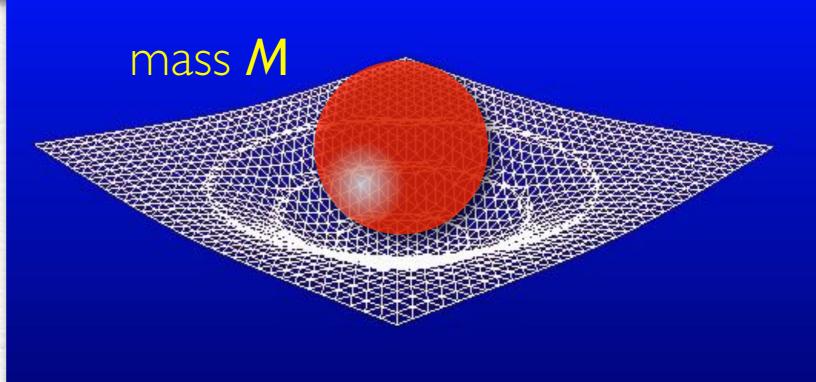
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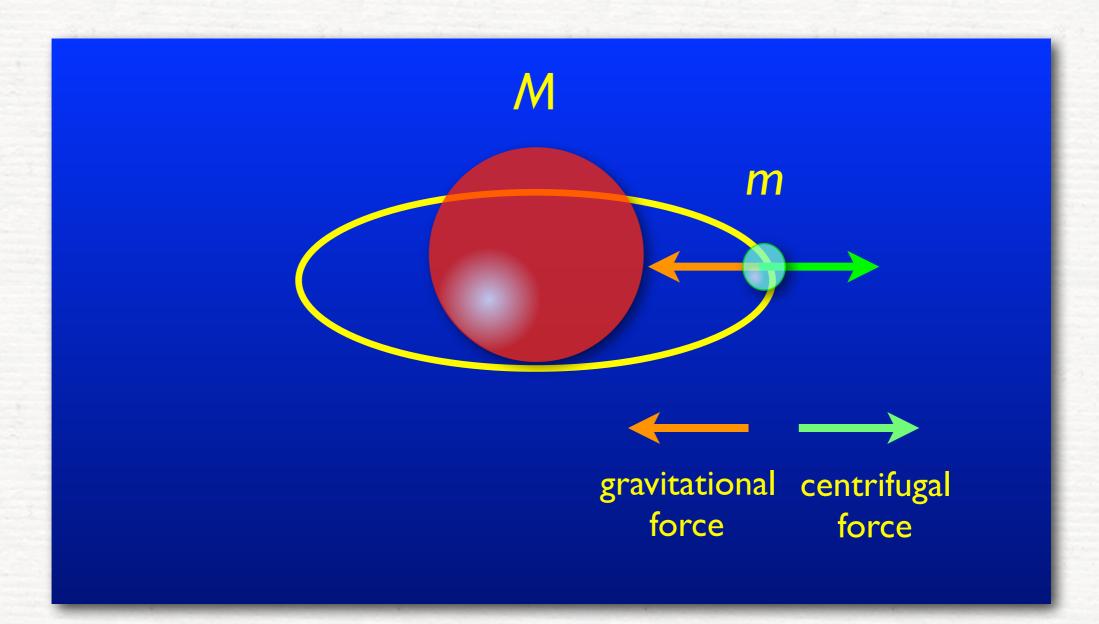
If instead it contains a mass M, it will have a nonzero curvature and will therefore be a curved spacetime



#### Gravity à la Newton

Consider orbital motion of an object of small mass m around an object of large mass M: (e. g., Earth around the Sun)

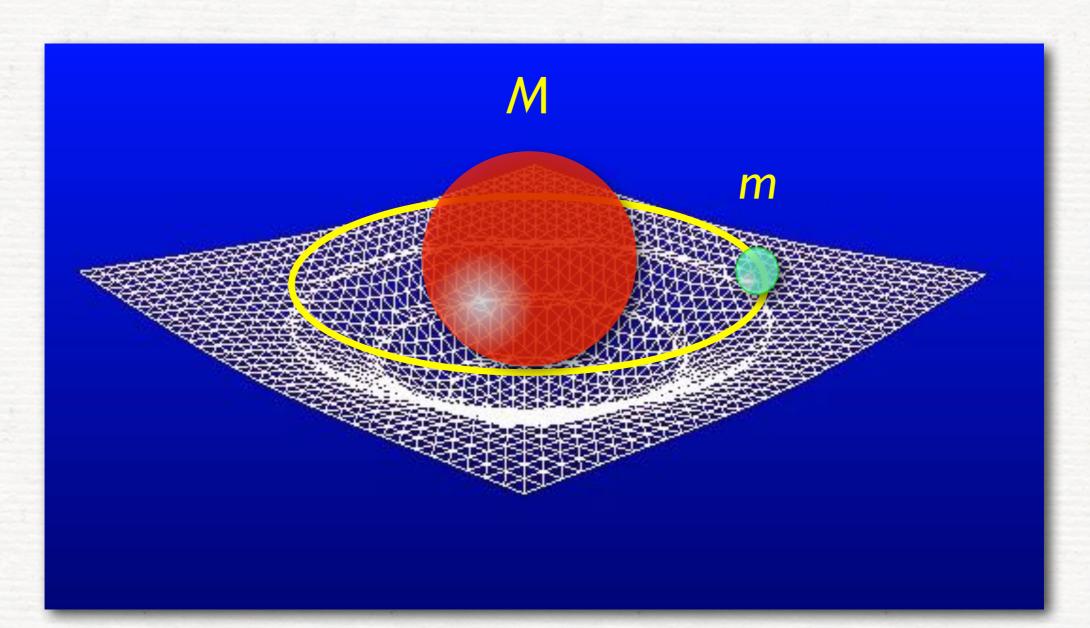
**Newton**: orbit is the balance between the **gravitational force** and the **centrifugal one** 



#### Gravity à la Einstein

Consider orbital motion of an object of small mass m around an object of large mass M: (e. g., Earth around the Sun)

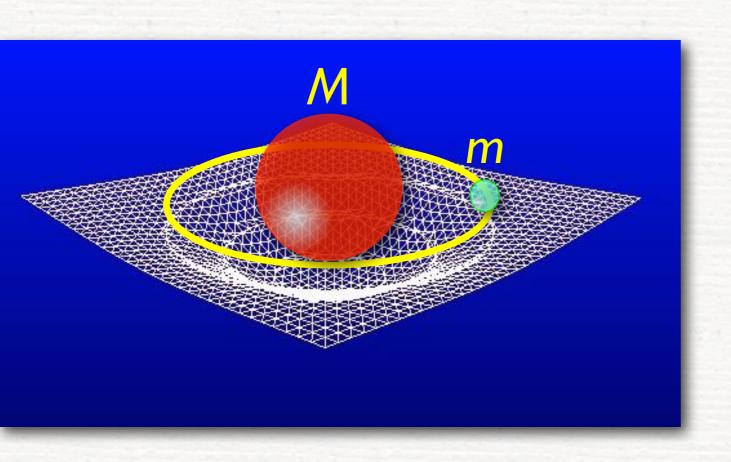
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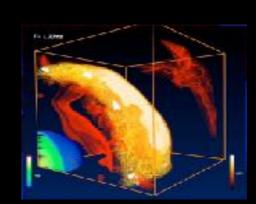
### Black holes, neutron stars and gravitational waves two important common features:

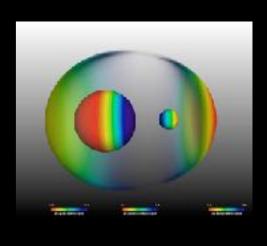
- high curvature (compactness, M/R)
- •move near speed of light

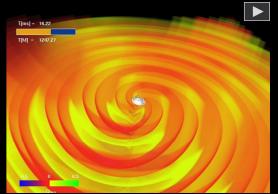
### Black holes, neutron stars and gravitational waves two important common features:

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Studying black holes, neutron stars and gravitational waves is not easy!







Indeed, one needs to solve the full set of Einstein equations together with those of relativistic hydrodynamics/MHD

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$$G_{\mu\nu} = 8\pi T_{\mu\nu}$$

$$\nabla_{\mu} T^{\mu\nu} = 0$$

$$\nabla_{\mu} (\rho u^{\mu}) = 0$$

Hard not to be fascinated by the compact beauty of these equations and by their profound implications.

#### but then reality kicks in...

$$\begin{split} \partial_t \tilde{\gamma}_{ij} &= -2\alpha \tilde{A}^{\mathrm{TF}}_{ij} + 2\tilde{\gamma}_{k(i}\partial_{j)} \, \beta^k - \frac{2}{3}\tilde{\gamma}_{ij}\partial_k \, \beta^k + \beta^k \partial_k \tilde{\gamma}_{ij} \,, \\ \partial_t \tilde{A}_{ij} &= \phi^2 \left[ -\nabla_i \nabla_j \alpha + \alpha \left( R_{ij} + \nabla_i Z_j + \nabla_j Z_i - 8\pi S_{ij} \right) \right]^{\mathrm{TF}} + \alpha \tilde{A}_{ij} \left( K - 2\Theta \right) \\ &\quad - 2\alpha \tilde{A}_{il} \tilde{A}^j_j + 2\tilde{A}_{k(i}\partial_{j)} \, \beta^k - \frac{2}{3}\tilde{A}_{ij}\partial_k \, \beta^k + \beta^k \partial_k \tilde{A}_{ij} \,, \\ \partial_t \phi &= \frac{1}{3}\alpha \phi K - \frac{1}{3}\phi \partial_k \beta^k + \beta^k \partial_k \phi \,, \\ \partial_t K &= -\nabla^i \nabla_i \alpha + \alpha \left( R + 2\nabla_i Z^i + K^2 - 2\Theta K \right) + \beta^j \partial_j K - 3\alpha \kappa_1 \left( 1 + \kappa_2 \right) \Theta + 4\pi \alpha \left( S - 3\tau \right) \,, \\ \partial_t \hat{\Gamma}^i &= 2\alpha \left( \tilde{\Gamma}^i_{jk} \tilde{A}^{jk} - 3\tilde{A}^{ij} \frac{\partial_j \phi}{\phi} - \frac{2}{3}\tilde{\gamma}^{ij} \partial_j K \right) + 2\tilde{\gamma}^{ki} \left( \alpha \partial_k \Theta - \Theta \partial_k \alpha - \frac{2}{3}\alpha K Z_k \right) - 2\tilde{A}^{ij} \partial_j \alpha \\ &\quad + \tilde{\gamma}^{kl} \partial_k \partial_l \beta^i + \frac{1}{3}\tilde{\gamma}^{ik} \partial_k \partial_l \beta^l + \frac{2}{3}\tilde{\Gamma}^i \partial_k \beta^k - \tilde{\Gamma}^k \partial_k \beta^i + 2\kappa_3 \left( \frac{2}{3}\tilde{\gamma}^{ij} Z_j \partial_k \beta^k - \tilde{\gamma}^{jk} Z_j \partial_k \beta^i \right) \\ &\quad + \beta^k \partial_k \hat{\Gamma}^i - 2\alpha \kappa_1 \tilde{\gamma}^{ij} Z_j - 16\pi \alpha \tilde{\gamma}^{ij} S_j \,, \\ \partial_t \Theta &= \frac{1}{2}\alpha \left( R + 2\nabla_i Z^i - \tilde{A}_{ij} \tilde{A}^{ij} + \frac{2}{3} K^2 - 2\Theta K \right) - Z^i \partial_i \alpha + \beta^k \partial_k \Theta - \alpha \kappa_1 \left( 2 + \kappa_2 \right) \Theta - 8\pi \alpha \right. \\ \partial_t \alpha &= -2\alpha \left( K - 2\Theta \right) + \beta^k \partial_k \alpha \,, \\ \partial_t \beta^i &= f B^i + \beta^k \partial_k \beta^i \,, \\ \partial_t B^i &= \partial_t \hat{\Gamma}^i - \beta^k \partial_k \hat{\Gamma}^i + \beta^k \partial_k B^i - \eta B^i \,, \end{split}$$

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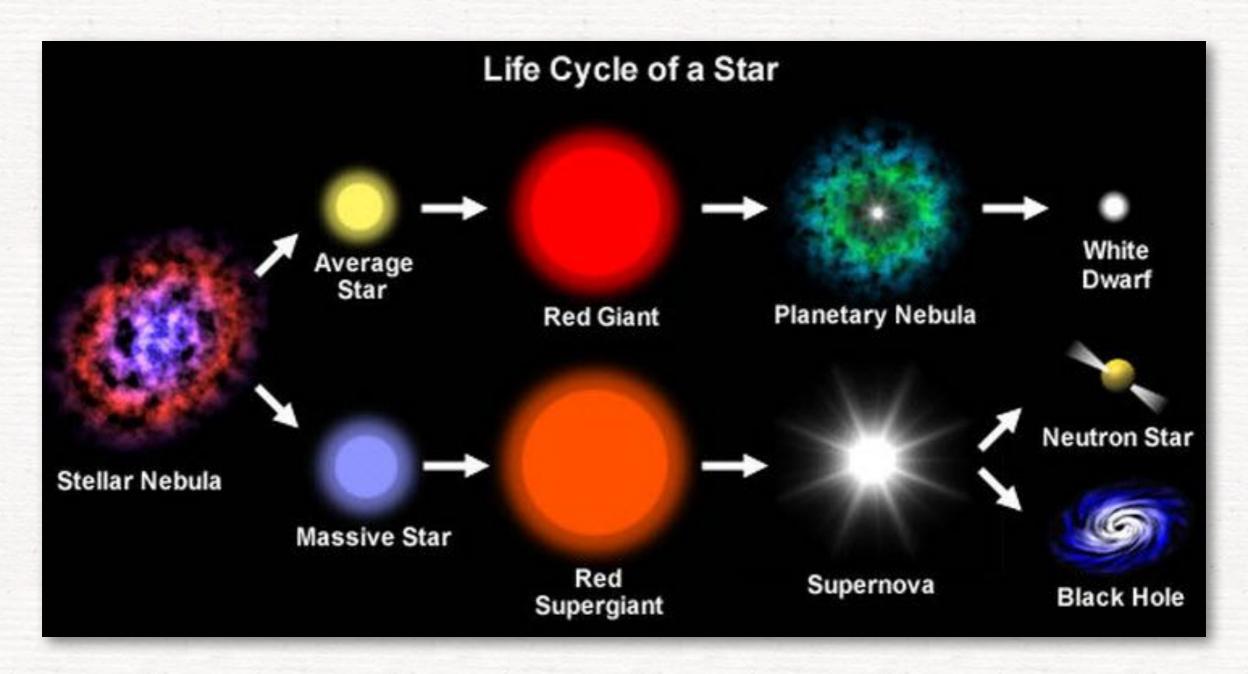
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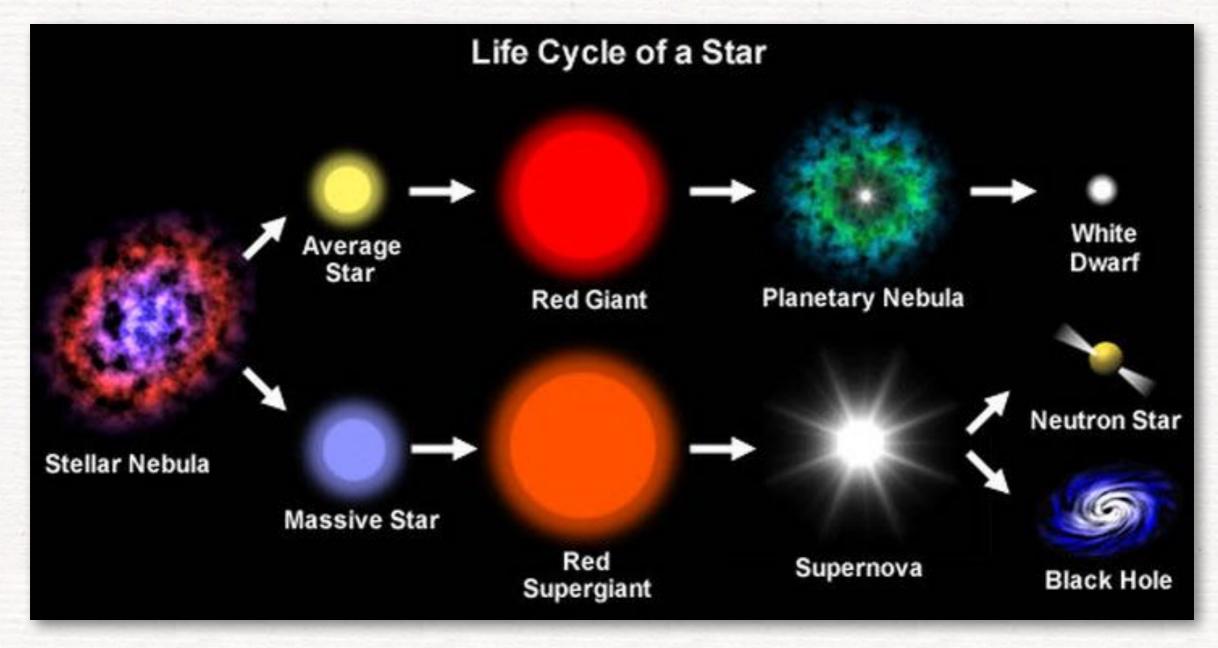
#### Neutron stars



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Neutron stars are the most common end of the evolution of massive stars, ie stars with mass  $10 M_{\odot} \lesssim M \lesssim 100 M_{\odot}$ 

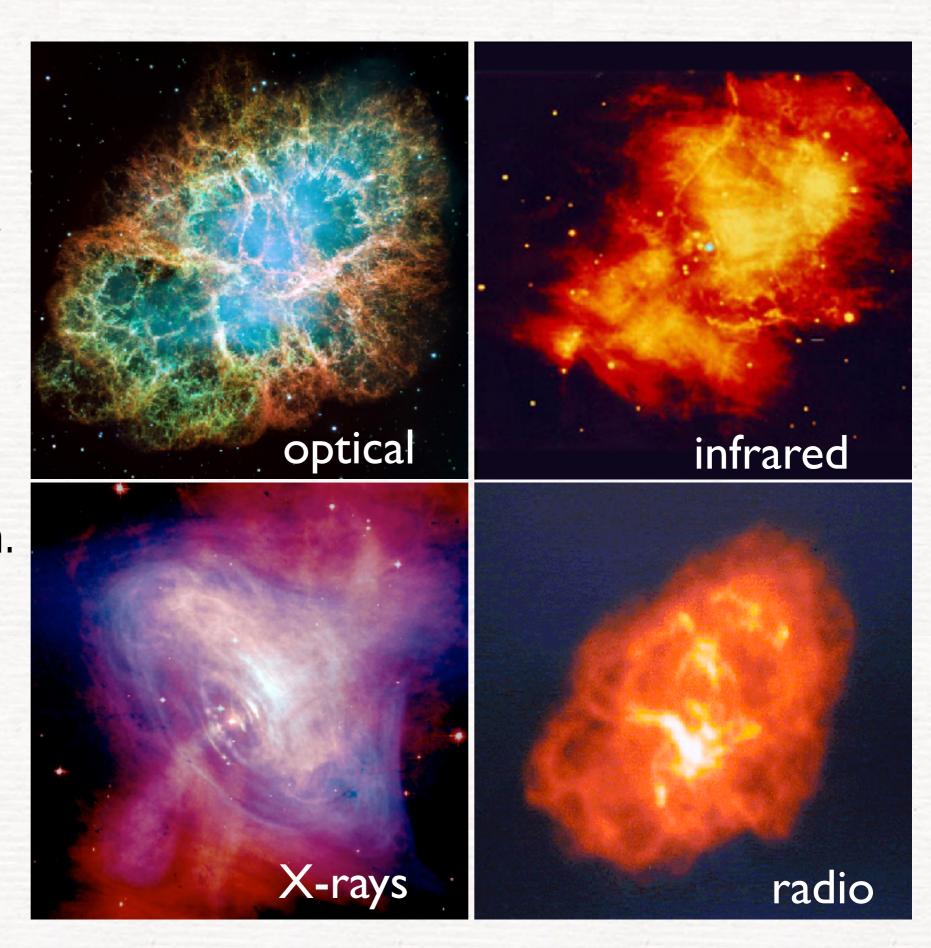
Such stars end their evolution as supernovae

### A beautiful example

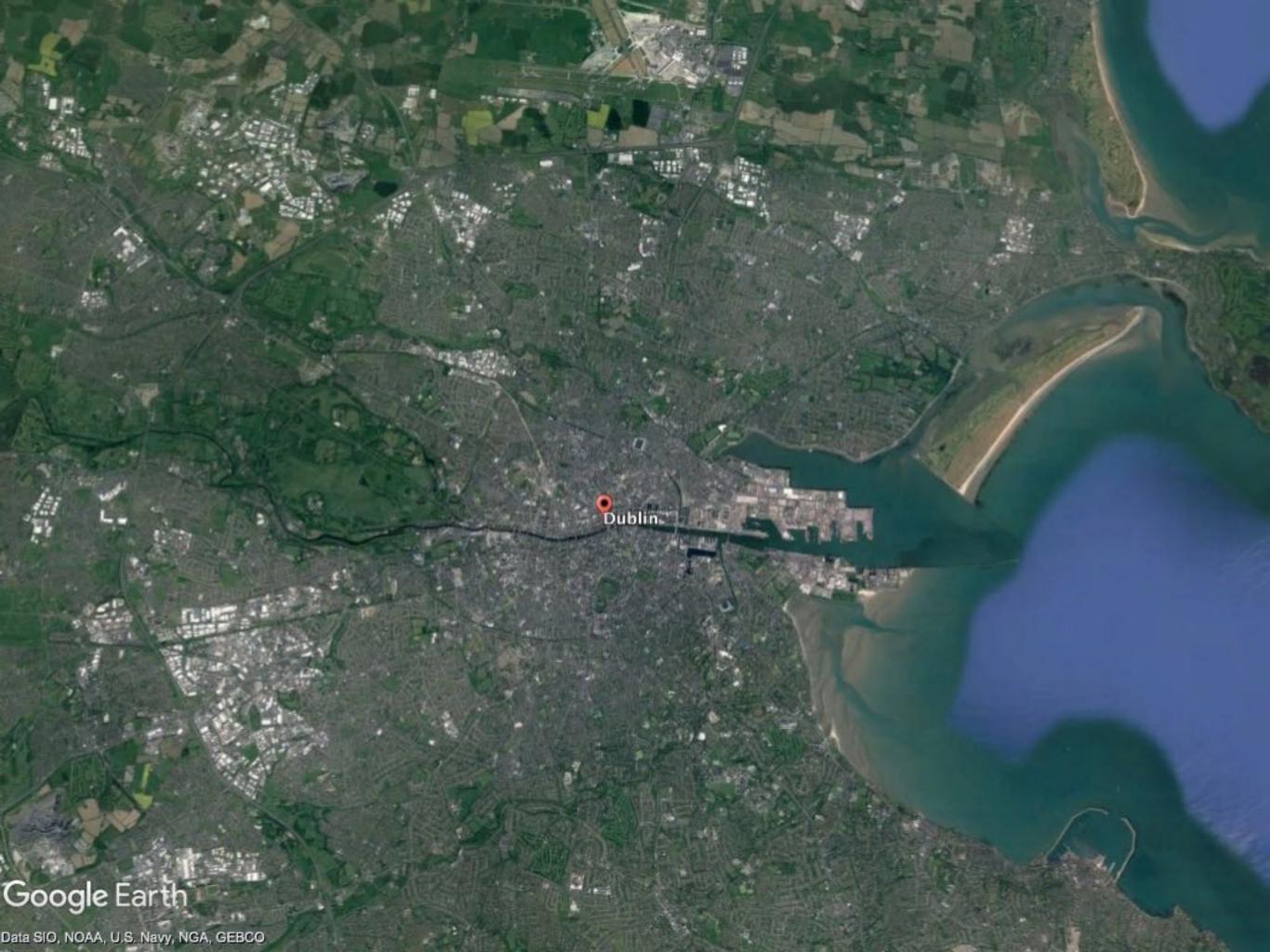
China, 1054 AC: a new star appears in the sky and is visible even in daylight in the Crab constellation.

In reality it was a supernova that had produced a neutron star:

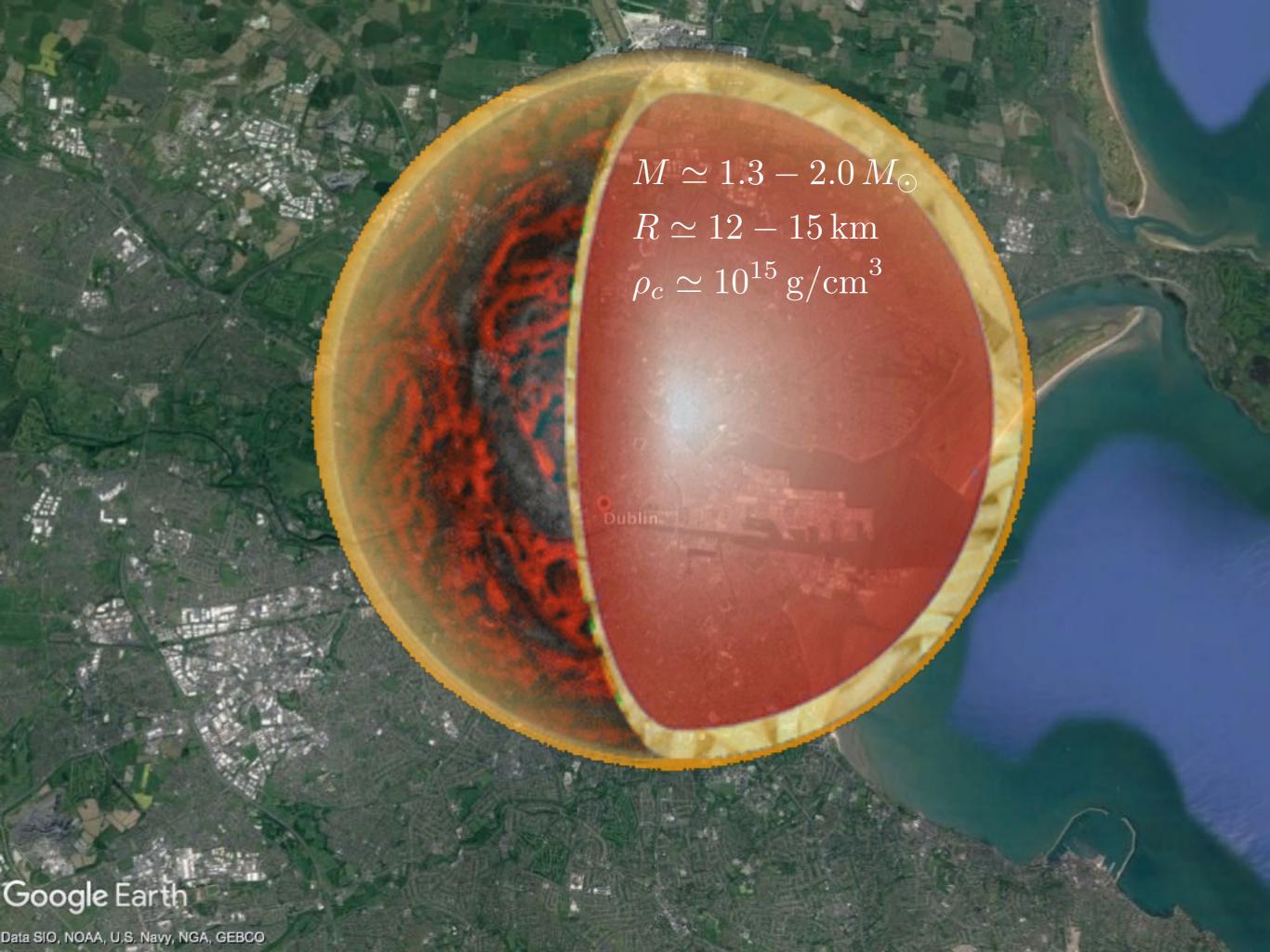
Crab pulsar.



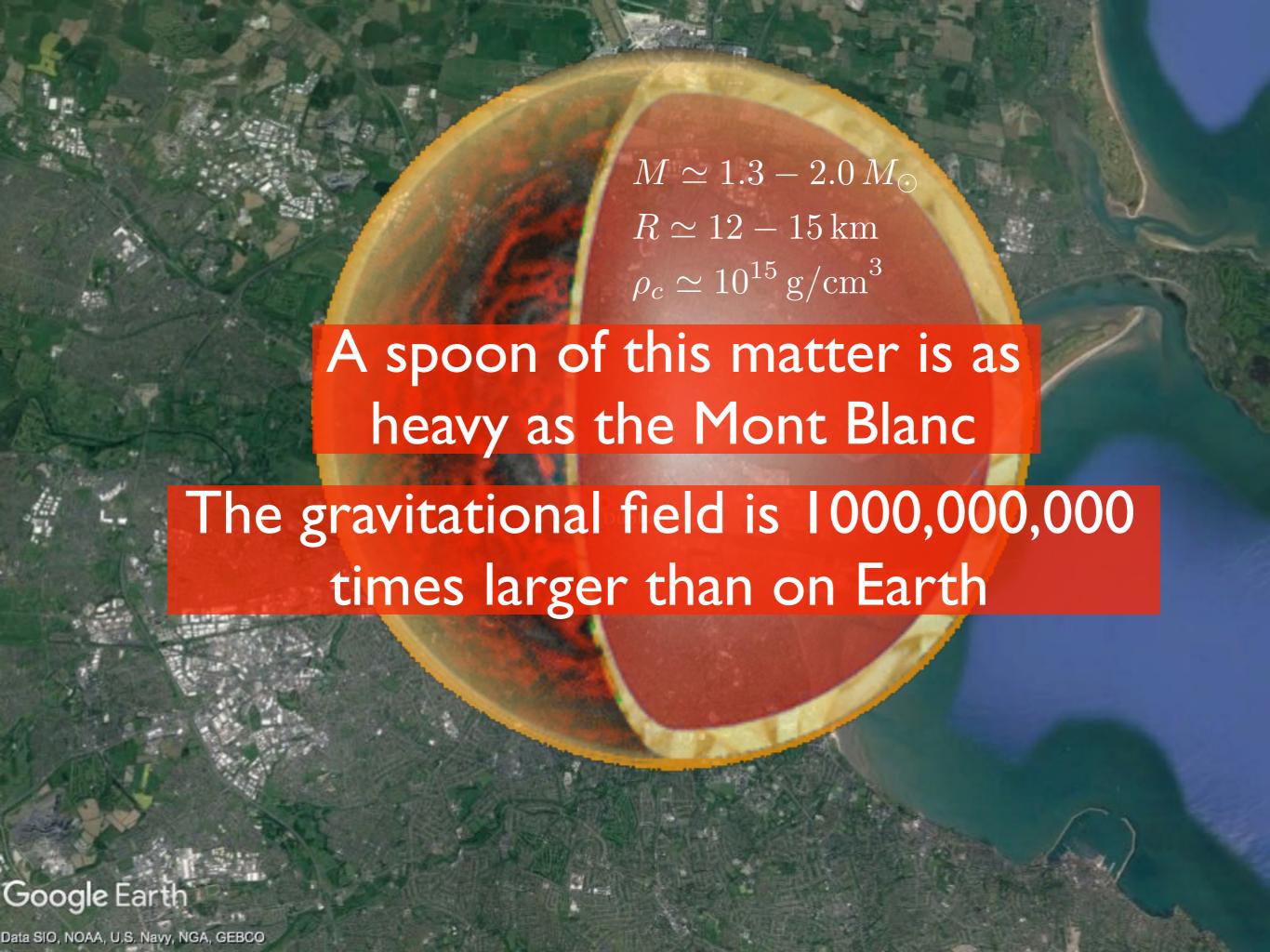
### Neutron stars are real marvels of nature

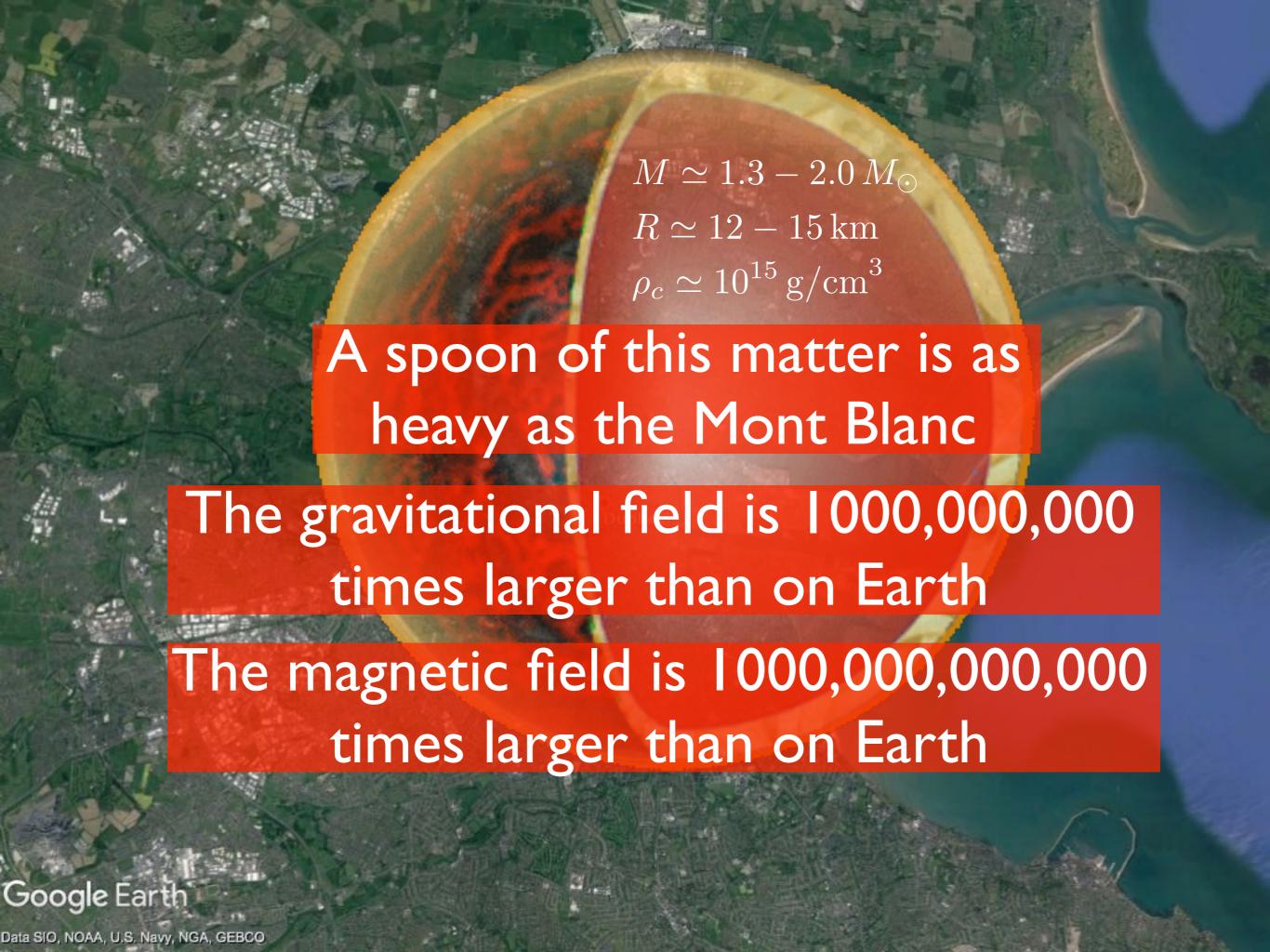


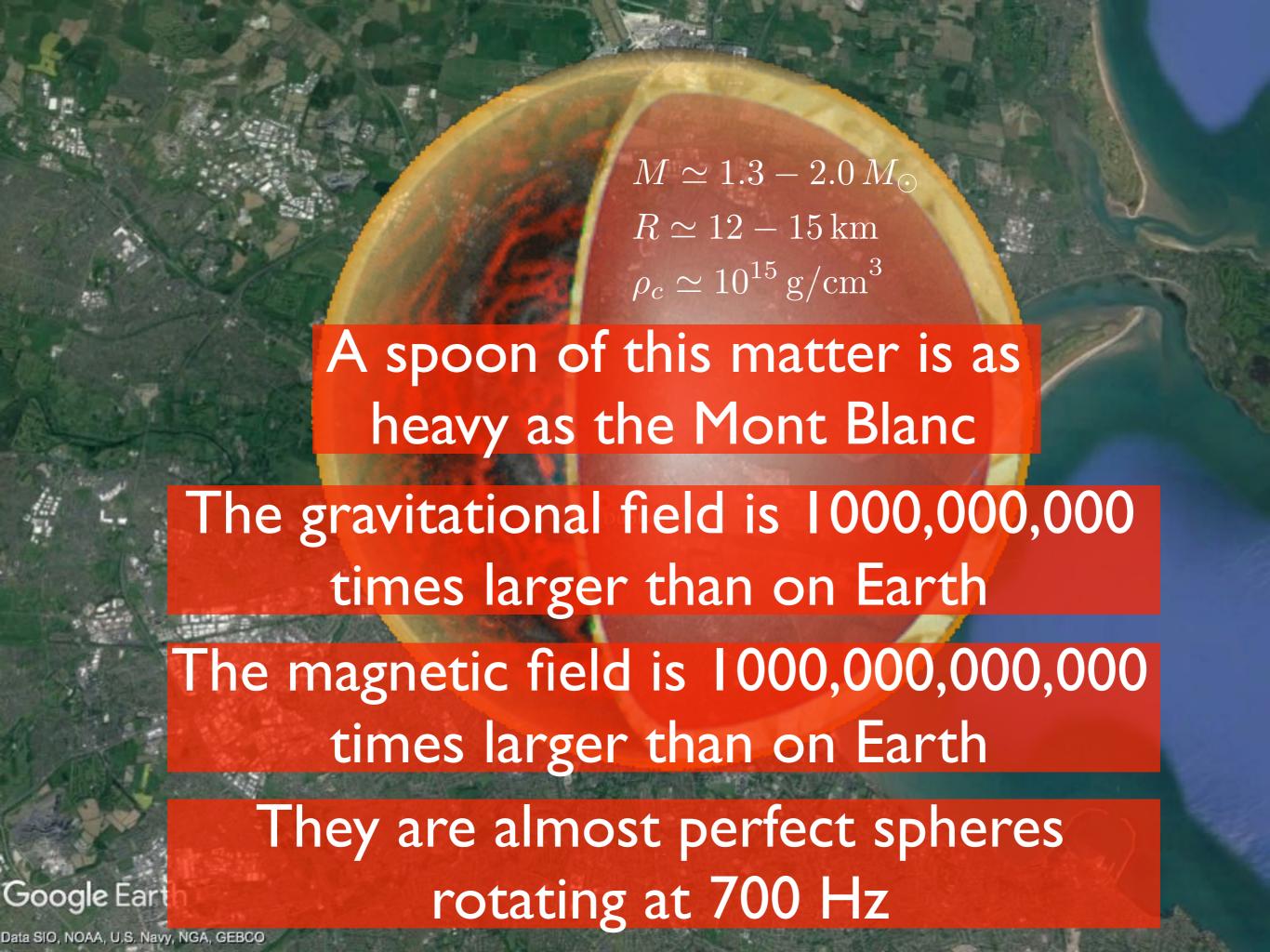








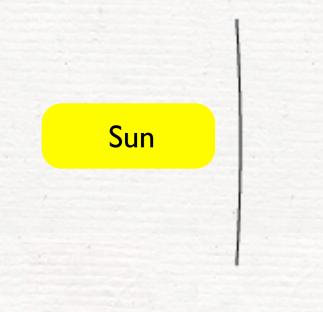




## Let's compare sizes and compactness



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 $R_{\odot} \simeq 70,000 \,\mathrm{km}; M/R \simeq 10^{-6}$ 

white dwarf

 $R_{\text{white dwarf}} \simeq 10000 \,\text{km}; M/R \simeq 10^{-4} - 10^{-5}$ 

white dwarf

neutron star

#### Let's compare sizes and compactness

Sun

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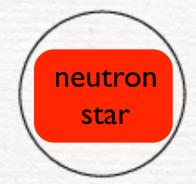
white dwarf

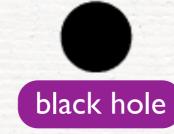
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 $R_{\rm white\ dwarf} \simeq 10000\ {\rm km}; M/R \simeq 10^{-4} - 10^{-5}$ 

neutron star

 $R_{\rm neutron\ star} \simeq 12\,\mathrm{km}; M/R \simeq 0.15-0.25$ 





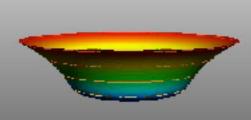
 $R_{\rm black\ hole} \simeq 1.5 \,\mathrm{km}; M/R = 0.5$ 

#### Neutron Star vs Black Hole

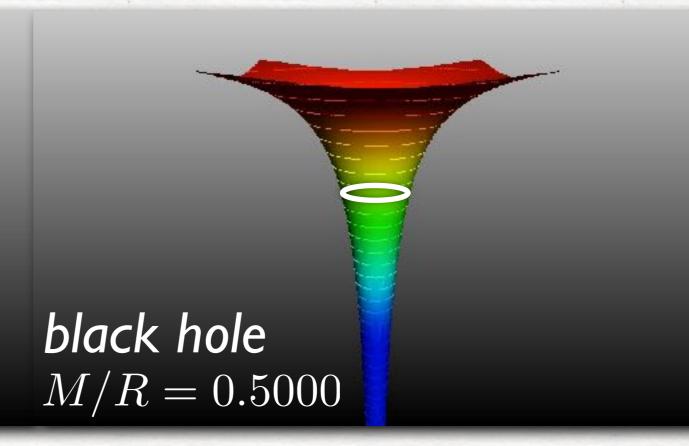
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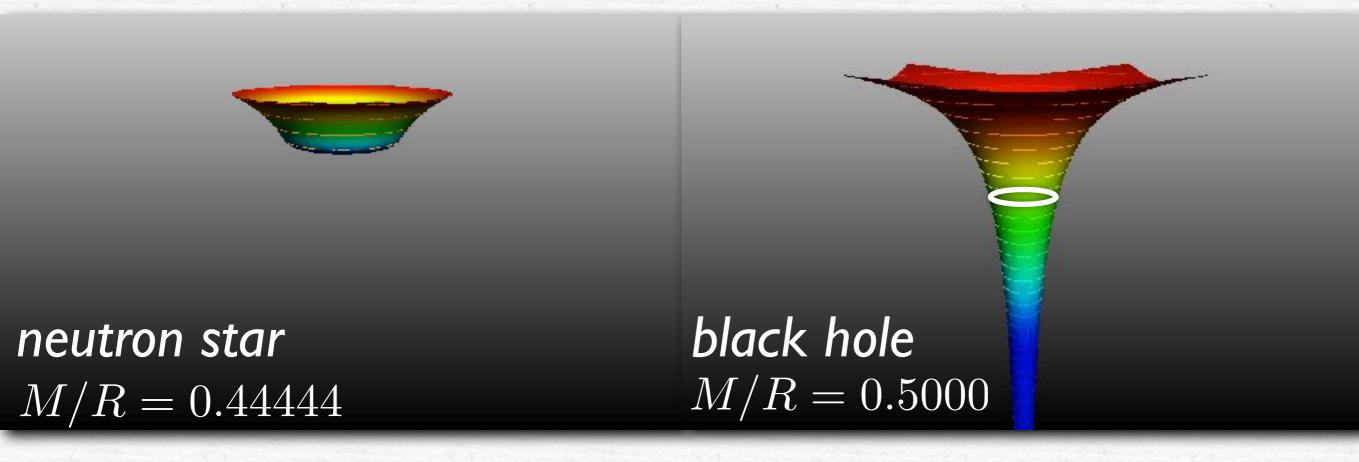


neutron star M/R = 0.444444



#### Neutron Star vs Black Hole

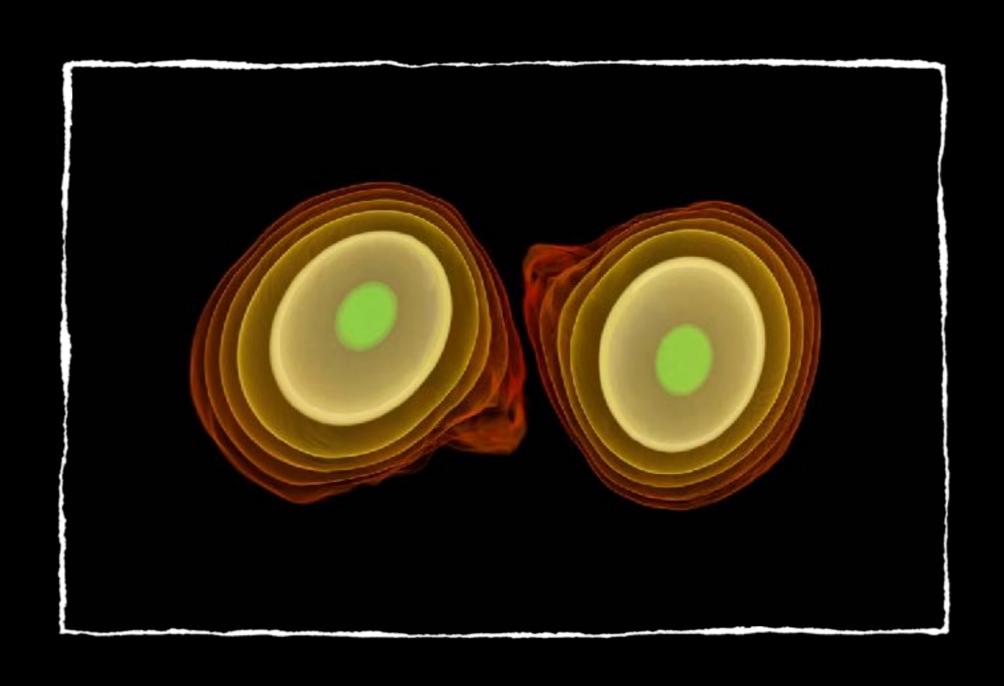
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In two things they differ:

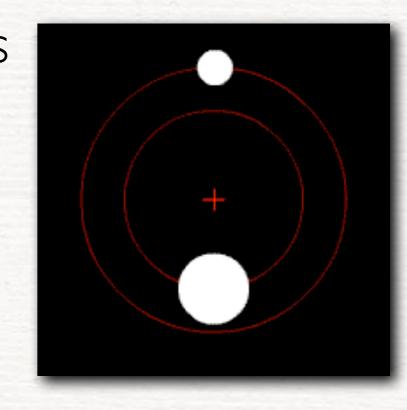
neutron stars have a hard surface and finite curvature; black holes have no surface, central curvature is infinite!

# Binary neutron stars



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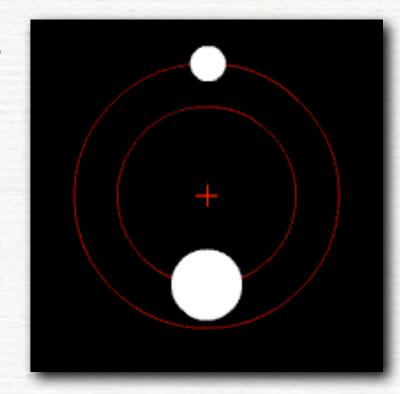
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$$\ddot{\boldsymbol{r}} = -\frac{GM}{d_{12}^3} \boldsymbol{r}$$

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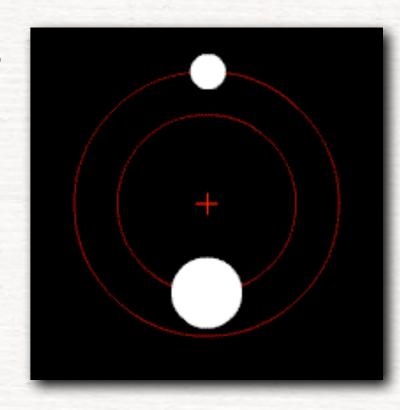
In Newton's gravity solution is analytic: there exist closed orbits (circular/elliptic)

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,  $\boldsymbol{r} \equiv \boldsymbol{r}_1 - \boldsymbol{r}_2$ ,  $d_{12} \equiv |\boldsymbol{r}_1 - \boldsymbol{r}_2|$ .

In Einstein's gravity no analytic solution!

No closed orbits: the system loses energy/angular momentum via gravitational waves.



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$$BH + BH \longrightarrow BH + GWs$$

• For NSs the question is more **subtle**: the merger leads to an hyper-massive neutron star (HMNS), ie a metastable equilibrium:

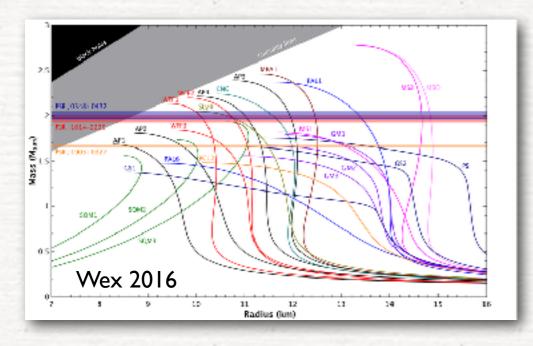
$$NS + NS \longrightarrow HMNS + ...? \longrightarrow BH + torus + ...? \longrightarrow BH$$

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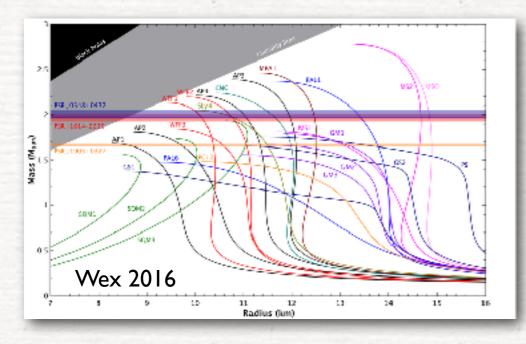


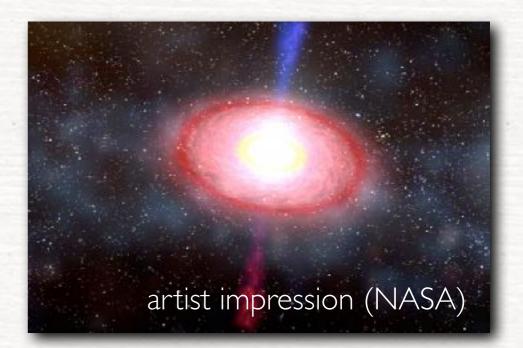
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• BH+torus system may tell us on the central engine of GRBs

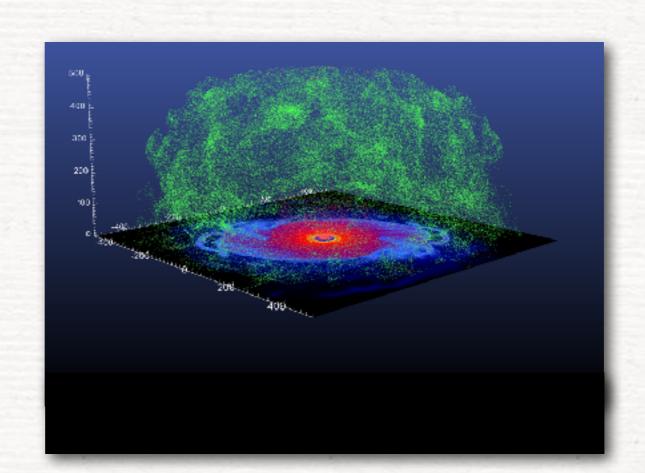
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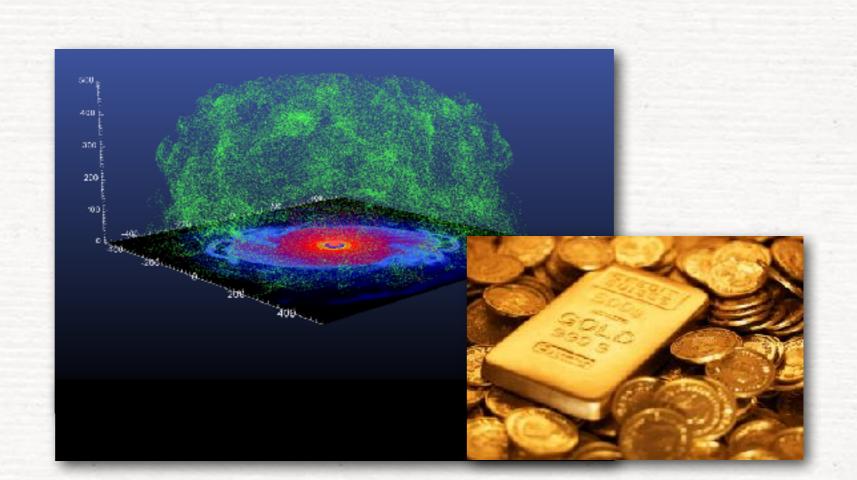


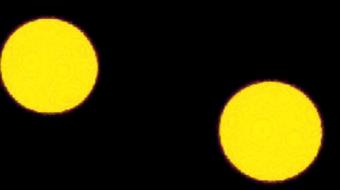
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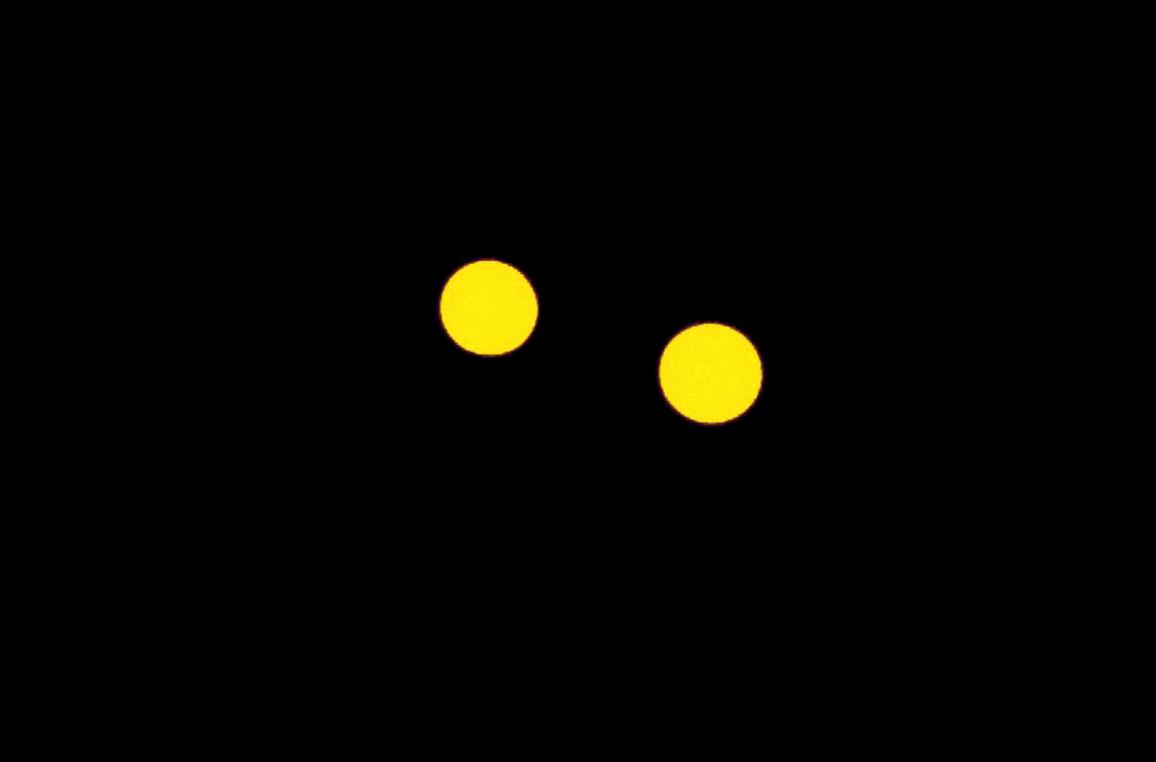
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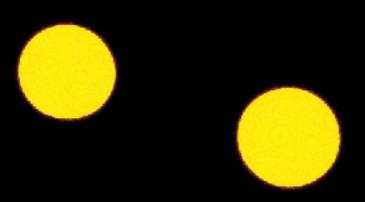
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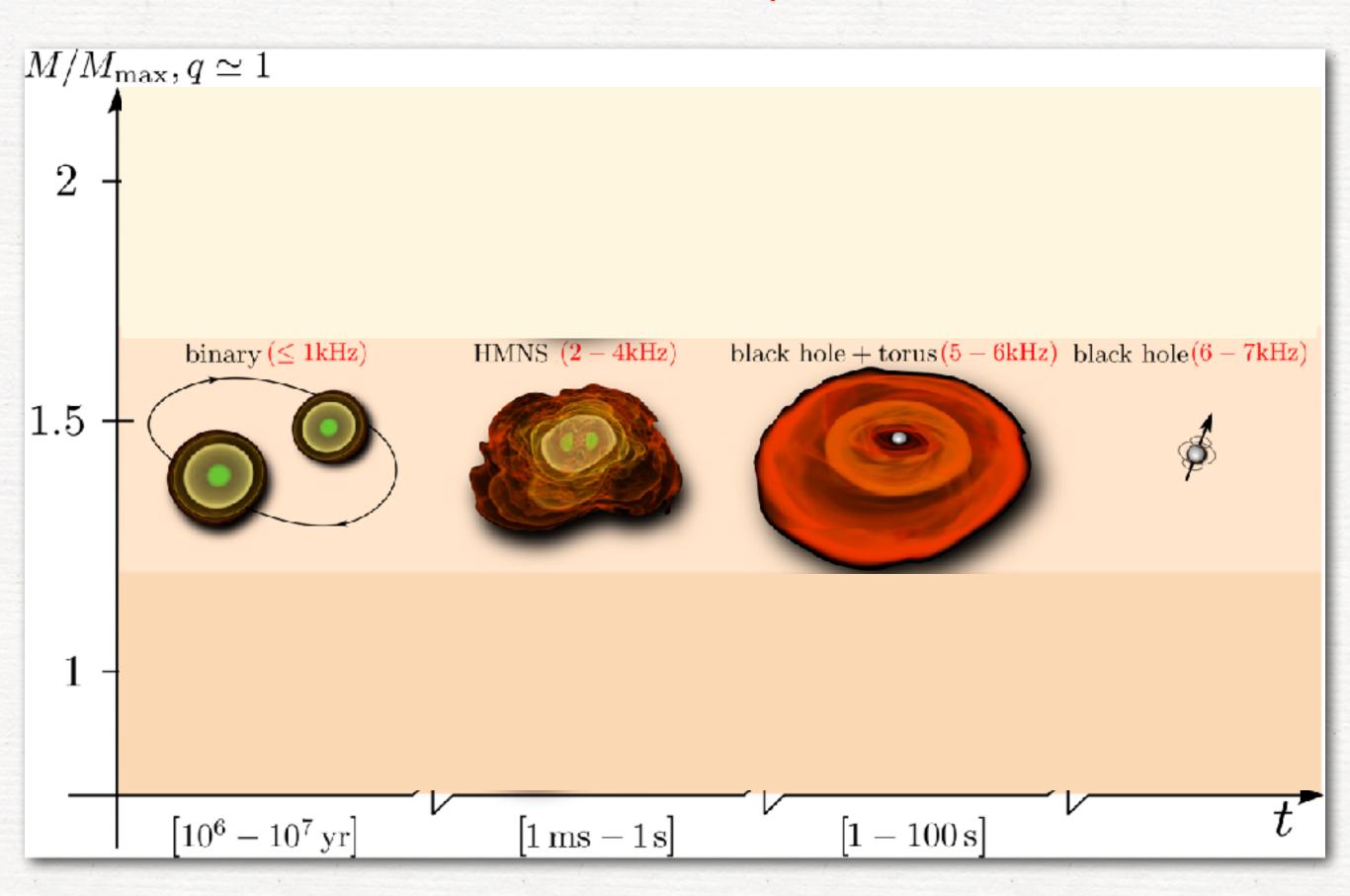


 $M = 2 \times 1.35 M_{\odot}$ LS220 EOS

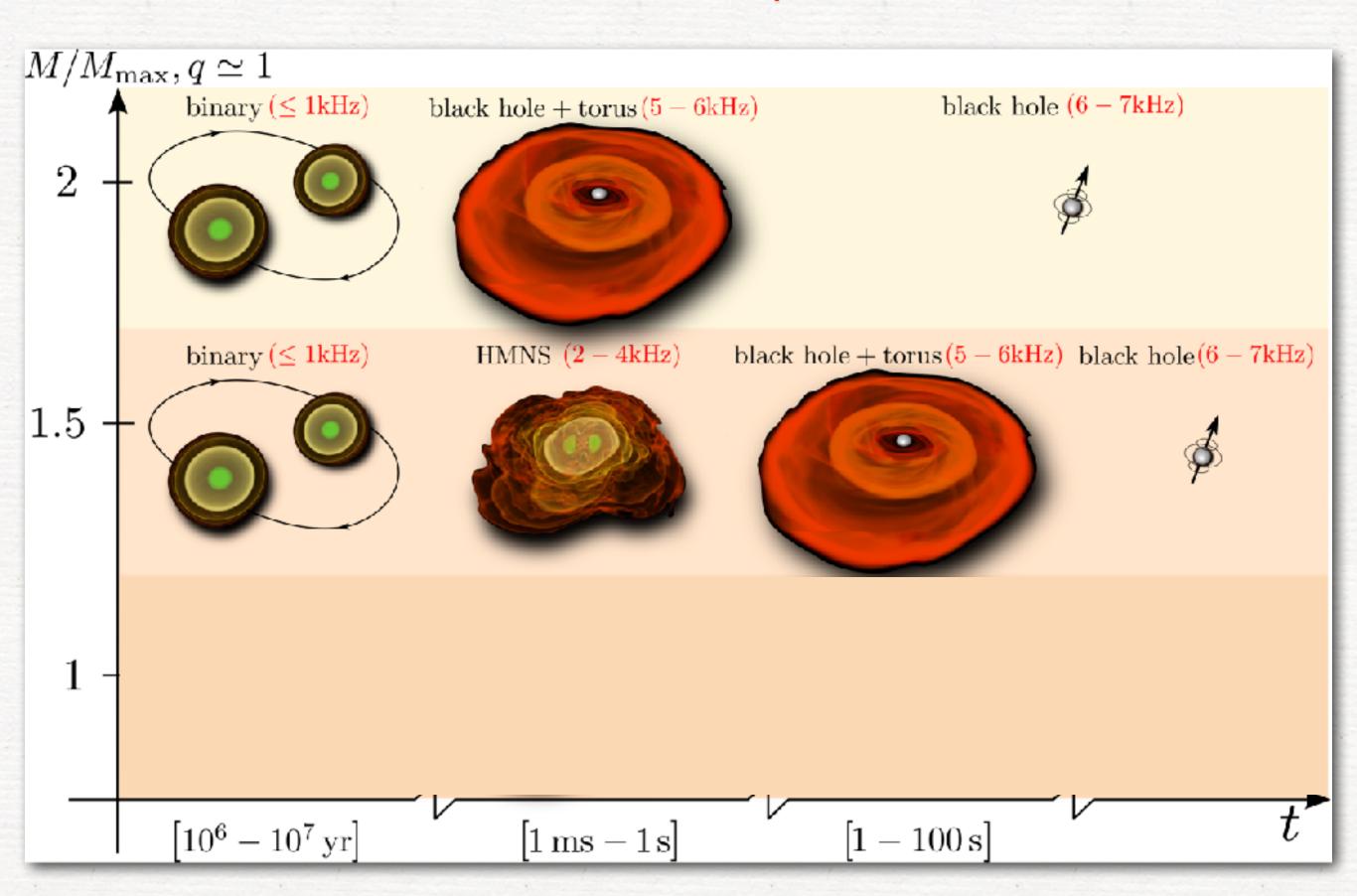




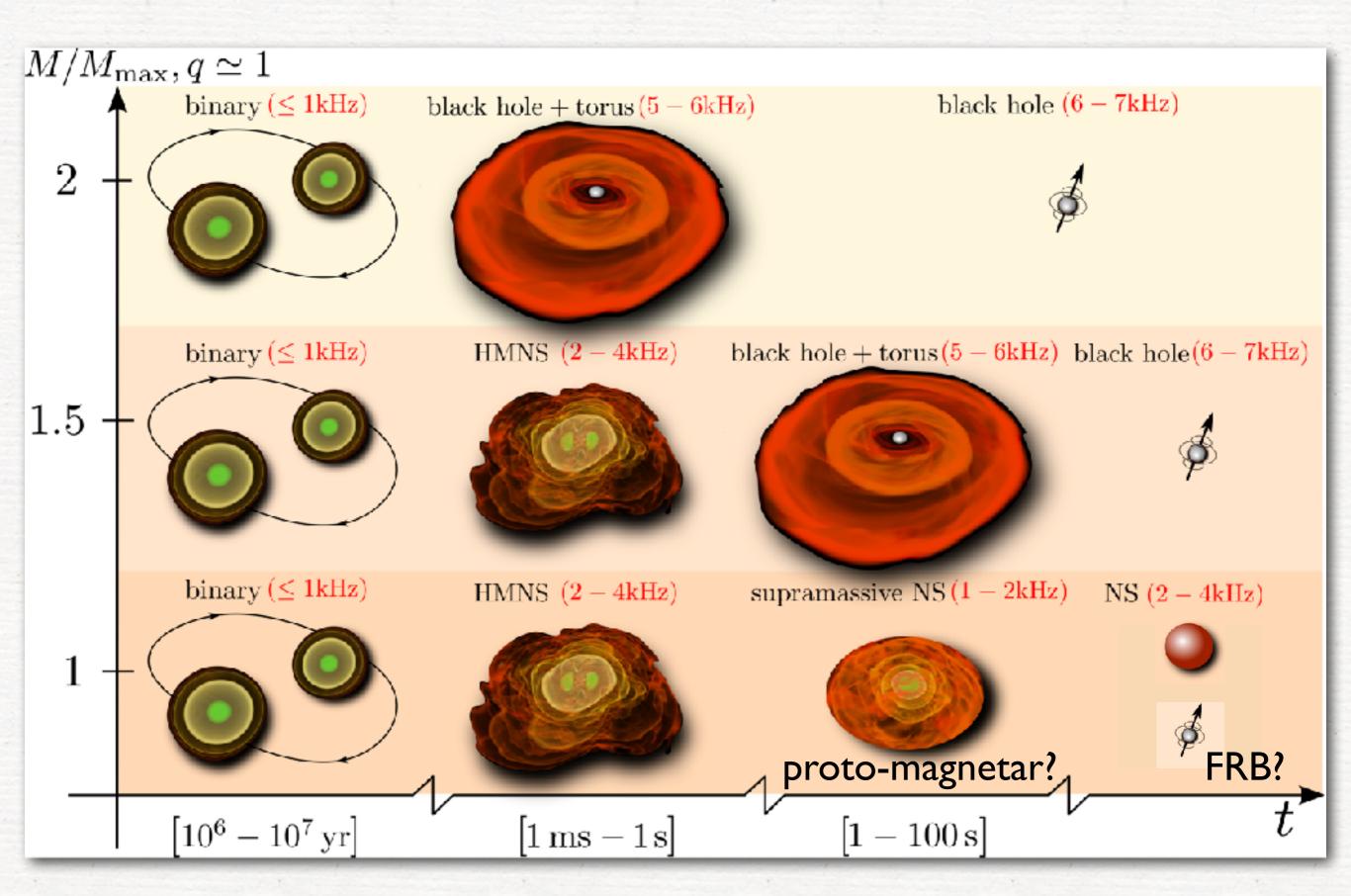
# Broadbrush picture



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Quantitative differences are produced by:

total mass (prompt vs delayed collapse)

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- mass asymmetries (HMNS and torus)

Total mass:  $3.37 M_{\odot}$ ; mass ratio: 0.80;











- \* the torii are generically more massive
- \* the torii are generically more extended
- \* the torii tend to stable quasi-Keplerian configurations
- \* overall unequal-mass systems have all the ingredients
- needed to create a GRB

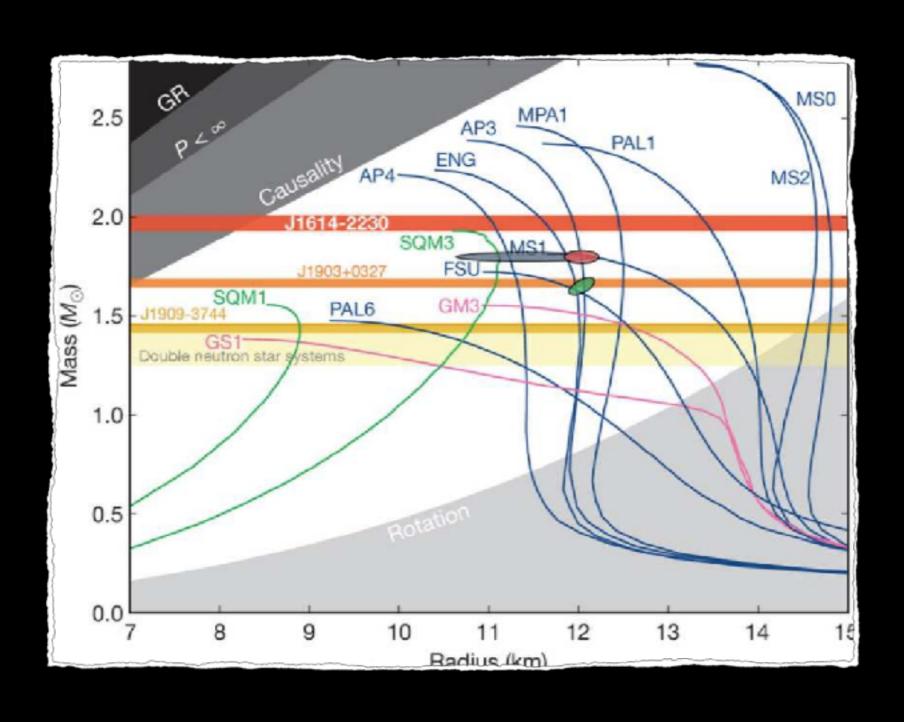
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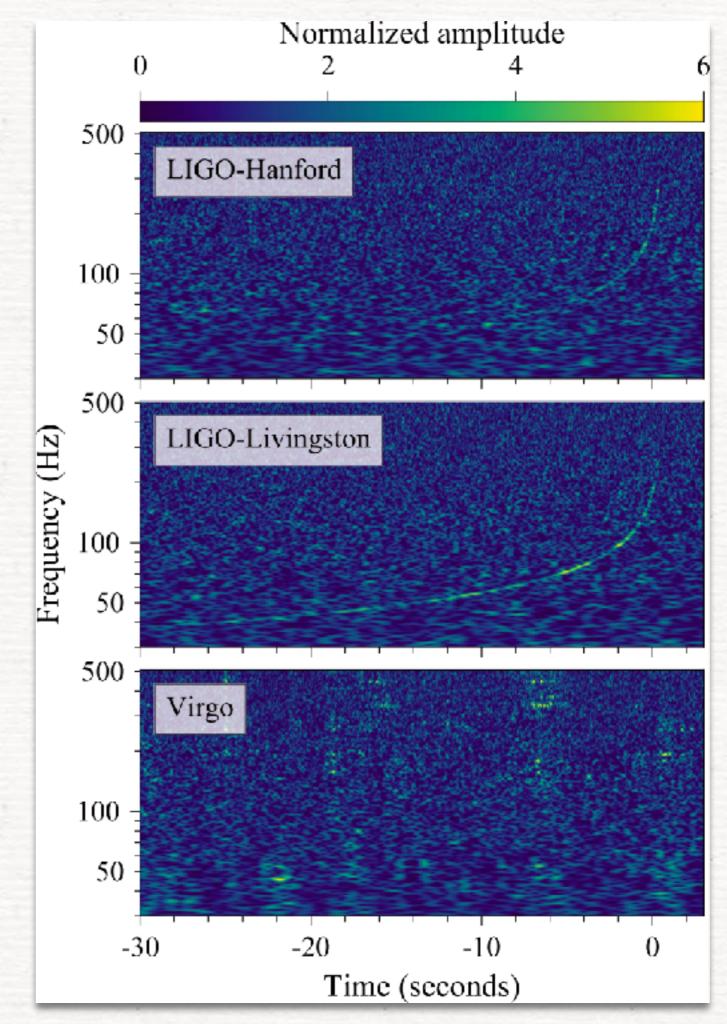
- total mass (prompt vs delayed collapse)
- mass asymmetries (HMNS and torus)
- Equation of State (EOS) soft/stiff (grav. waves)
- magnetic fields (equil. and EM emission)
- radiative losses (equil. and nucleosynthesis)

# How to constrain the EOS



#### GW170817

•On 16 October 2017 the LSC/Virgo collaboration announced detection of the gravitational signal from merging binary neutron-star system.



#### GW170817

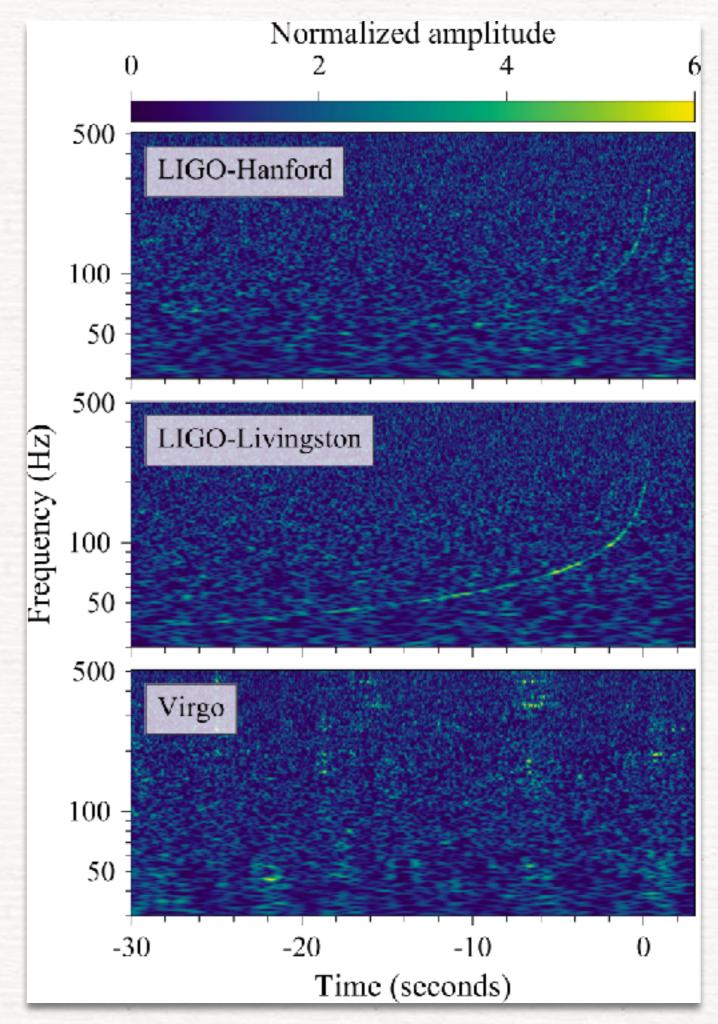
- •On 16 October 2017 the LSC/Virgo collaboration announced detection of the gravitational signal from merging binary neutron-star system.
- Total mass:

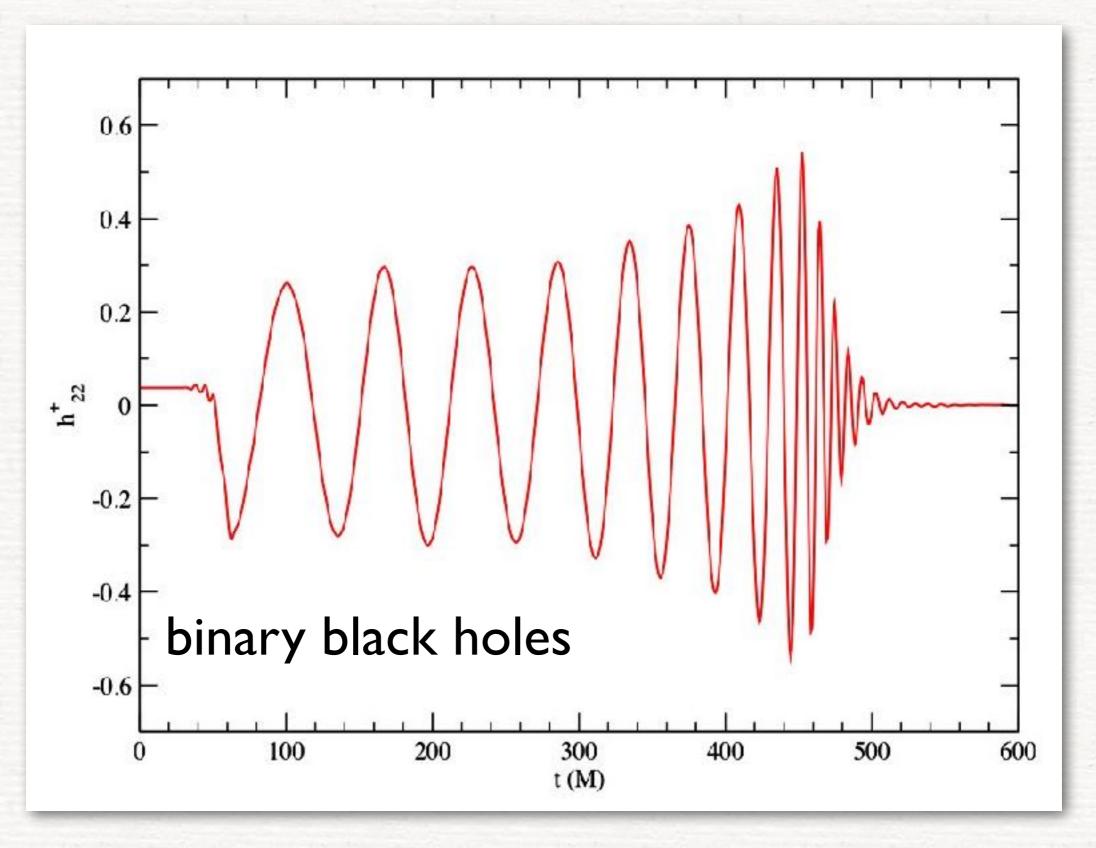
$$M_1 + M_2 = 2.74^{+0.04}_{-0.01} M_{\odot}$$

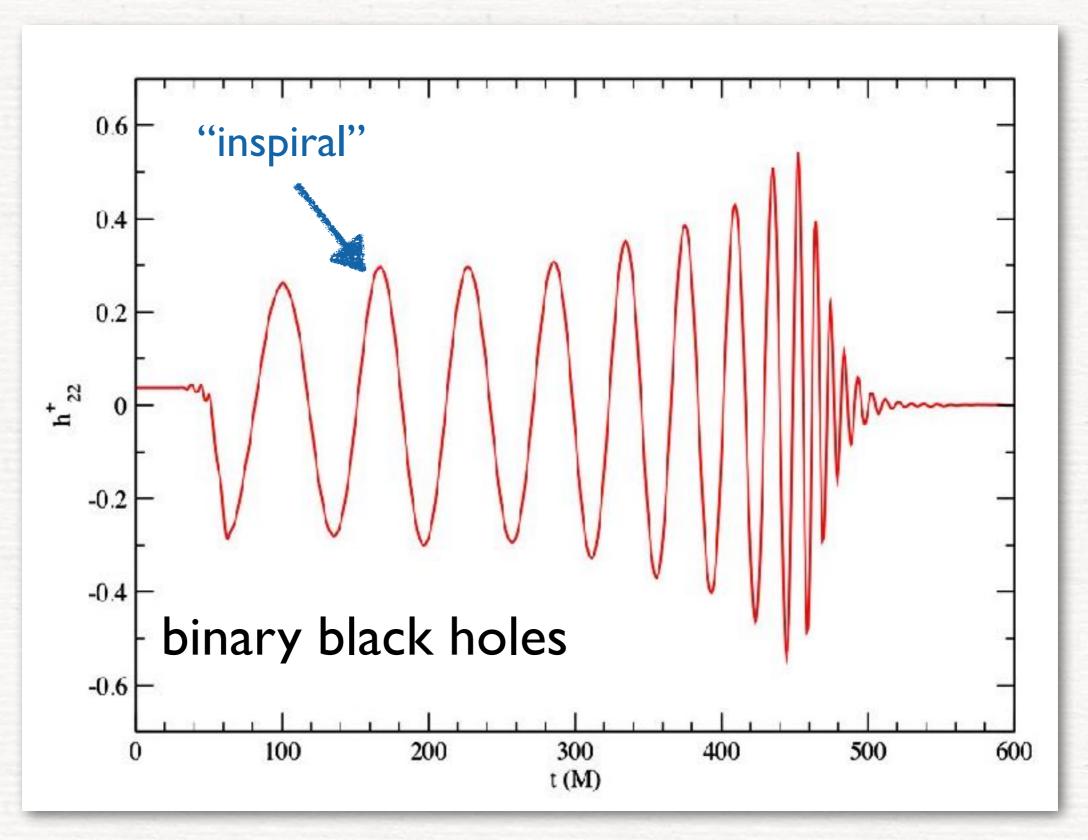
Individual masses:

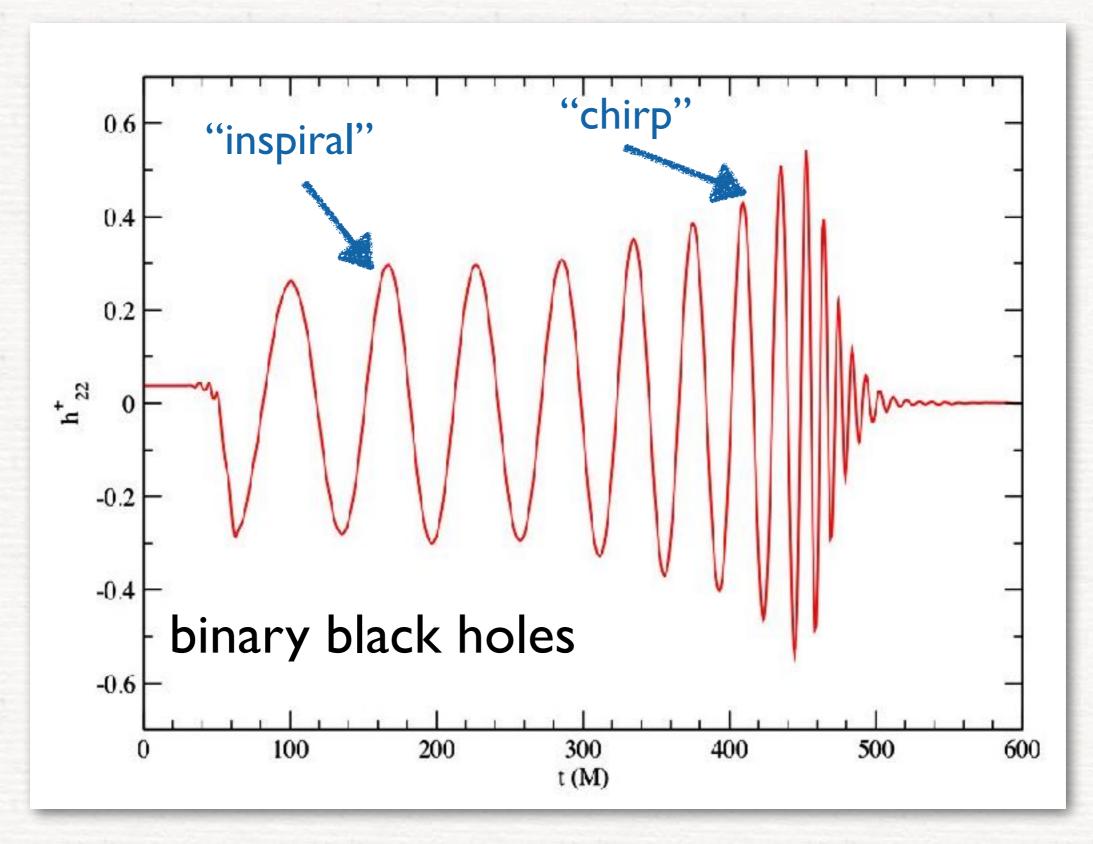
$$M_1 = 1.36 - 1.60 M_{\odot}$$

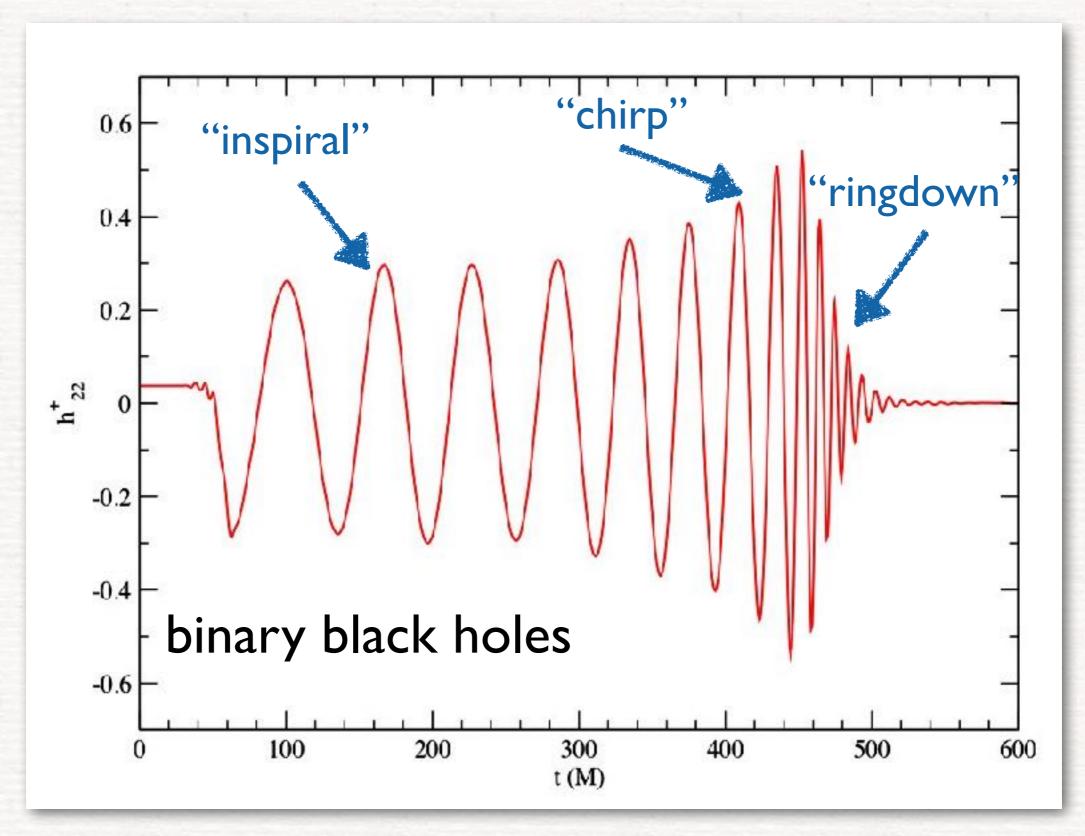
$$M_2 = 1.17 - 1.36 M_{\odot}$$

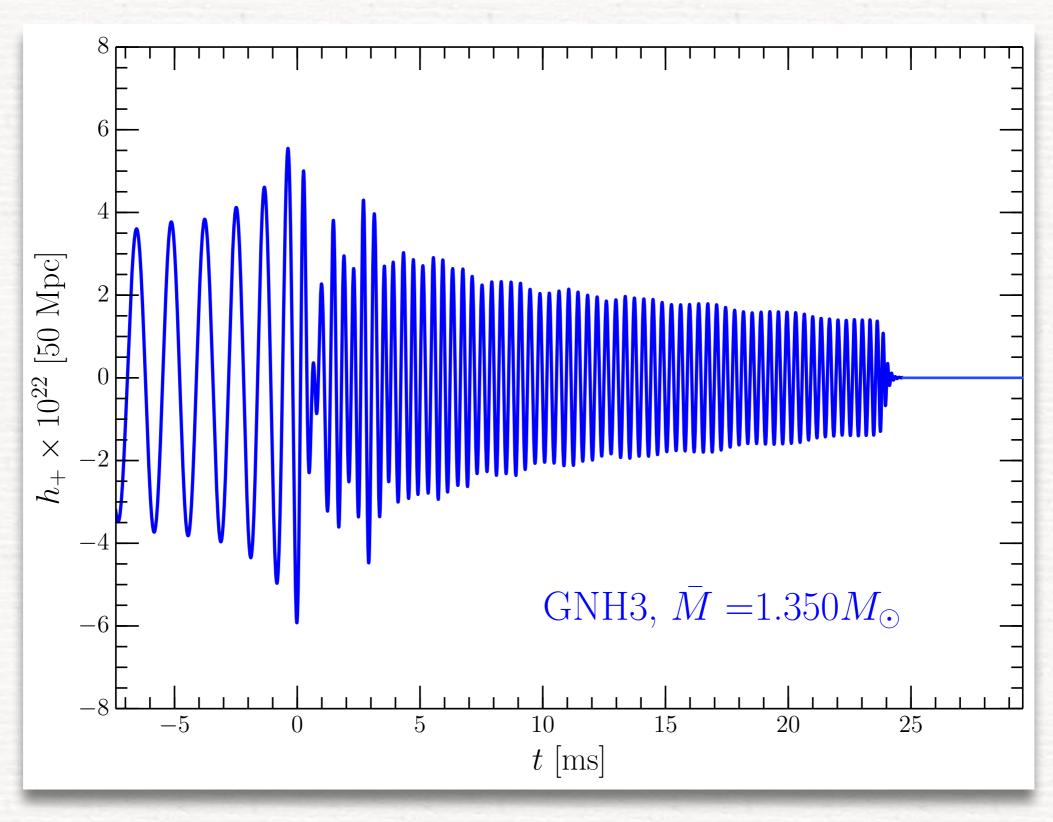


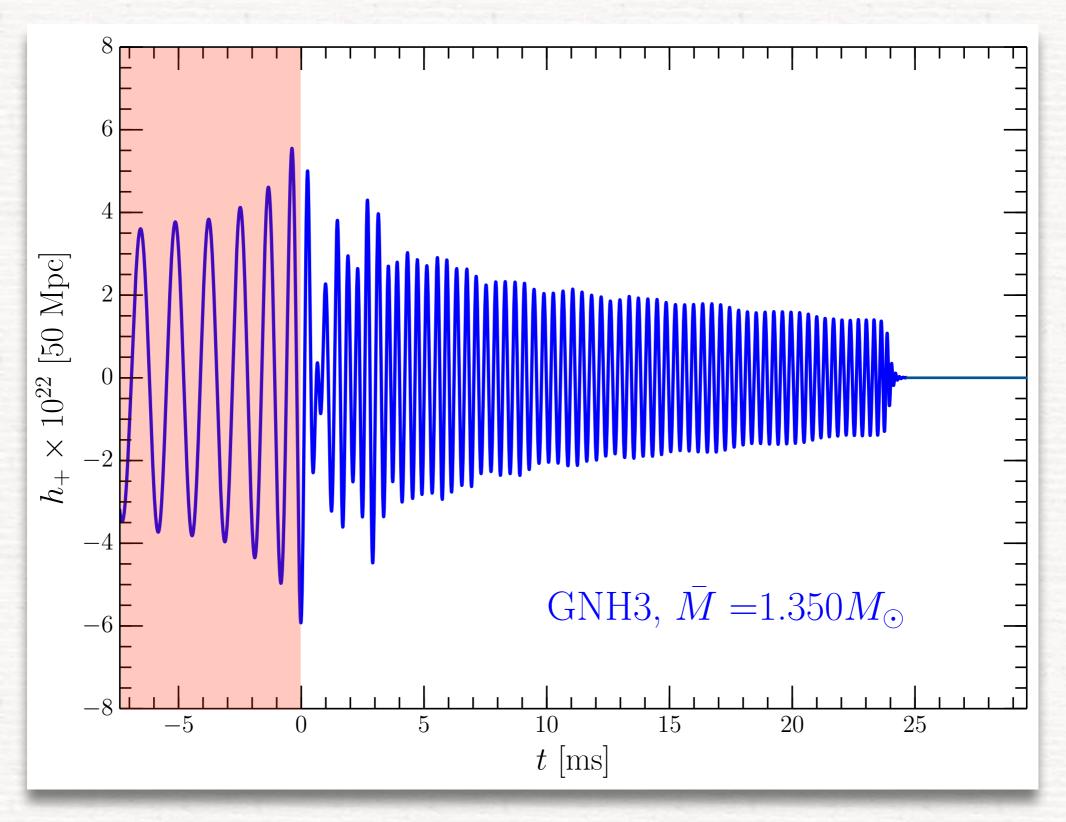




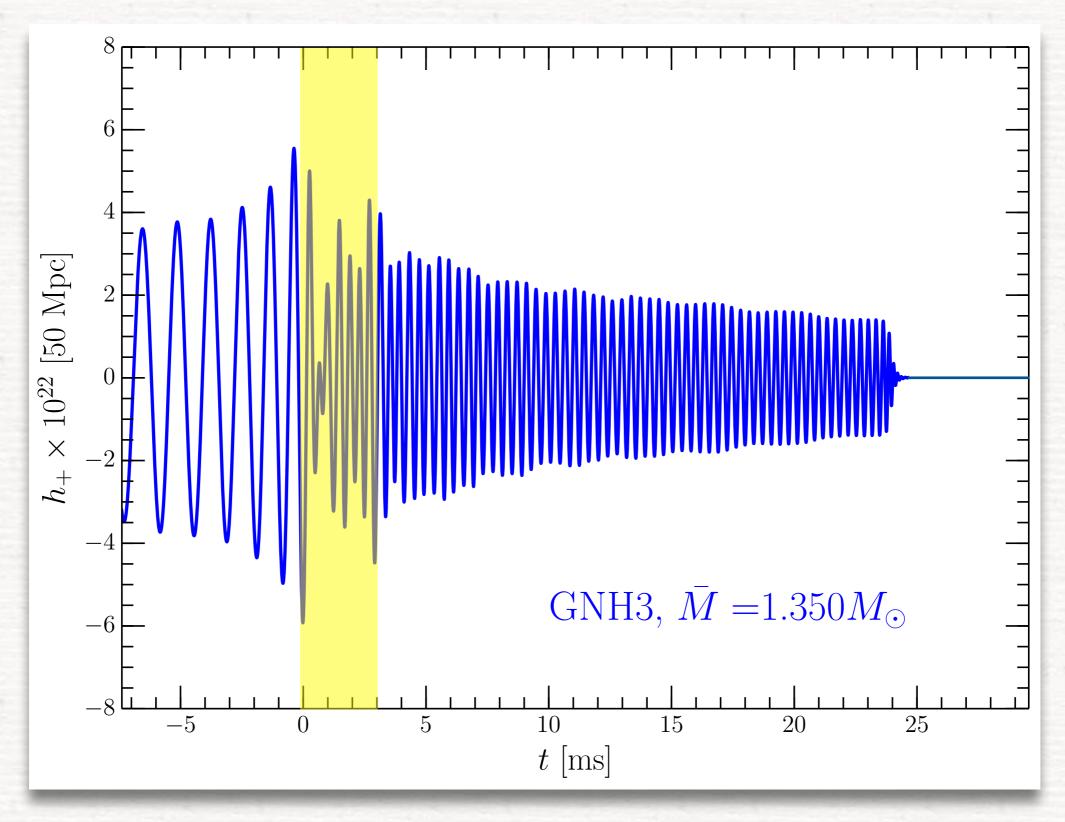




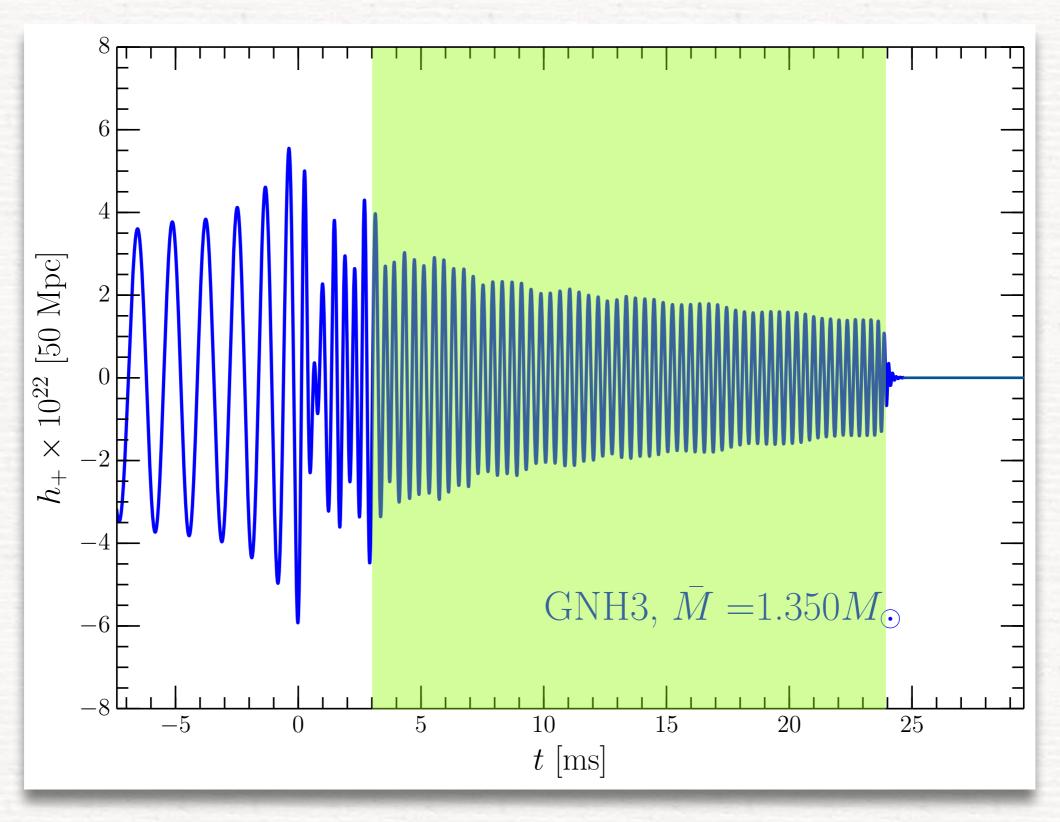




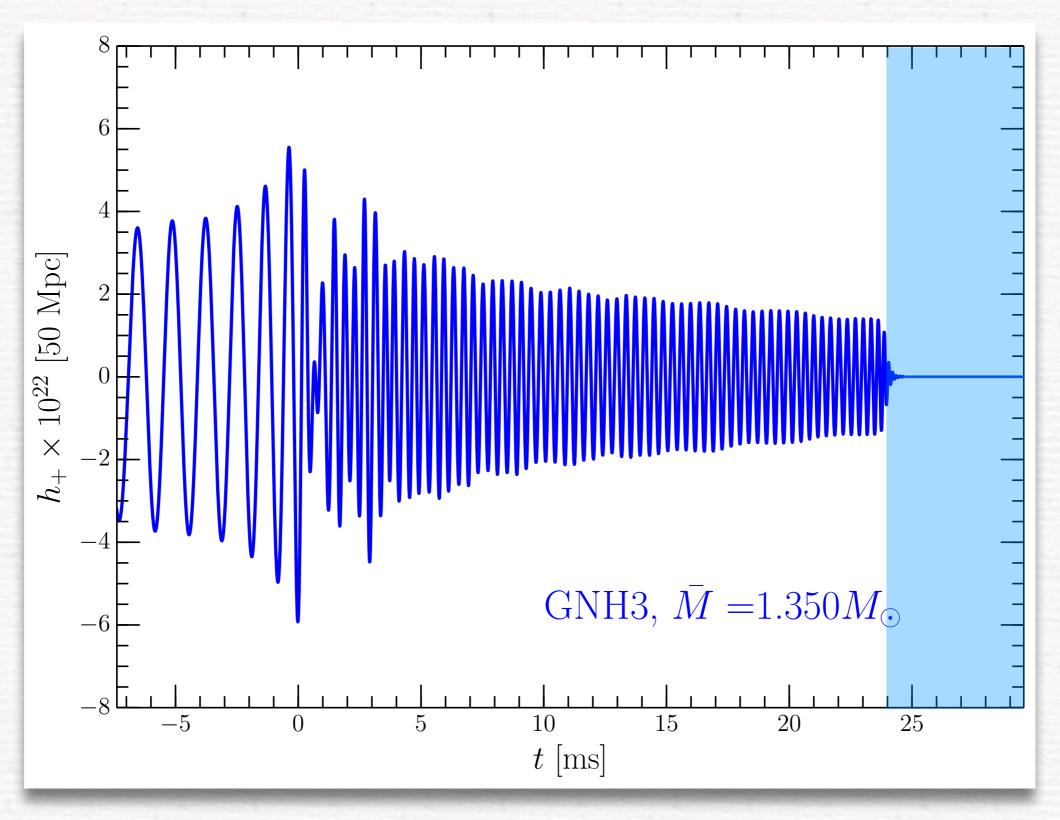
Inspiral/chirp: well approximated by semianalytic approaches



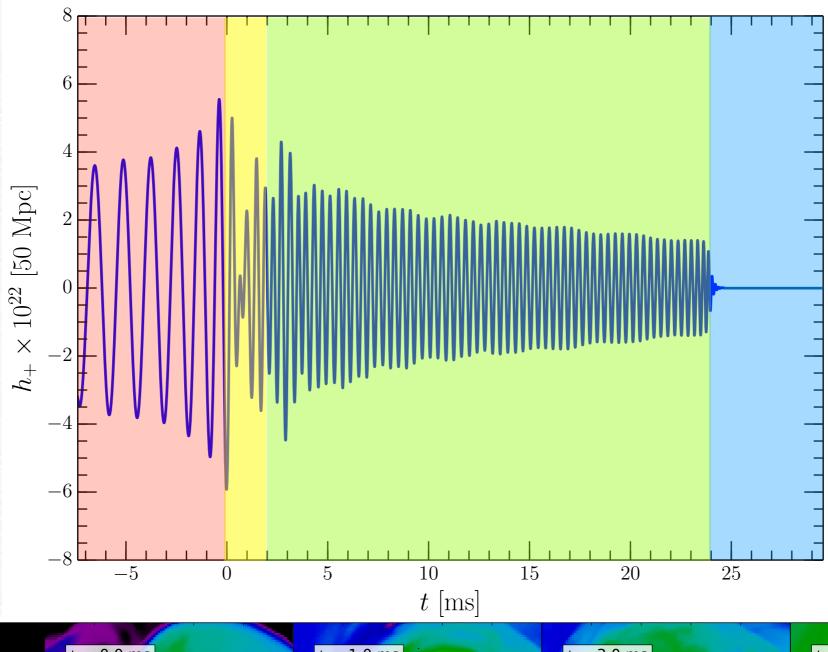
Merger: highly nonlinear but analytic description possible

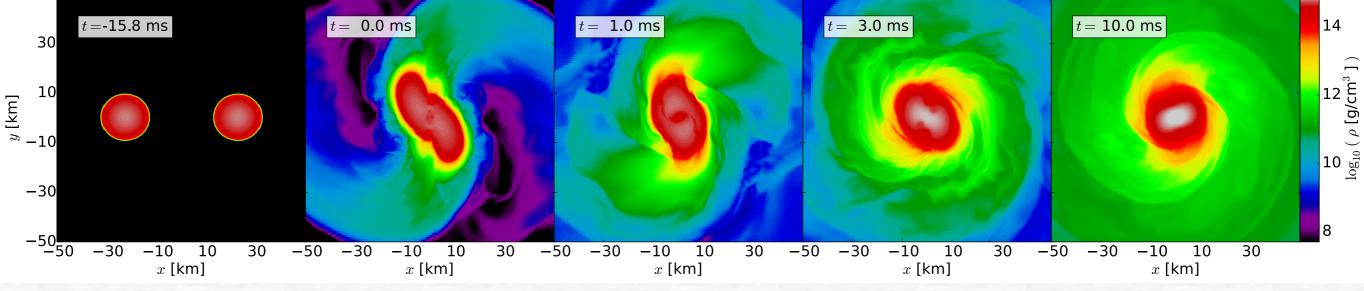


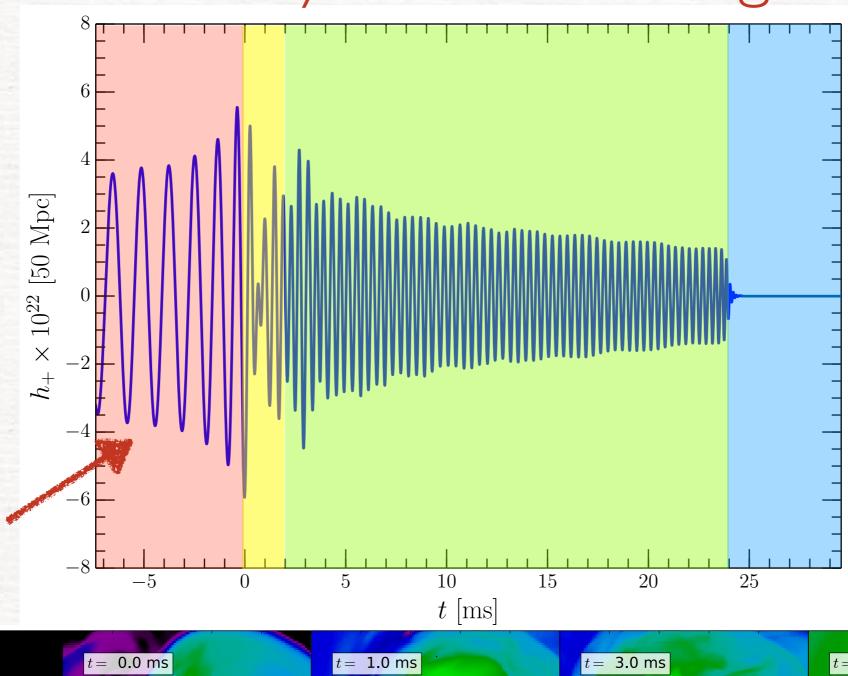
post-merger: quasi-periodic emission of bar-deformed HMNS



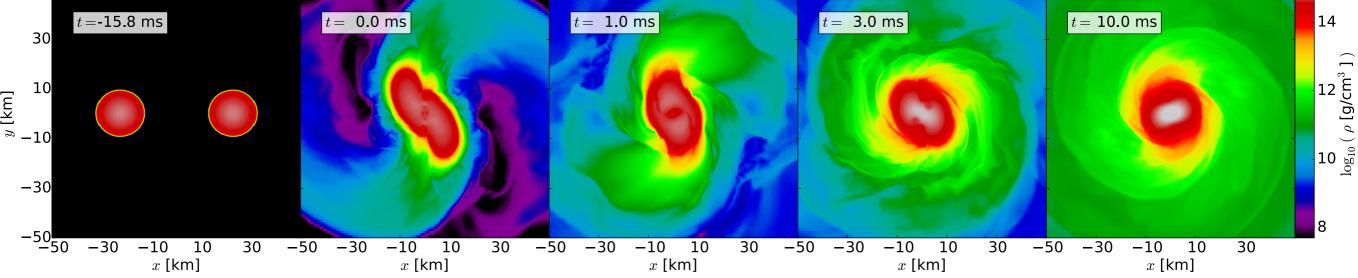
Collapse-ringdown: signal essentially shuts off.

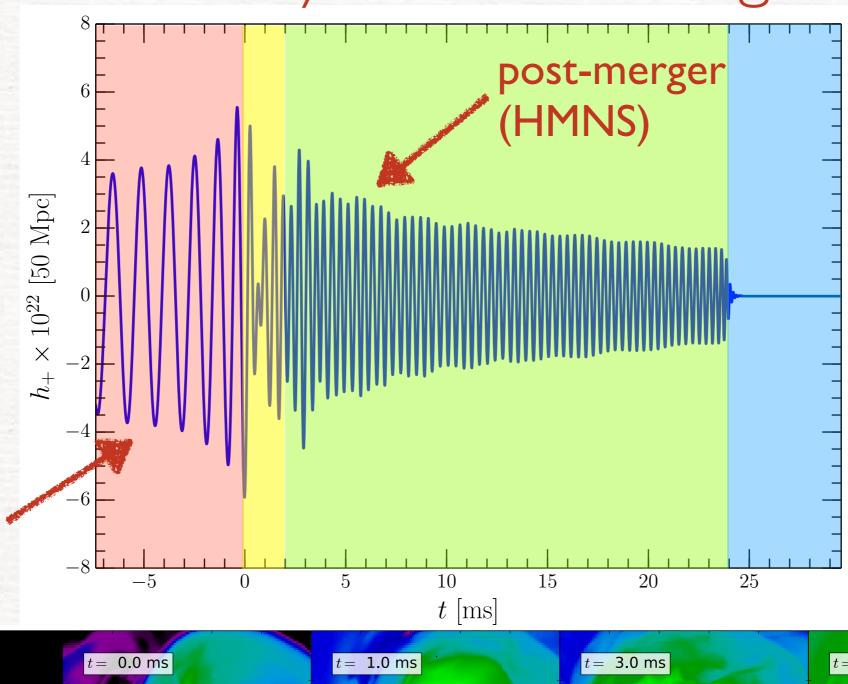




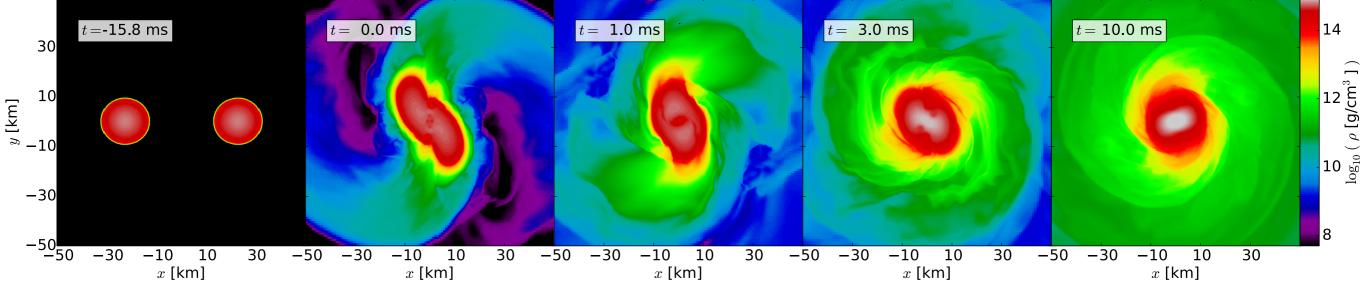


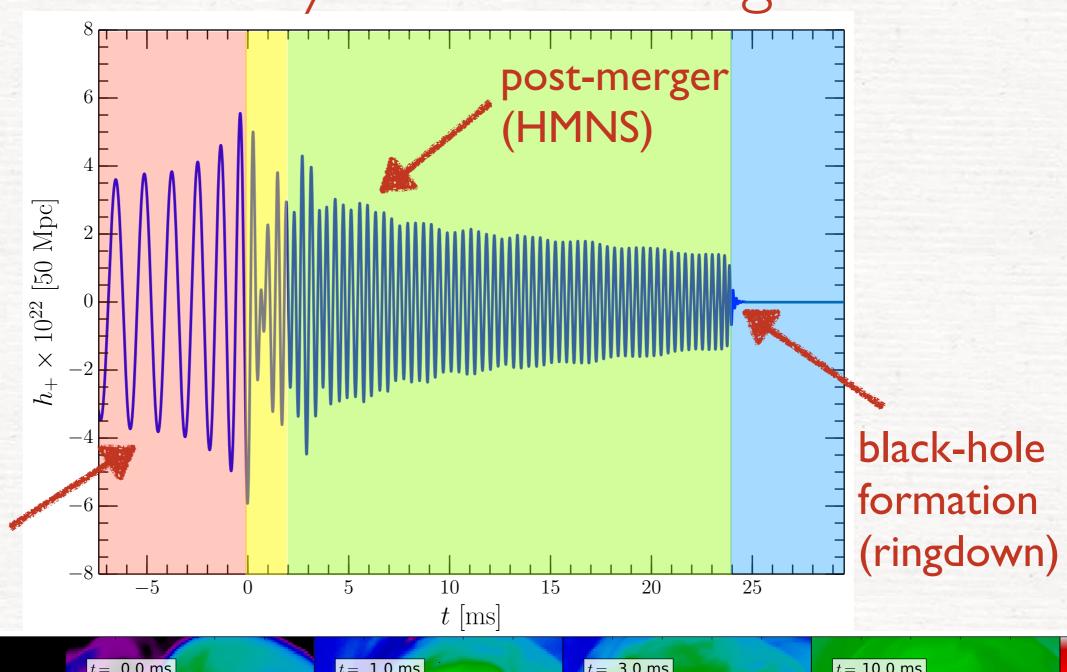




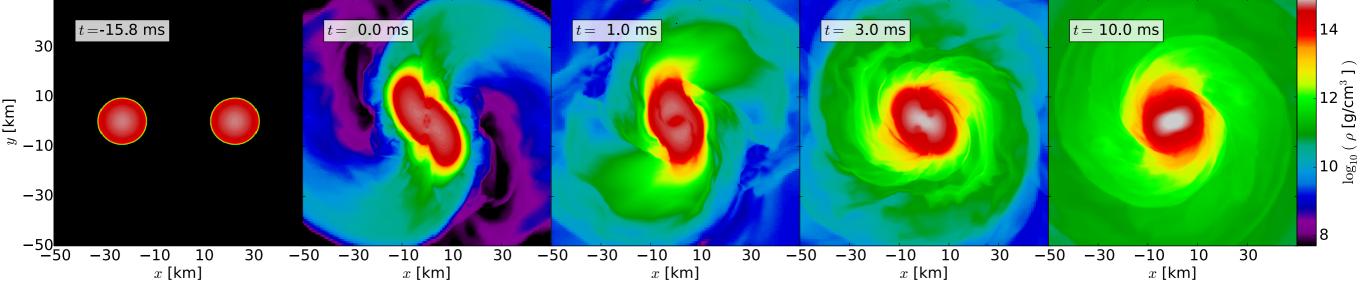


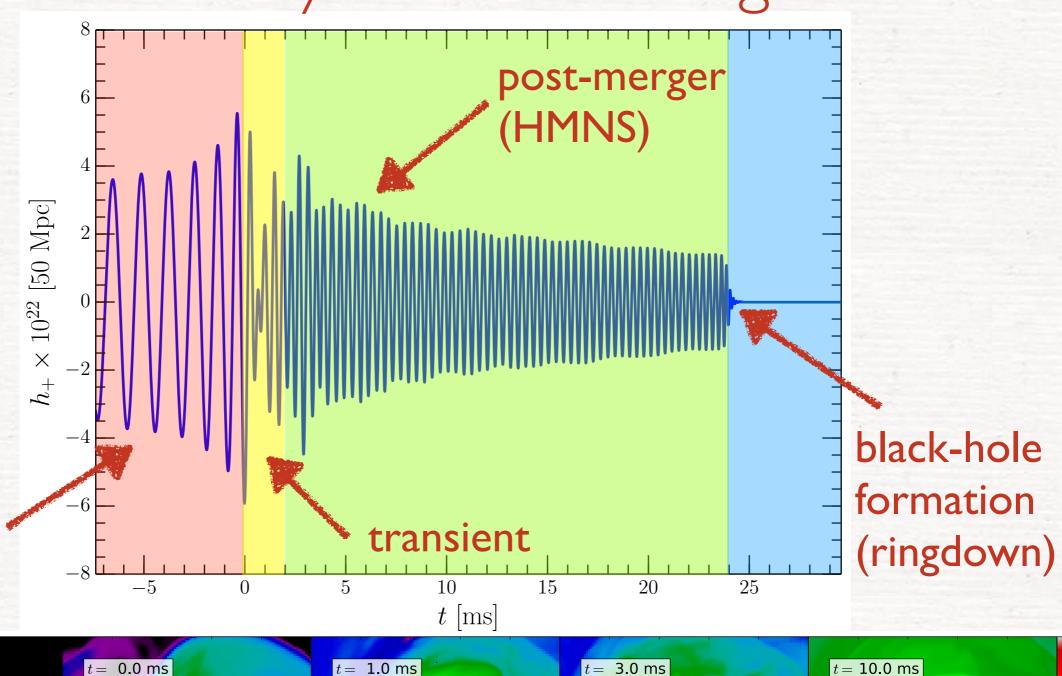
Chirp signal

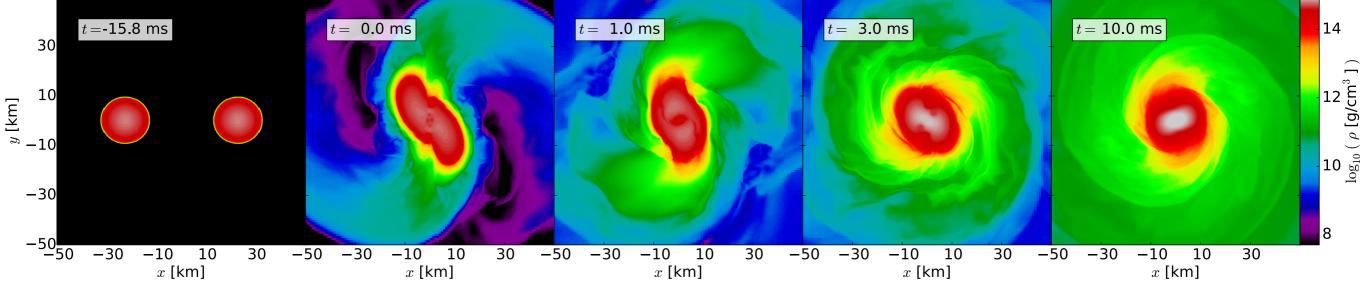




Chirp signal

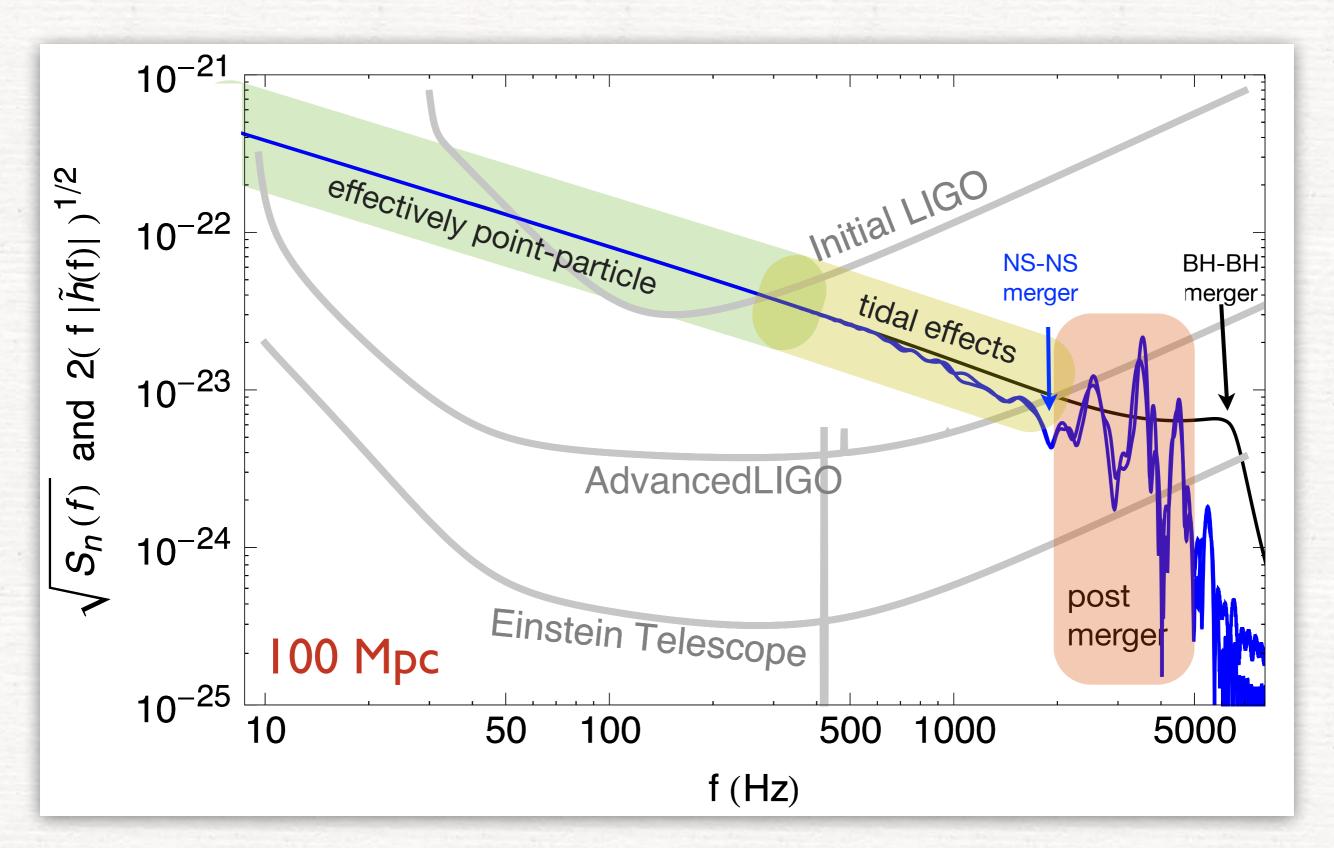




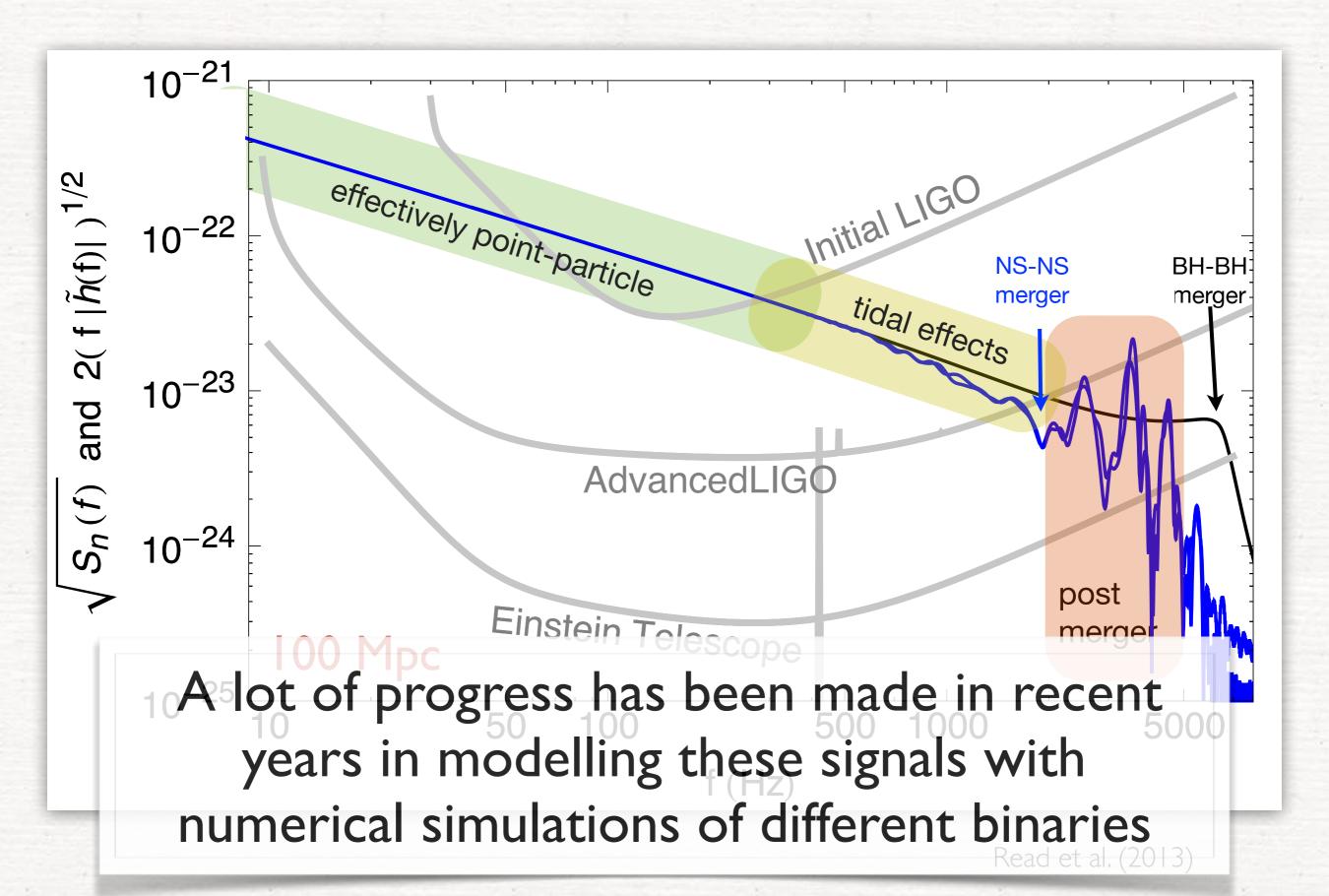


Chirp signal

#### In frequency space

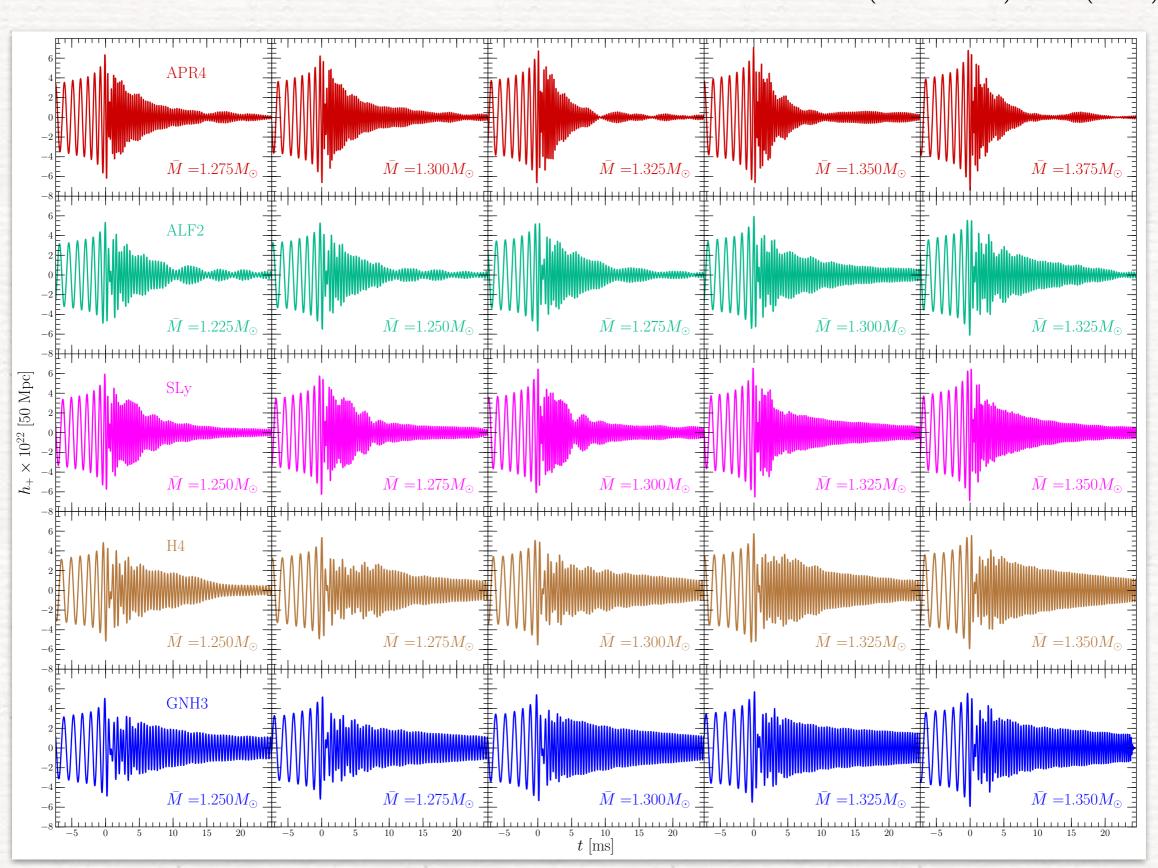


#### In frequency space



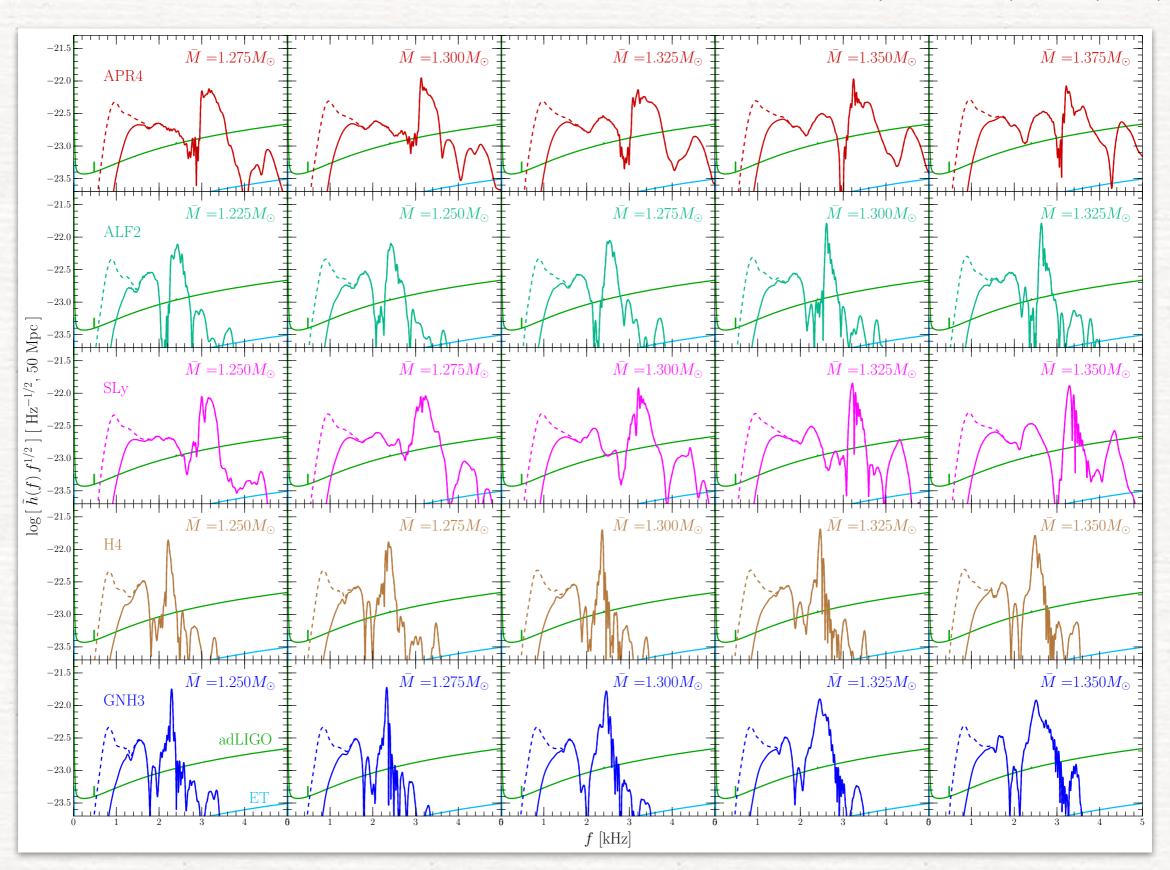
#### What we can do nowadays

Takami, LR, Baiotti (2014, 2015), LR+ (2016)



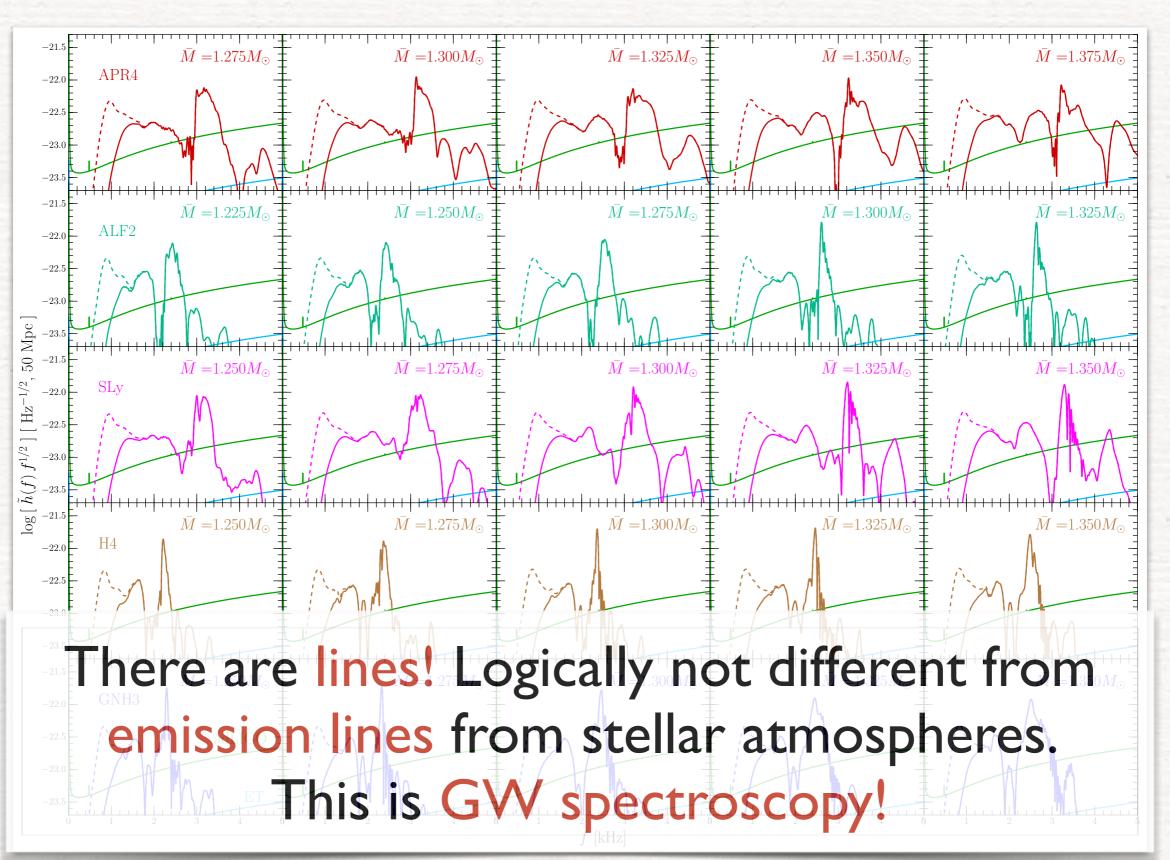
# Extracting information from the EOS

Takami, LR, Baiotti (2014, 2015), LR+ (2016)



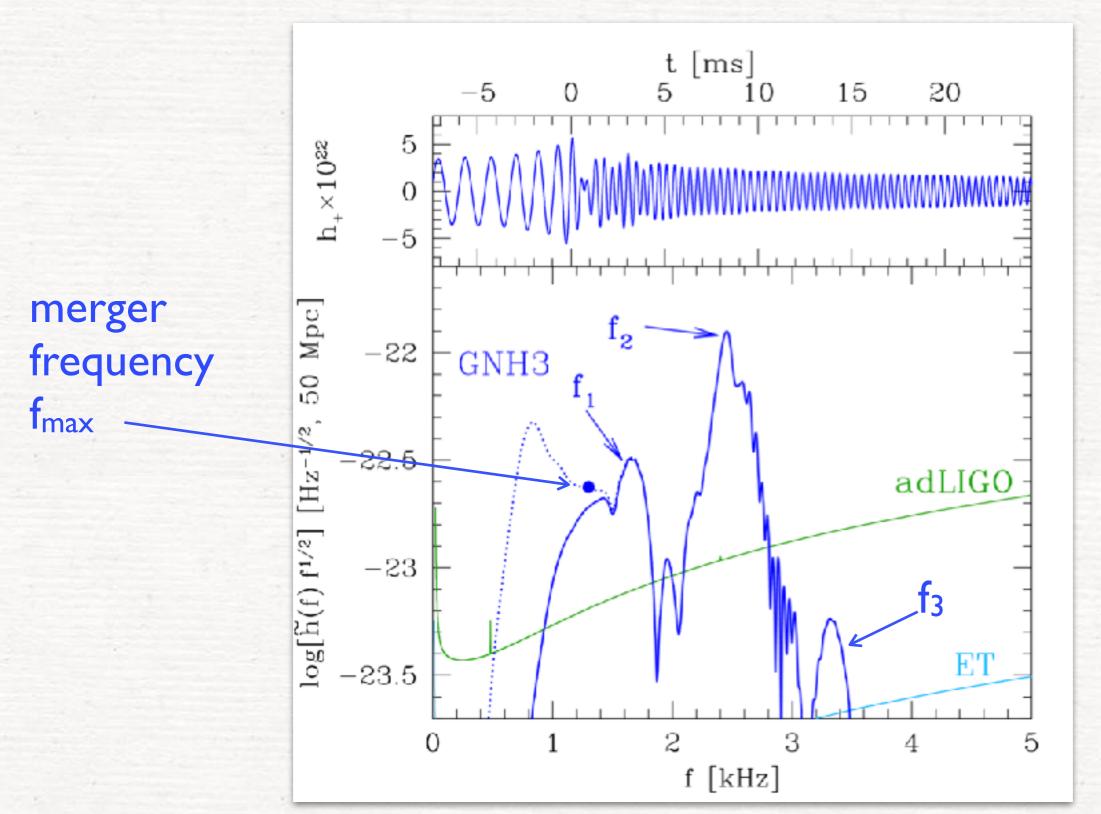
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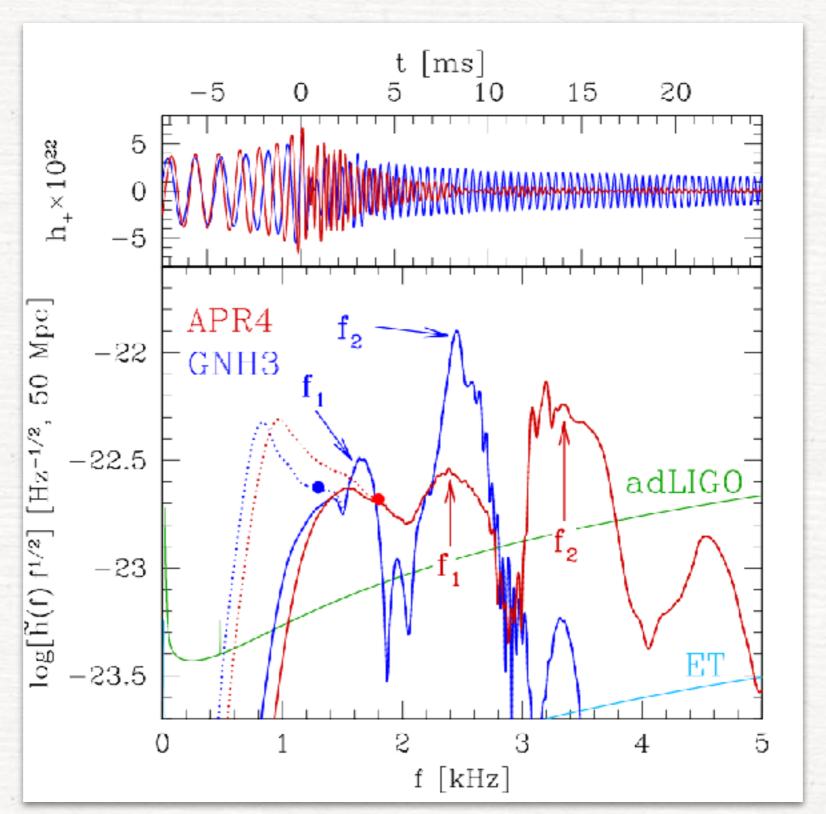
### A new approach to constrain the EOS

Oechslin+2007, Baiotti+2008, Bauswein+ 2011, 2012, Stergioulas+ 2011, Hotokezaka+ 2013, Takami 2014, 2015, Bernuzzi 2014, 2015, Bauswein+ 2015, Palenzuela+ 15, Lehner+ 2016, LR+2016...



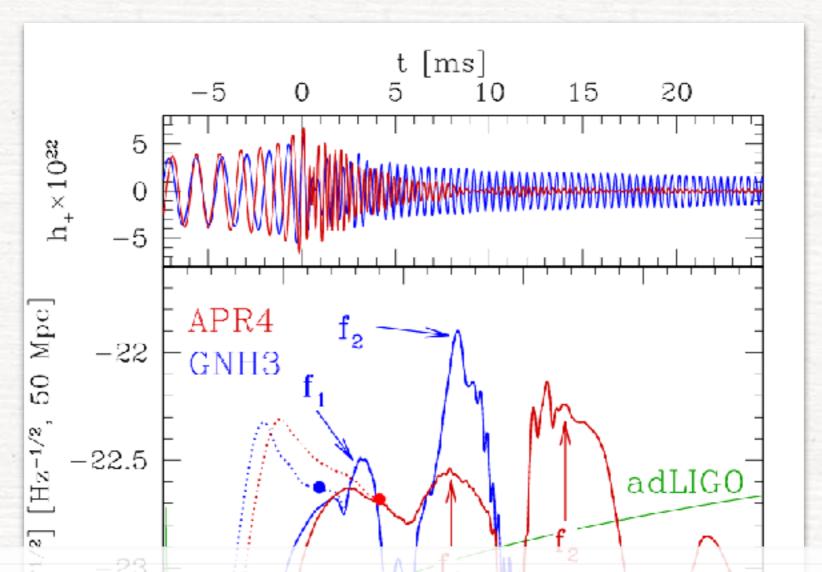
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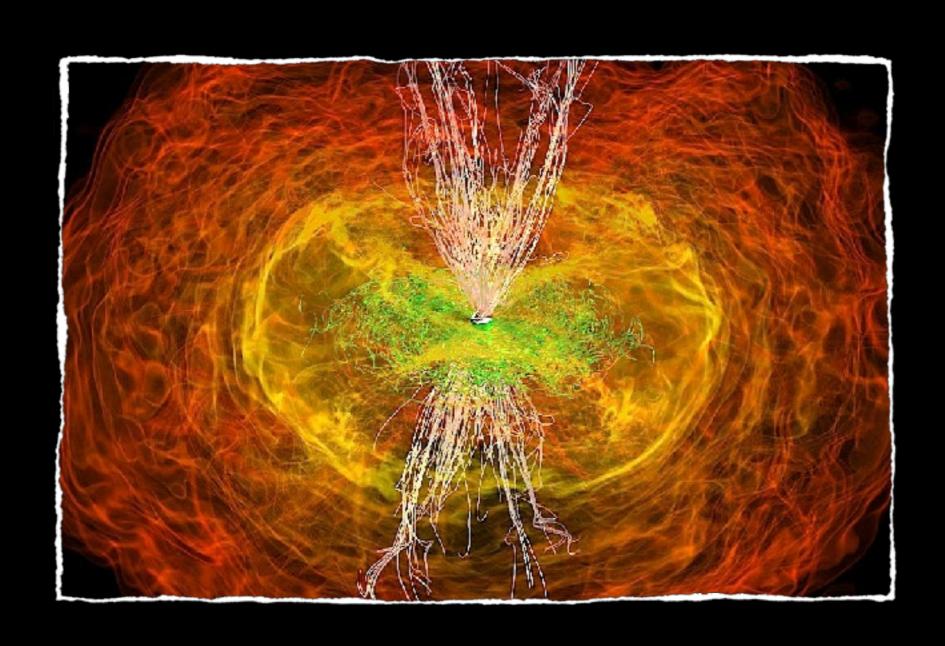
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We now know how to relate these frequencies to the property of the stars! We only need a "golden binary"!...

# Electromagnetic counterparts



# Electromagnetic counterparts

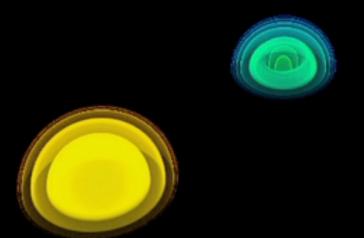
- Already in the 70's, astronomers realised that very rapid flashes of gamma rays are observed regularly by satellites
- These flashes come from most remote corners and have enormous energies of  $10^{50-53}$  erg: gamma-ray bursts.
- There are two families of bursts: "long" and "short"
- The first ones last **tens** or more of **seconds** and seem to be due to the collapse of very massive stars.
- The second ones last less than a second.
- Merging neutron stars always though to be most reasonable explanation but how do you produce a **jet**?



What happens when magnetised stars collide?

#### What happens when magnetised stars collide?

# Need to solve equations of magnetohydrodynamics in addition to the Einstein equations



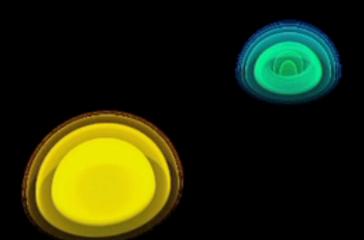
$$M = 1.5 M_{\odot}, B_0 = 10^{12} \,\mathrm{G}$$

Animations:, LR, Koppitz

11.75

14.5

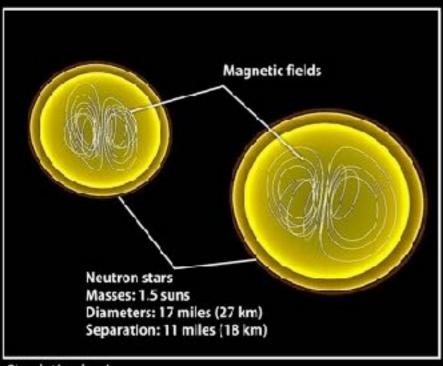


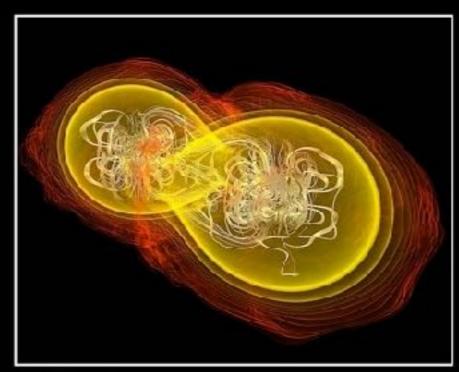


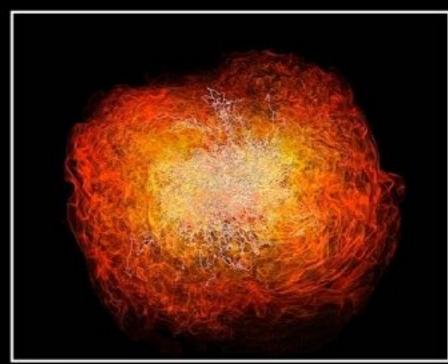
11.75 9.5 12 14.5 14.5 lg(|B|) [Gauss]

lg(rho)[g/cm³]

#### What happens when magnetised stars collide?



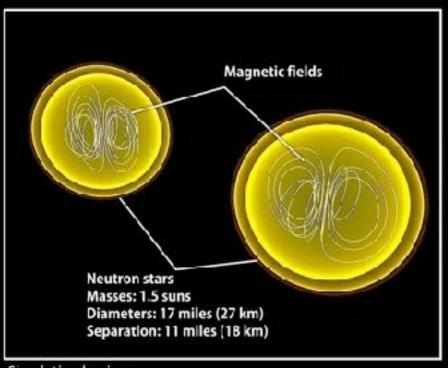


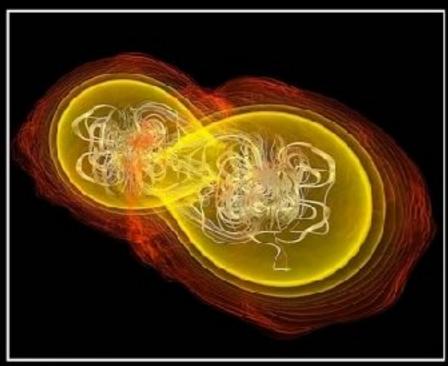


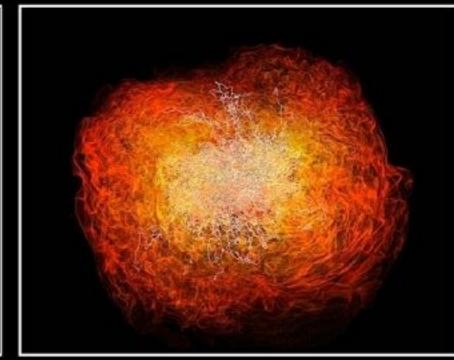
Simulation begins 7.4 milliseconds

13.8 milliseconds

#### What happens when magnetised stars collide?





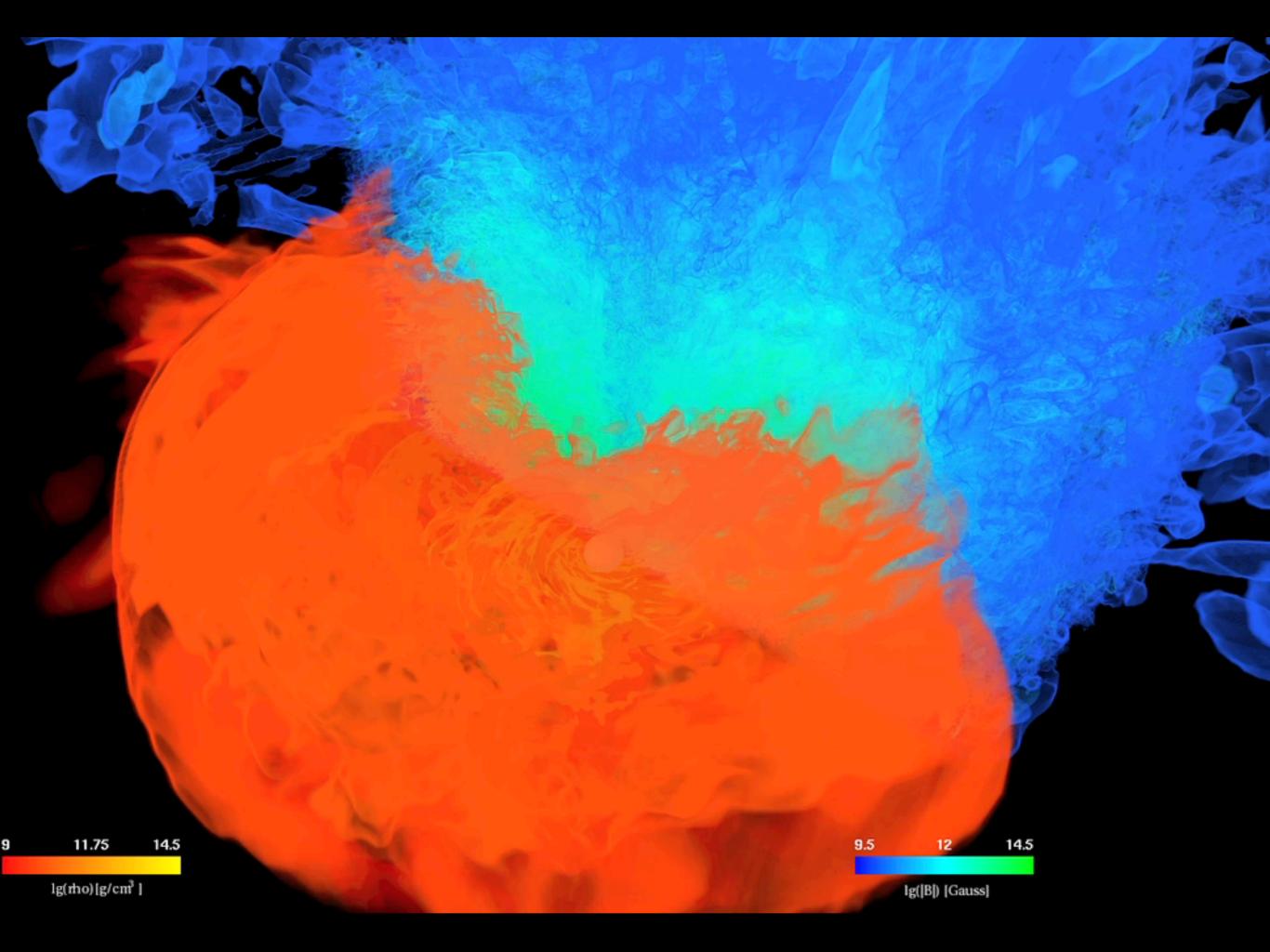


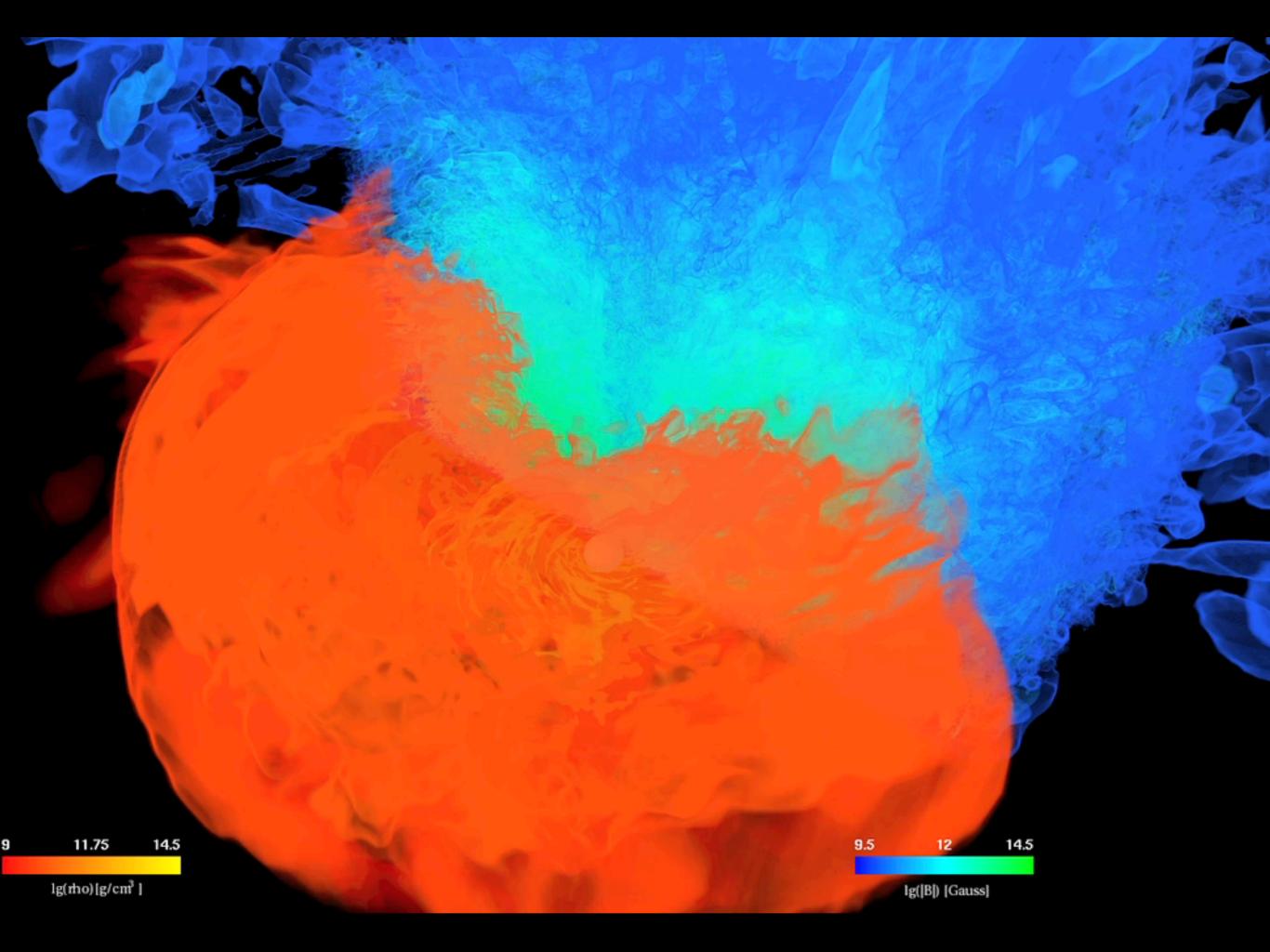
Simulation begins

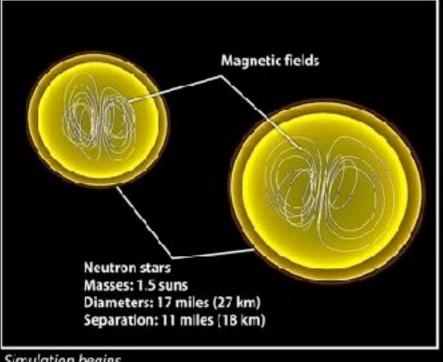
7.4 milliseconds

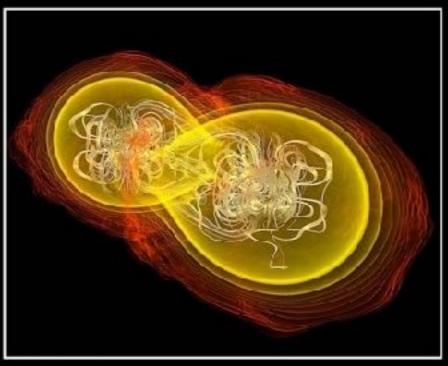
13.8 milliseconds

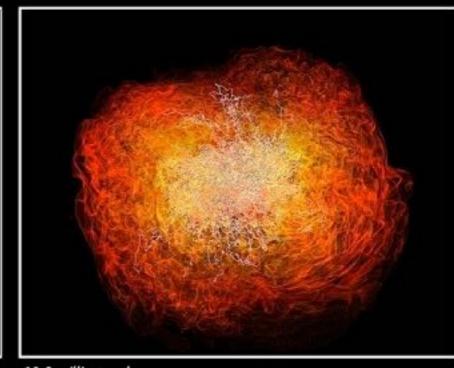
Magnetic fields in the HMNS have complex topology: dipolar fields are destroyed.







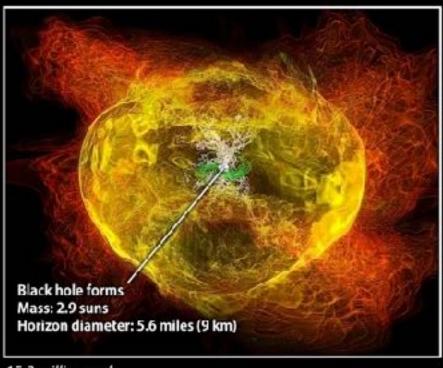




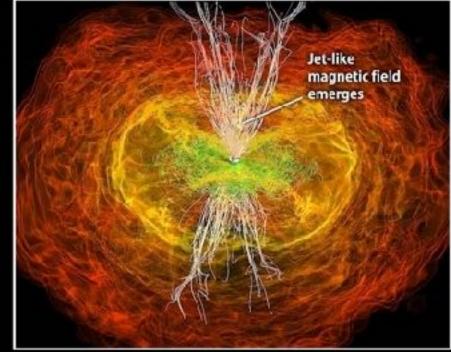
Simulation begins

7.4 milliseconds

13.8 milliseconds







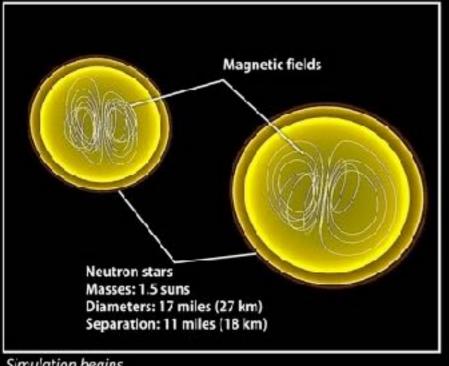
15.3 milliseconds

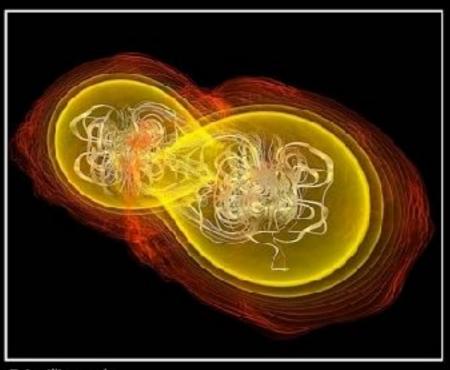
21.2 milliseconds

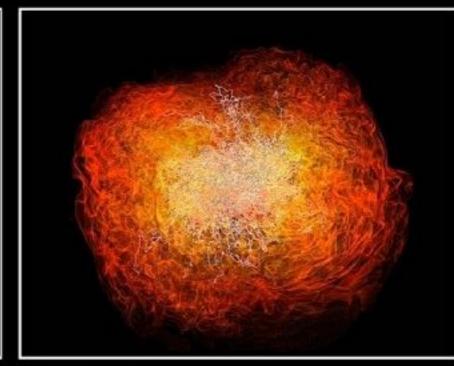
26.5 milliseconds

 $\overline{J/M^2} = 0.83$ 

Credit: NASA/AEI/ZIB/M. Koppitz and L. Rezzolla  $M_{\rm tor} = 0.063 M_{\odot}$   $t_{\rm accr} \simeq M_{\rm tor}/\dot{M} \simeq 0.3 {
m s}$ 



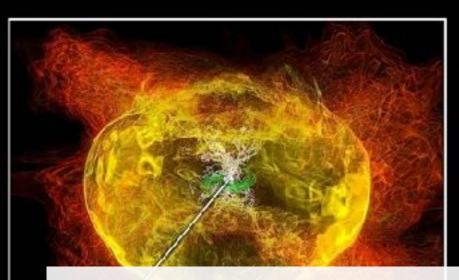




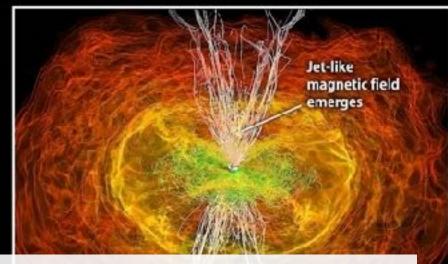
Simulation begins

7.4 milliseconds

13.8 milliseconds



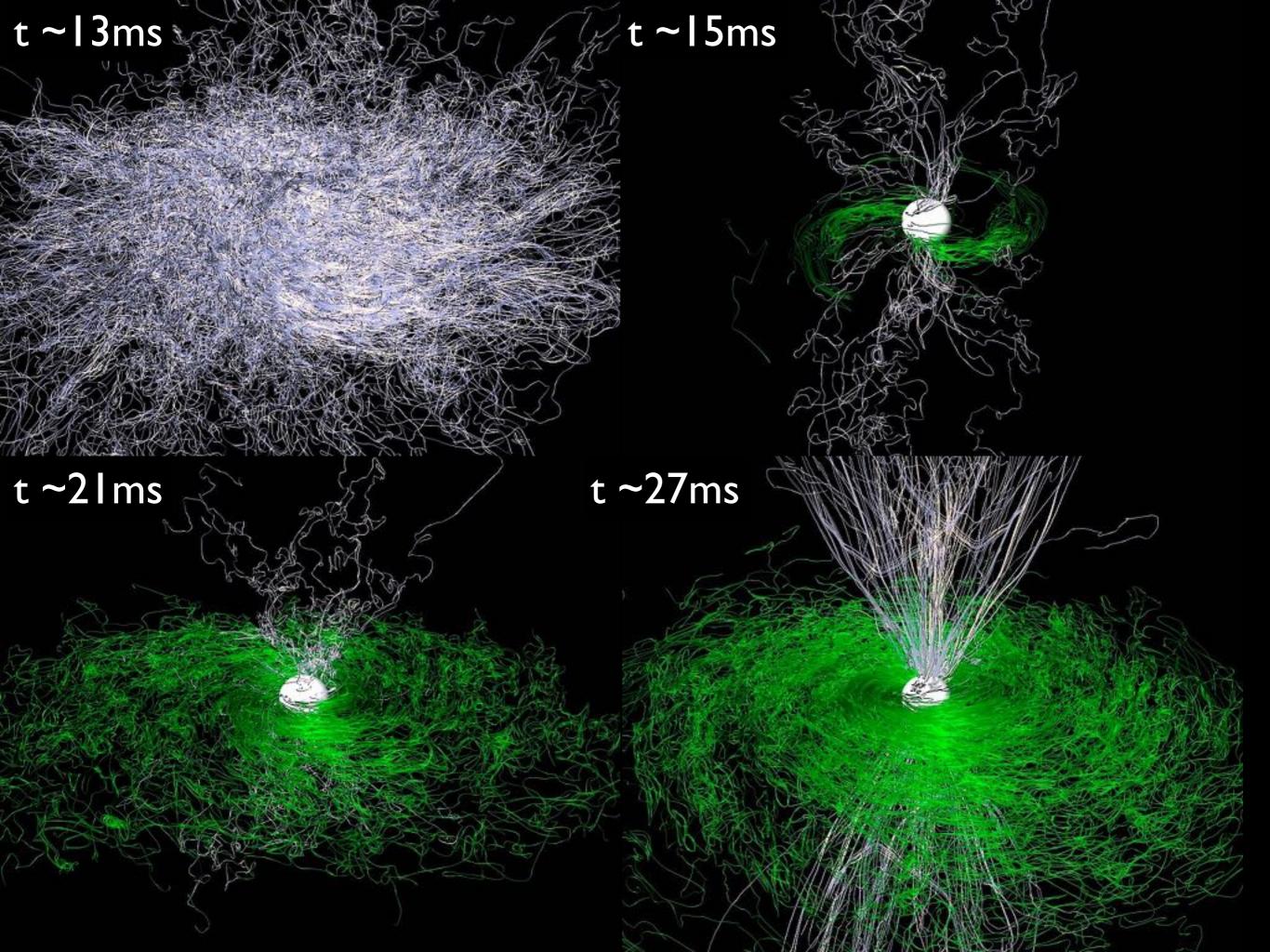




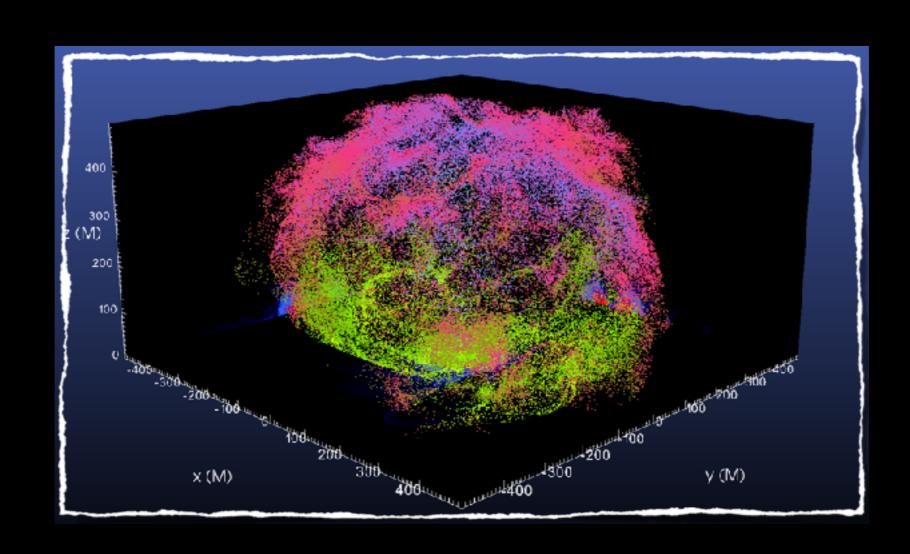
These simulations have shown that the merger of a magnetised binary has all the basic features behind SGRBs

 $J/M^2 = 0.83$ 

 $M_{\rm tor} = 0.063 M_{\odot}$   $t_{\rm accr} \simeq M_{\rm tor}/M \simeq 0.3 {
m s}$ 

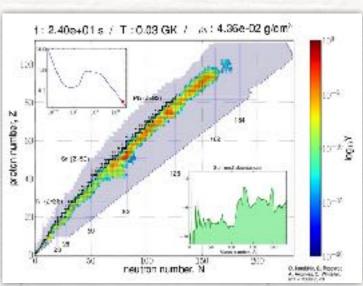


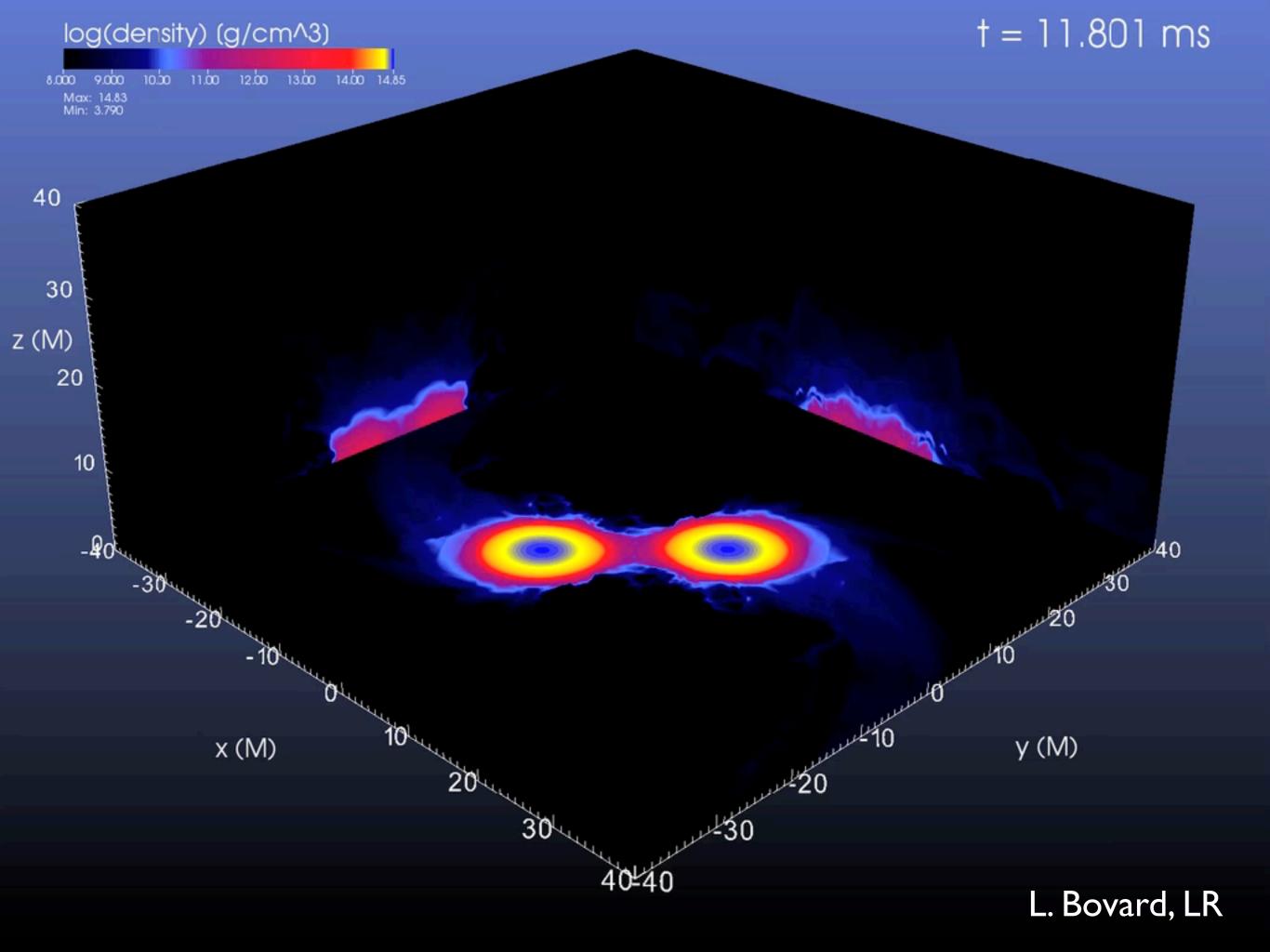
# Ejected matter and nucleosynthesis

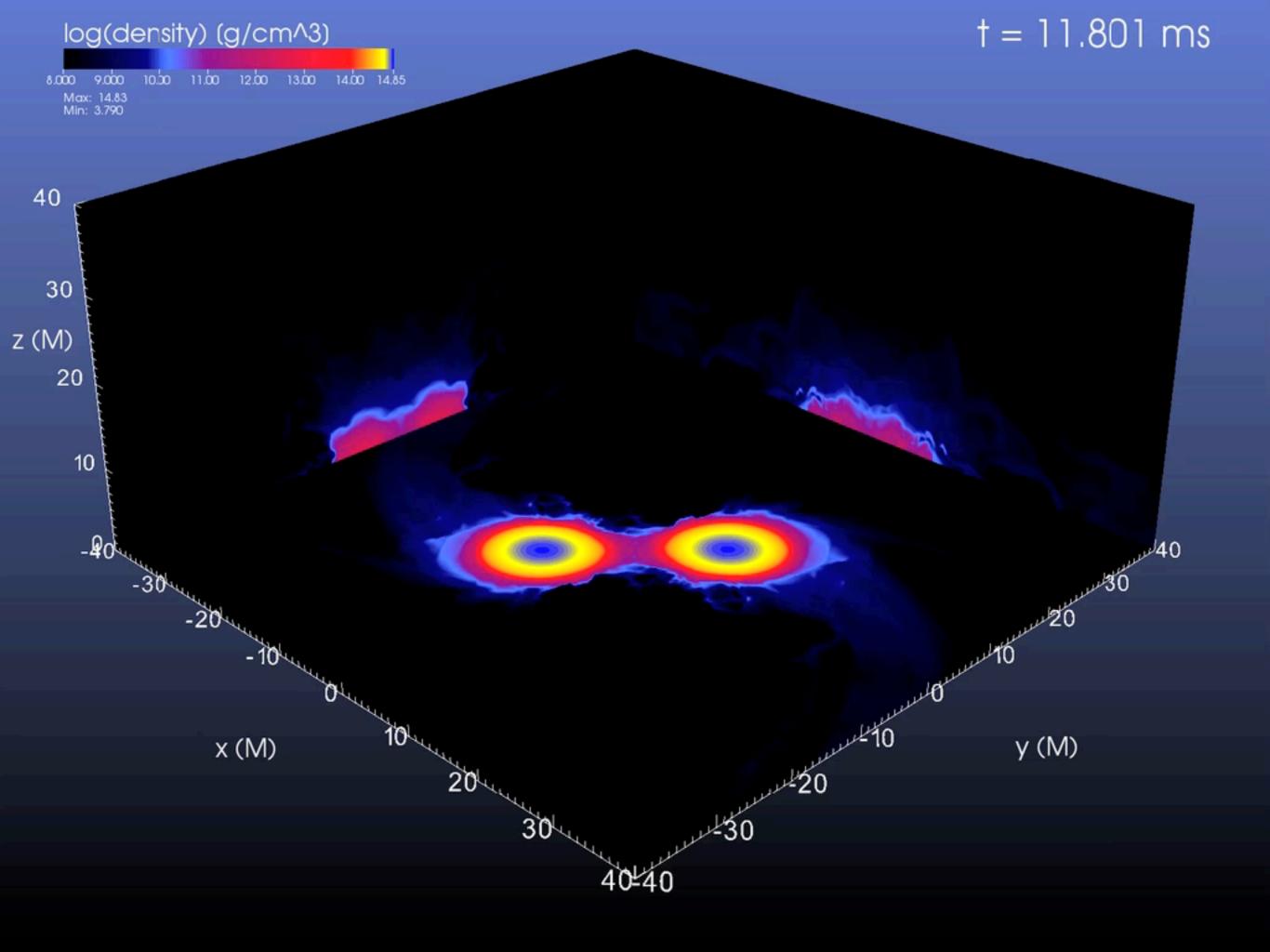


## Nucleosynthesis

- Already in the 50's, nuclear physicists had tracked the production of elements in stars via nuclear fusion.
- •Heavy elements  $(A \gtrsim 56)$  cannot be produced in stellar interiors but can be synthesised during a supernova.
- •Modern numerical simulations of supernovae have shown that the temperature and energies are not large enough to produce the "very heavy" elements  $(A \gtrsim 120)$ .
- To produce such elements one needs very high temperatures and "neutron-rich" material.
- Neutron-star mergers seem perfect candidates for this process!





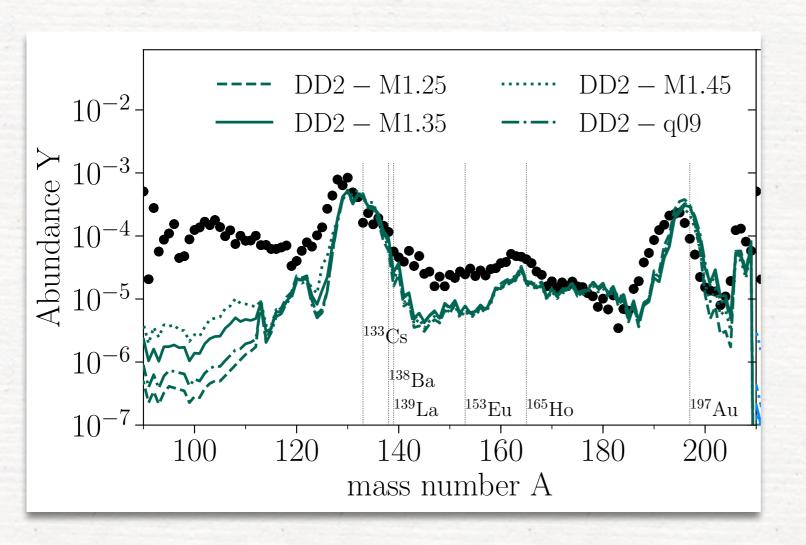


• Abundance pattern for A>120 in good agreement with solar.

- Abundance pattern for A > 120 in good agreement with solar.
- Even tiny amounts of ejected matter  $(0.01 M_{\odot})$  sufficient to explain observed abundances.

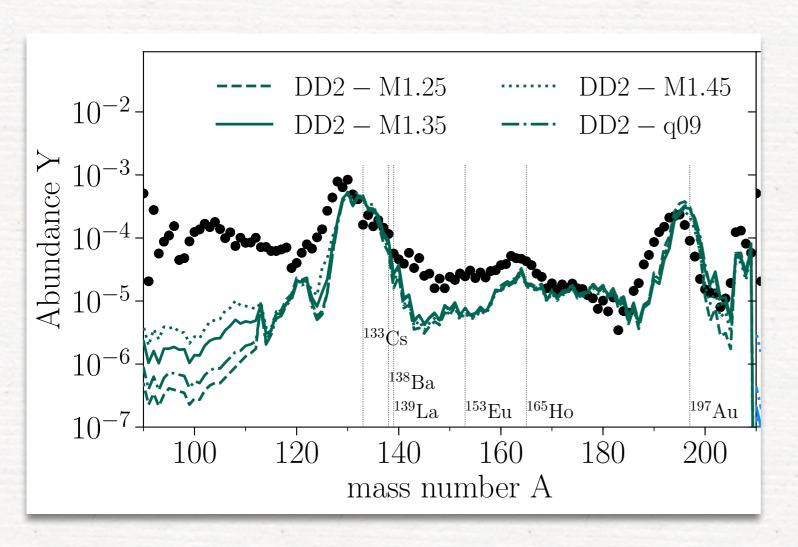
Bovard+ 17

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Bovard+ 17

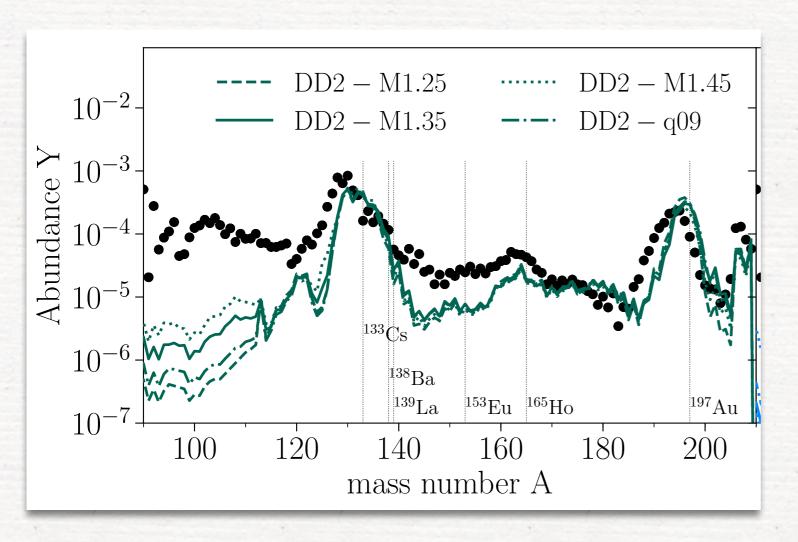
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• GW170817 produced total of 16,000 times the mass of the Earth in heavy elements (10 Earth masses in gold/platinum)

Bovard+ 17

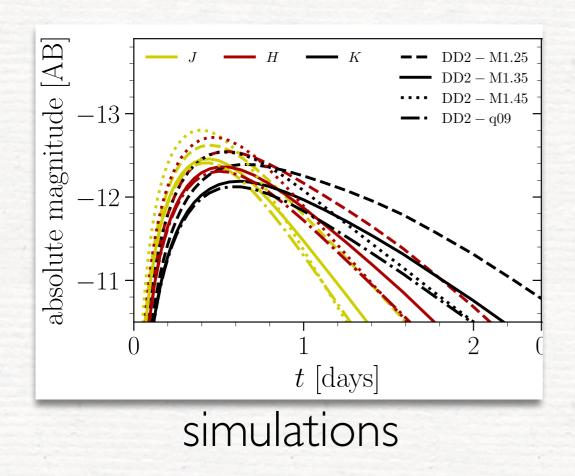
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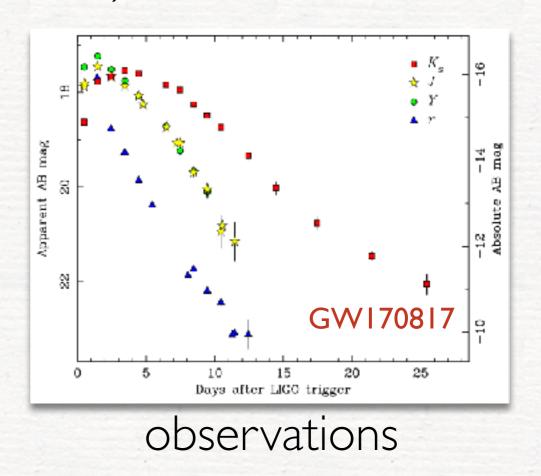


- GW170817 produced total of 16,000 times the mass of the Earth in heavy elements (10 Earth masses in gold/platinum)
- We are not only stellar dust but also neutronstar dust!

#### Kilonova emission

- Ejected matter undergoes nucleosynthesis as expands and cools.
- When critical densities and temperatures are reached, matter undergoes radioactive decay emitting light (optical/infrared): kilonova/macronova (Li & Paczynski '98).





 Astronomical observations of GW170817 show kilonova emission: evidence connection GRBs and binary neutron stars!

#### Conclusions

- \* Binary neutron stars are arguably Einstein's richest laboratory.
- \*They combine extreme gravity with some of the most extreme states of matter in the universe.
- \* Exploring these objects requires advanced mathematical and numerical methods and the power of supercomputers.
- \* Gravitational waves from these systems can teach us a lot about gravity, nuclear physics and solve astrophysical puzzles.
- \* A single detection (GW170817) has already provided us with a wealth of information: more are to come in the near future.

Working in this area has never been as exciting!...